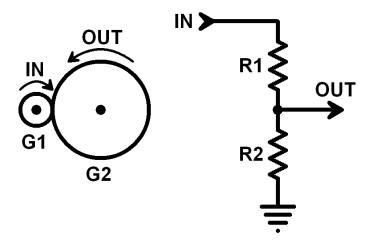
CMPSCI 145 MIDTERM #1
Solution Key
SPRING 2020
February 28, 2020
Professor William T. Verts

<1> 10 Points – Examine the following diagram of two systems, one involving gears and the other involving resistors. Resistor **R1** is 3000 Ohms, and resistor **R2** is 1500 Ohms. Gear **G1** has 20 teeth.



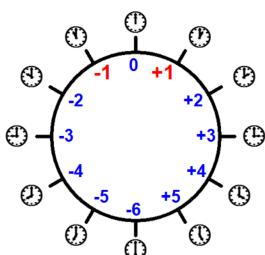
- A. (5 points) What is the output voltage of the circuit if the input voltage was 60 volts? 20 volts
- B. (5 points) How many teeth must gear **G2** have so that the division ratio of the gears matches the division ratio of the resistors? (Ignoring differences in sign.)

 60 teeth
- <2> 10 Points The image to the right shows a standard 12-hour clock, where the 12:00 position represents zero.

A. (1 point) Indicate on the diagram where +1 and -1 are located in a signed interpretation. (Required positions shown in red)

B. (3 points each, 1 point for sum, 2 points for the overflow) Compute the following sums, and tell me if there is an unsigned overflow, a signed overflow, both or neither:

$$(1)+(1)=(1)_{(3+7=10) \text{ neither}}$$
 $(1)+(1)=(1)_{(10+7=5, -2+-5=+5) \text{ both}}$



<3> 18 Points (1 point each box) – Show the *decimal* (base 10) value of the four-bit binary numbers interpreted in each of the following ways. For signed interpretations, the leftmost bit is the sign bit.

The Number	0101	1111	1010
Unsigned Binary	5	15	10
Sign & Magnitude Signed Binary	+5	-7	-2
One's Complement Signed Binary	+5	-0	-5
Two's Complement Signed Binary	+5	-1	-6
BCD (if illegal answer ERROR)	5	ERROR	ERROR
Excess-3 (if illegal answer ERROR)	2	ERROR	7

- <4> 15 Points A new floating-point system uses 20 bits per number: 1 for the sign bit, 6 for the biased exponent, and 13 for the mantissa.
 - A. (2 points) What is the <u>bias</u> value for this format? $2^{6-1}-1=2^5-1=32-1=31$ (Accept any of the forms shown above)
 - B. (3 points) Write into the boxes below the binary value for +infinity?

(1 point each for sign, exponent, and mantissa, remove ½ per section for minor errors)

C. (5 points) Write into the boxes below the binary value for -1.0?

(1 point for sign, 2 for exponent, 2 for mantissa, -½ per minor error)

D. (5 points) Write into the boxes below the binary value for the number that has the binary scientific notation value of +1.1001101110101010101011×2⁵ (round up any bits that don't fit into the mantissa). Rounded bits shown in blue.

0 1 0 0 1 0 0 1 0 0 1 1 0 0 1 1 0 0 0

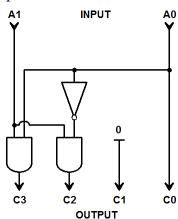
(1 point for sign, 2 for exponent, 2 for mantissa, -½ per minor error)

- <5> 10 Points (5 points each) An analog computation system can continuously represent any number between 0 and 10 (inclusive), but no other values. The scale markings are good to one digit to the right of the decimal point (that is, 0.0, 0.1, 0.2, ..., 9.9, 10.0).
 - A. What happens when the computation 1.5×2.3 is attempted? The product, 3.45, **requires more digits of precision** than are marked on the scale, so **the answer will not fall exactly on a scale mark** (but will be **halfway between** 3.4 and 3.5). Score as 5 points (they mostly get it), 3 (some right, some wrong/incomplete), 1 (a little bit there), or 0 (blank or not even close).
 - B. What happens when the computation 6.9×7.2 is attempted?

 Overflow. The product, 49.68, is larger than the maximum value of 10 that the device can accommodate. Score as 5 points (they mostly get it), 3 (some right, some wrong/incomplete), 1 (a little bit there), or 0 (blank or not even close).
- <6> 10 Points (2 points each) Which of the following are analog and which are digital?

A. A watch with a sweep second hand.
B. A NAND-gate.
C. A hydraulic press.
Digital
D. A light switch.
E. An odometer in a car with a moving needle.
Analog
Analog

<7> 16 Points – (1 point each) Trace the following circuit and show the outputs for all given inputs.



A1	A0	C3	C2	C1	C0
0	0	0	0	0	0
0	1	0	0	0	1
1	0	0	1	0	0
1	1	1	0	0	1

5 Points Extra Credit: What function does this circuit perform?

The output is the square of the input.

<8> 11 Points – SHORT ANSWER – The Inuit peoples of icy Greenland don't use paper maps, but instead use carved wooden maps as shown below here. What are the representational trade-offs between the two forms? Why might I use one over the other? Answer on the back of this page.



Paper is **difficult to obtain** in Greenland, paper is **not very sturdy when wet**, and paper maps **have to be unfolded** in order to be studied.

In contrast, wooden maps are **rugged**, and can be used and **studied by feel** in cold weather without removing them from inside warm mittens. They also provide a **tactile sense of 3D topology** not possible with flat paper.

I don't expect all students to get all of these reasons, and I do expect that some will come up with valid reasons not covered here. As long as they come up with a valid reason *against* paper <u>and</u> a valid reason *for* wood, they should get full credit.

Score as 11 points (they mostly get it), 6 (some right, some wrong or missing), 3 (a little bit there but not much), or 0 (blank or not even close).