

# CS 383: Artificial Intelligence

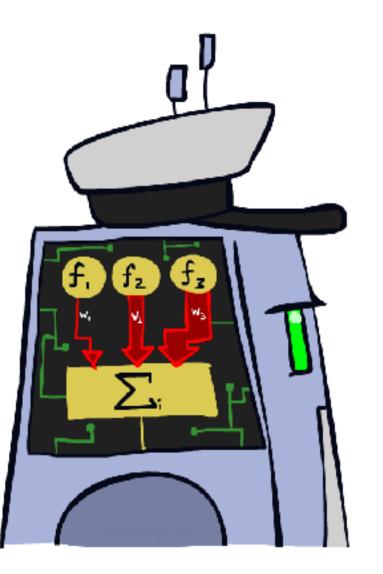
**Deep Learning** 

Prof. Scott Niekum — UMass Amherst

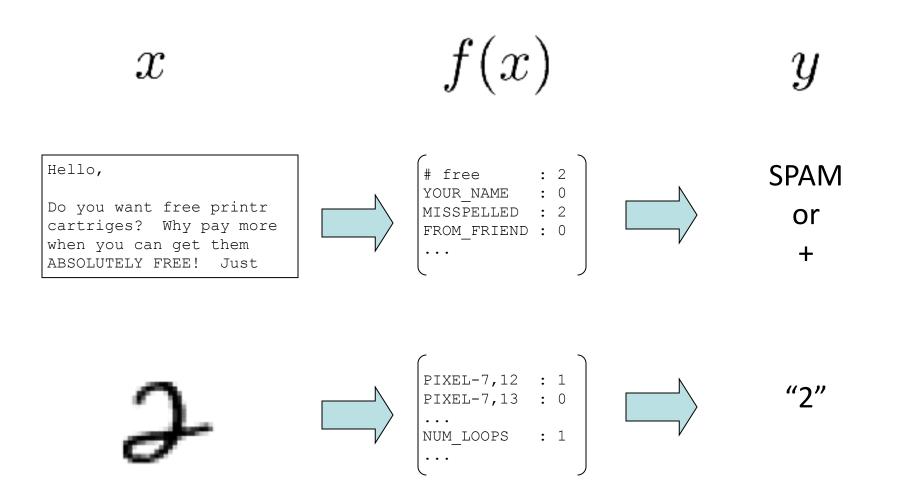
[These slides based on those of Dan Klein, Pieter Abbeel, Anca Dragan for CS188 Intro to AI at UC Berkeley. All CS188 materials are available at http://ai.berkeley.edu.]

### Please fill out course evals online!

#### **Review: Linear Classifiers**

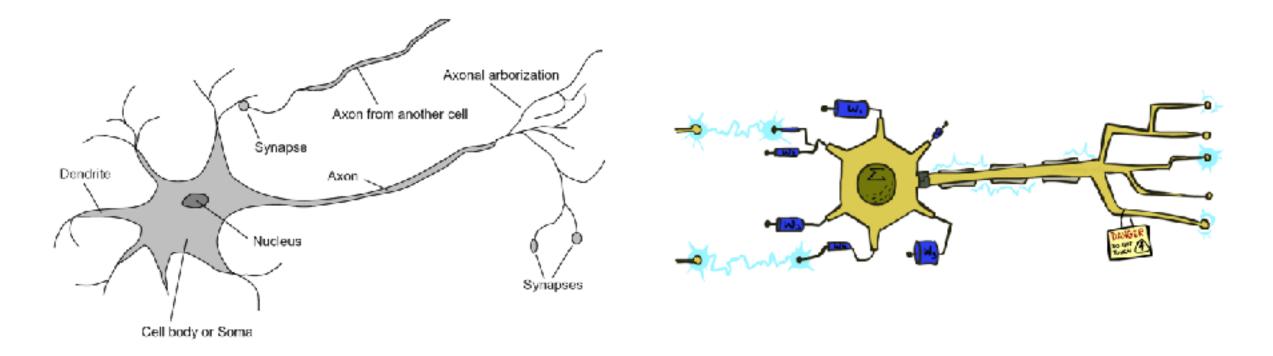


#### **Feature Vectors**



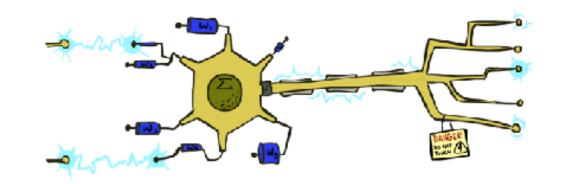
# Some (Simplified) Biology

#### Very loose inspiration: human neurons



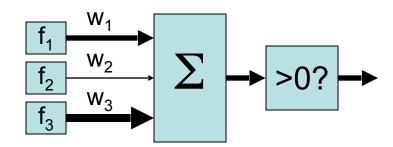
# Linear Classifiers

- Inputs are feature values
- Each feature has a weight
- Sum is the activation

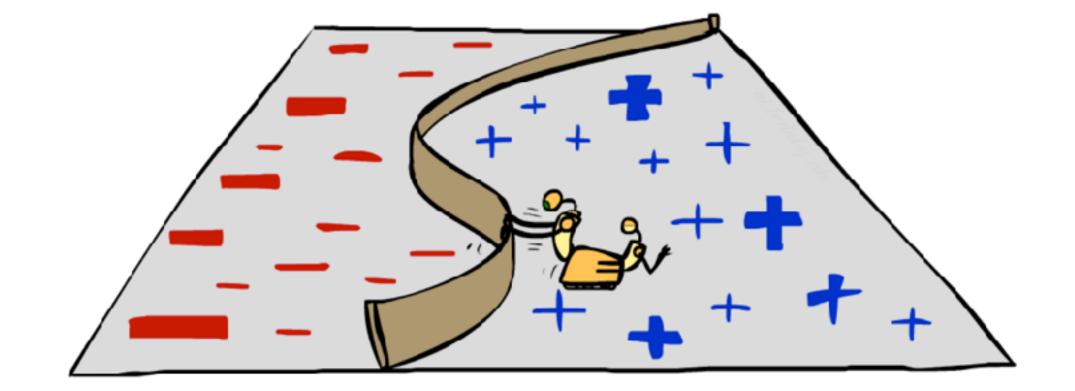


activation<sub>w</sub>(x) = 
$$\sum_{i} w_i \cdot f_i(x) = w \cdot f(x)$$

- If the activation is:
  - Positive, output +1
  - Negative, output -1

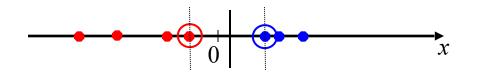


# Non-Linearity

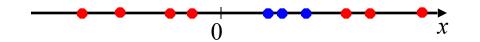


## **Non-Linear Separators**

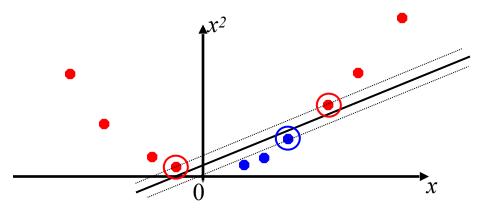
Data that is linearly separable works out great for linear decision rules:



But what are we going to do if the dataset is just too hard?



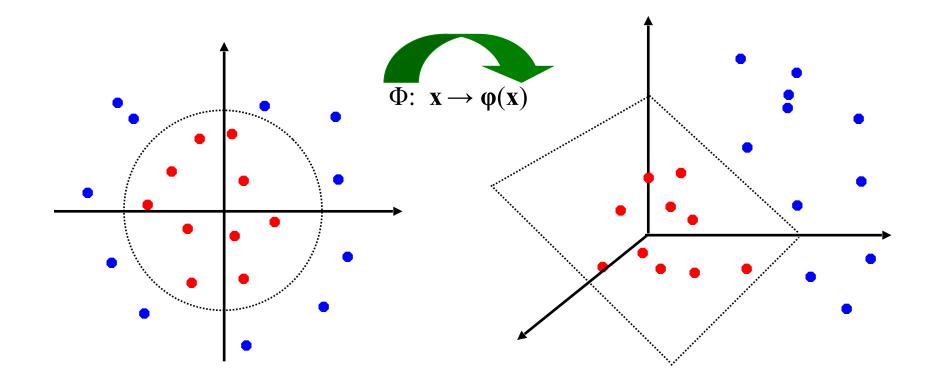
How about... mapping data to a higher-dimensional space:



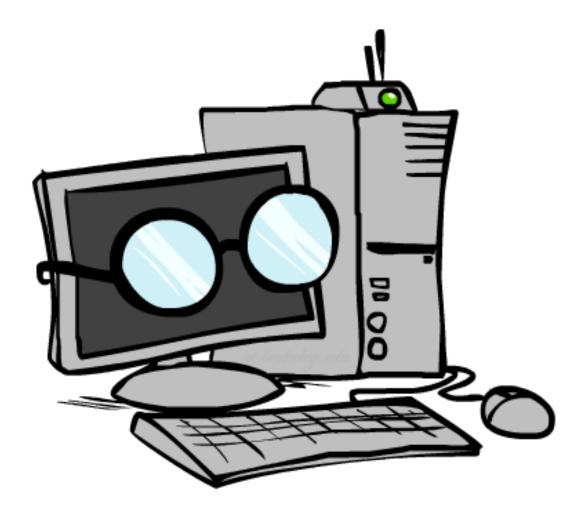
This and next slide adapted from Ray Mooney, UT

### **Non-Linear Separators**

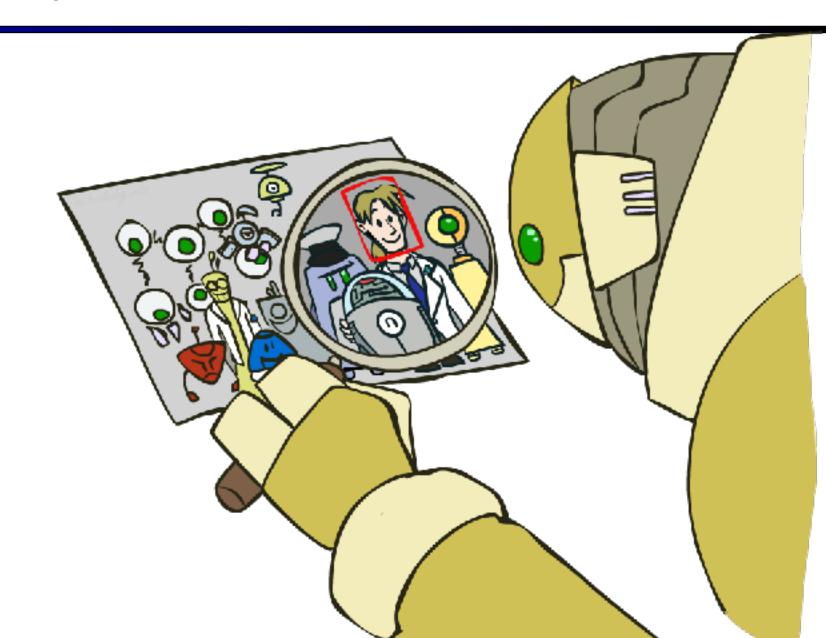
 General idea: the original feature space can always be mapped to some higherdimensional feature space where the training set is separable:



## **Computer Vision**

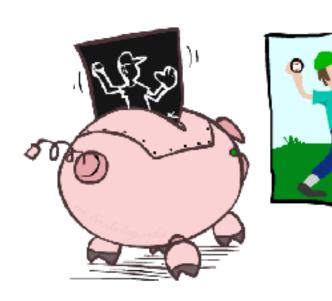


## **Object Detection**



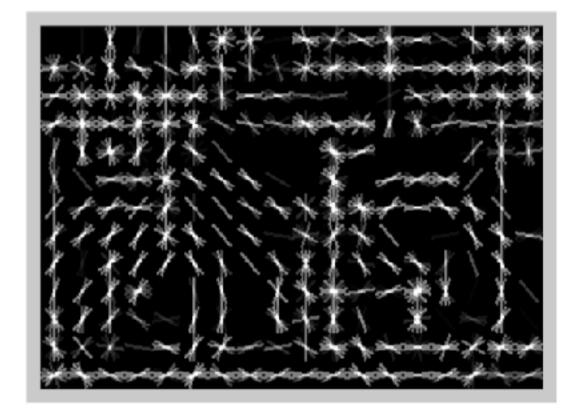
## Manual Feature Design







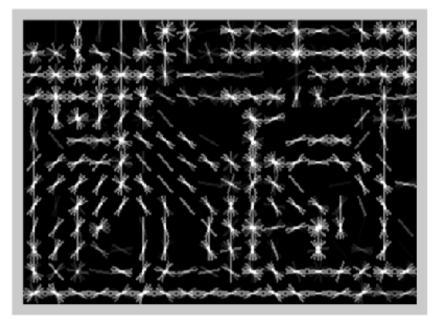
#### Features and Generalization



[Dalal and Triggs, 2005]

#### Features and Generalization

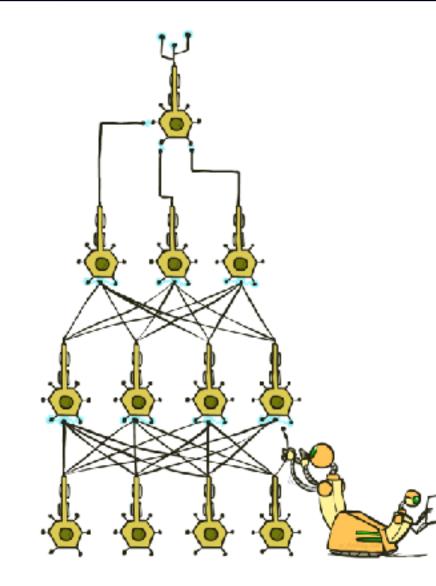




Image



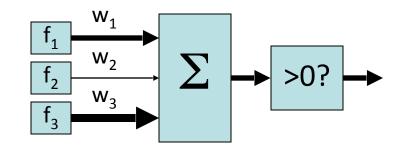
# Manual Feature Design →Deep Learning



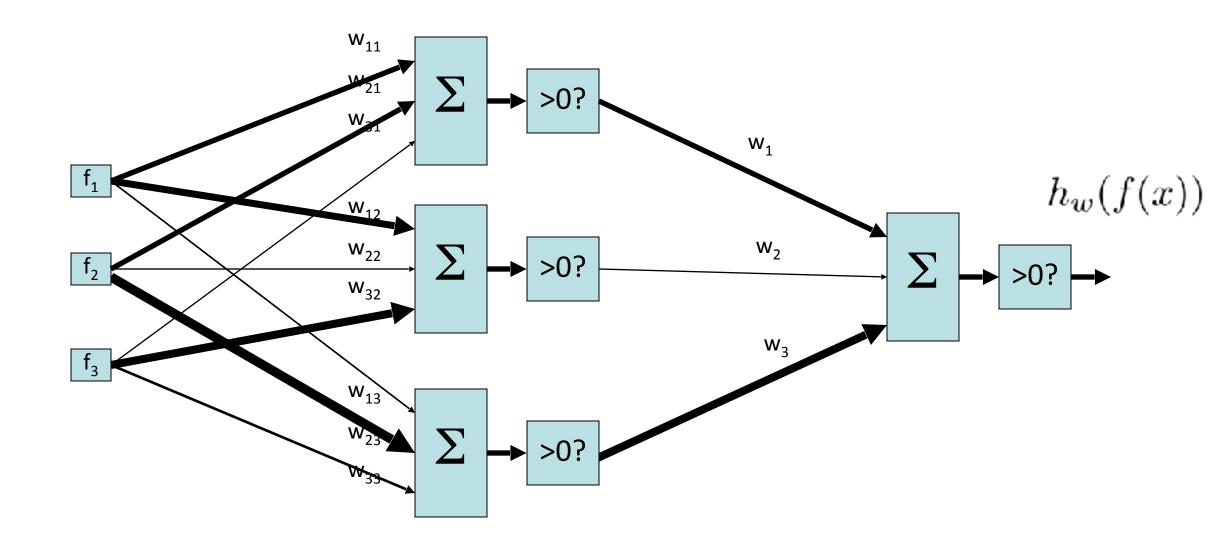
- Manual feature design requires:
  - Domain-specific expertise
  - Domain-specific effort

What if we could learn the features, too?
Deep Learning

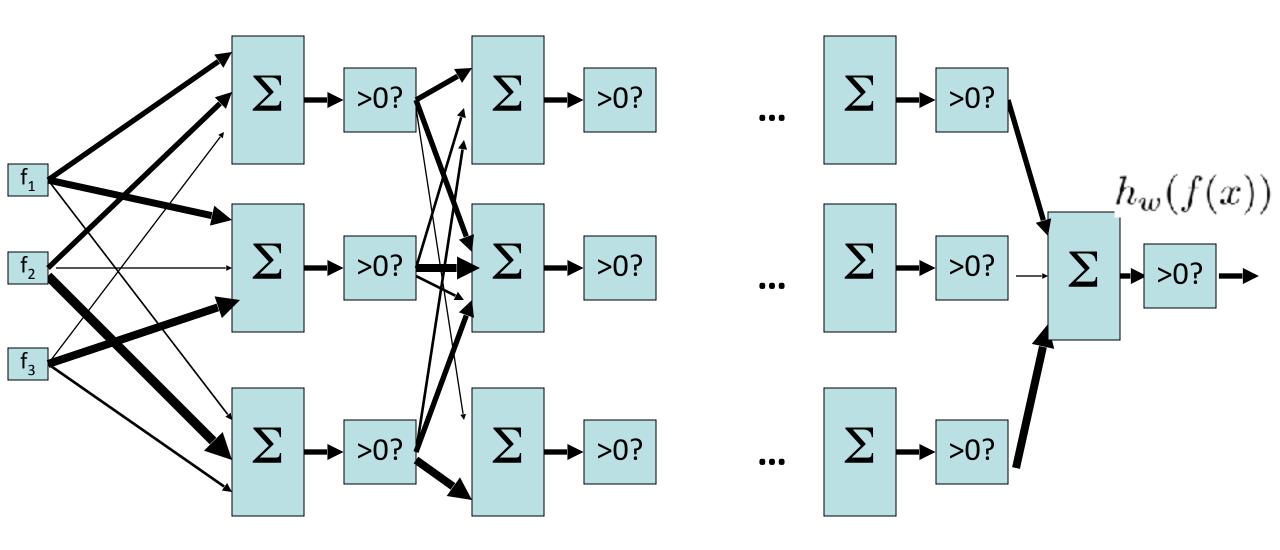
#### Perceptron



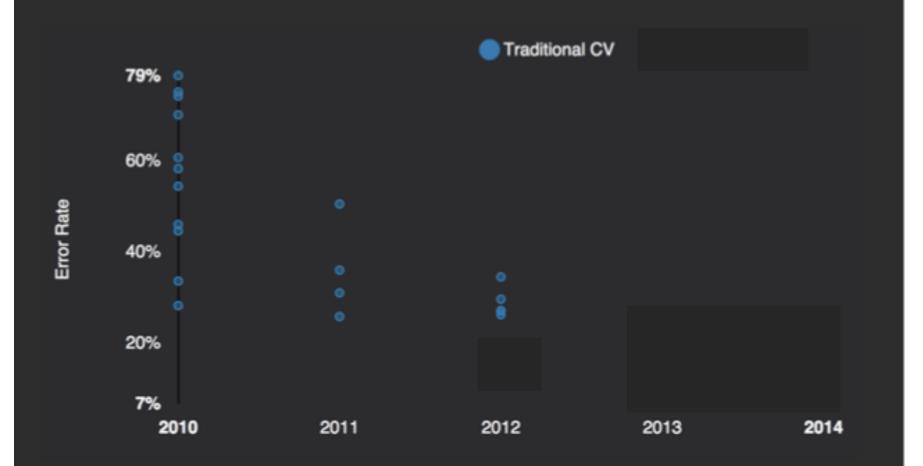
#### **Two-Layer Perceptron Network**



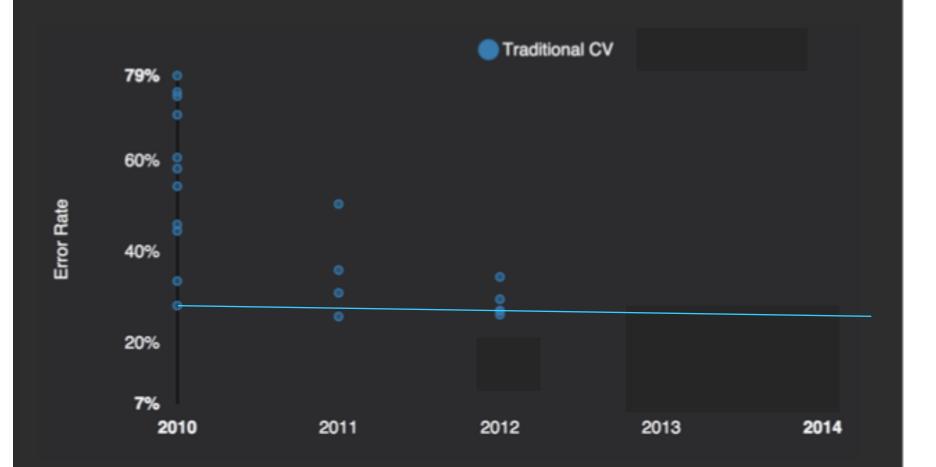
#### **N-Layer Perceptron Network**



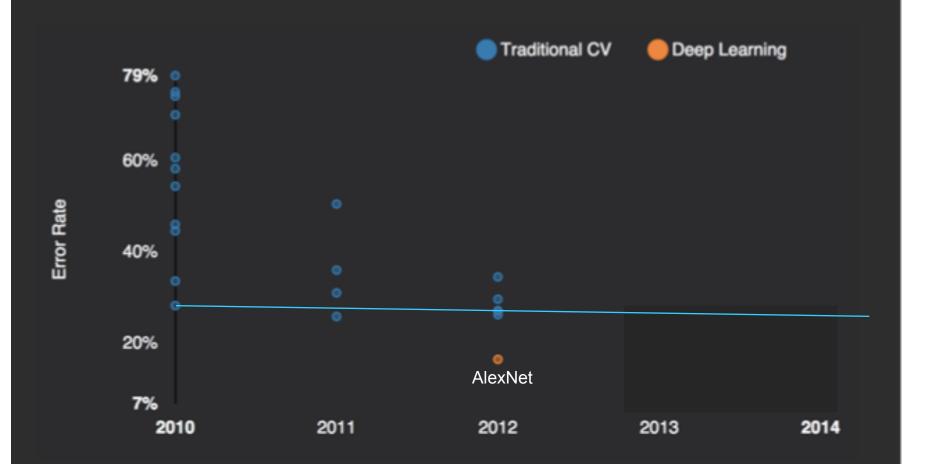
# ImageNet Error Rate 2010-2014



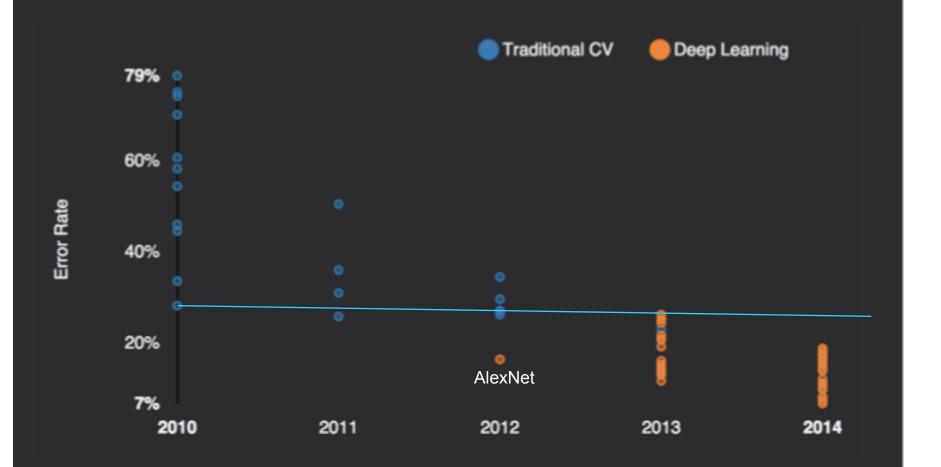
# ImageNet Error Rate 2010-2014



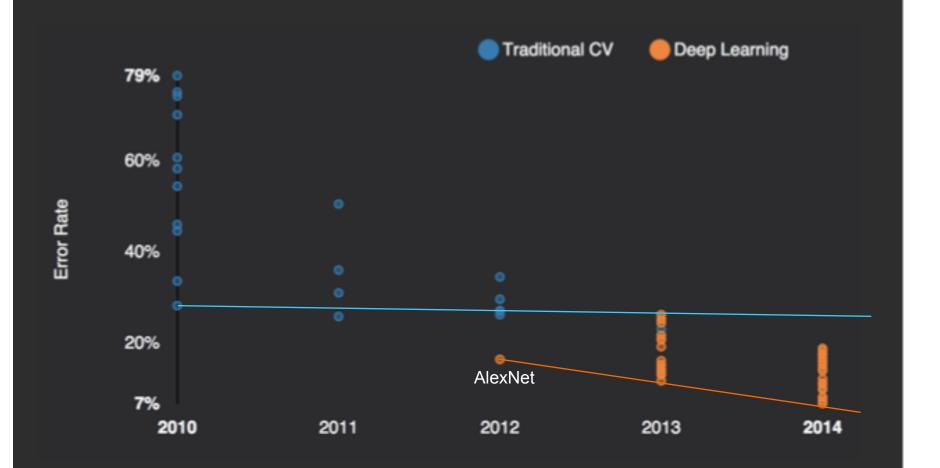
# ImageNet Error Rate 2010-2014



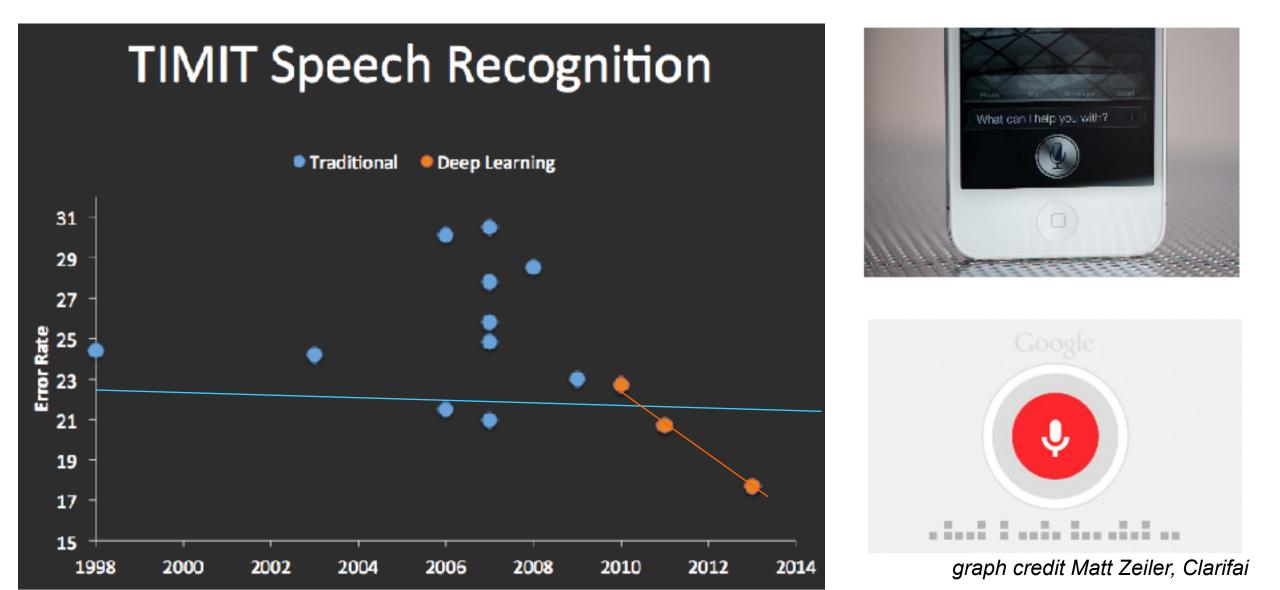
# ImageNet Error Rate 2010-2014



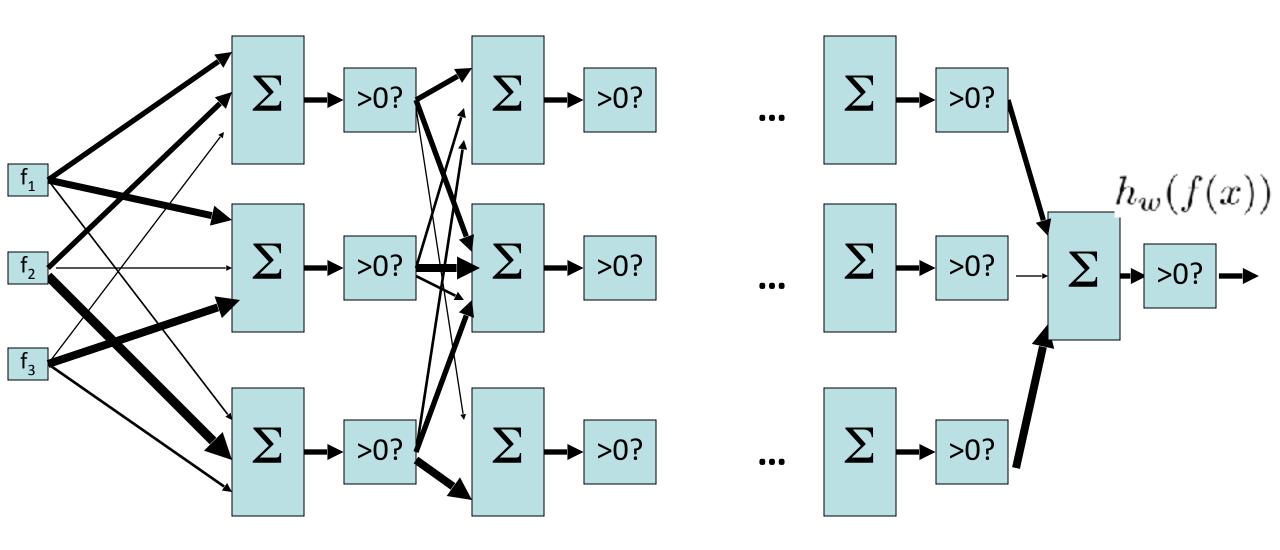
# ImageNet Error Rate 2010-2014



# Speech Recognition



#### **N-Layer Perceptron Network**



# Local Search

#### Simple, general idea:

- Start wherever
- Repeat: move to the best neighboring state
- If no neighbors better than current, quit
- Neighbors = small perturbations of w

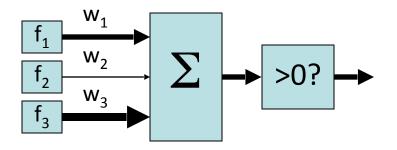
#### Properties

Plateaus and local optima

9.

How to escape plateaus and find a good local optimum? How to deal with very large parameter vectors? E.g.,  $w \in \mathbb{R}^{1billion}$ 

#### Perceptron



Objective: Classification Accuracy

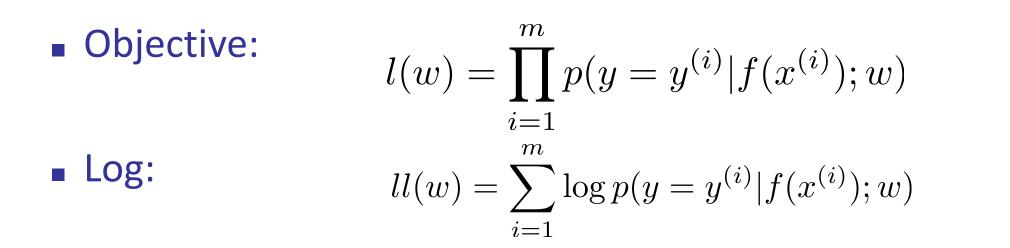
$$l^{\rm acc}(w) = \frac{1}{m} \sum_{i=1}^{m} \left( \operatorname{sign}(w^{\top} f(x^{(i)})) = y^{(i)} \right)$$

• Issue: many plateaus  $\rightarrow$  how to measure incremental progress toward a correct label?

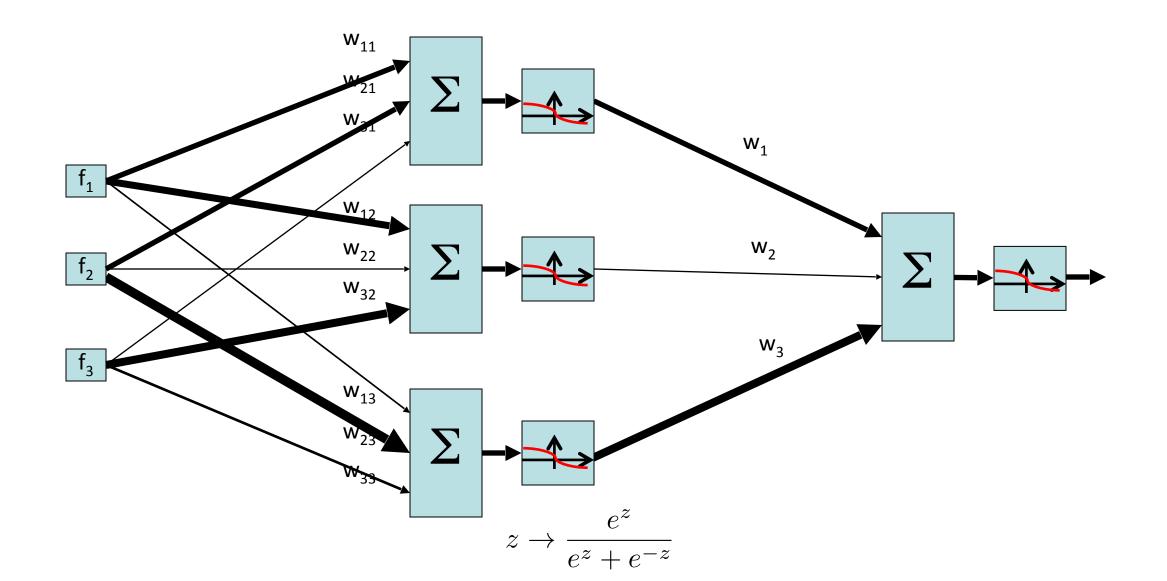
## Soft-Max

• Score for y=1:  $w^{\top}f(x)$  Score for y=-1:  $-w^{\top}f(x)$ 

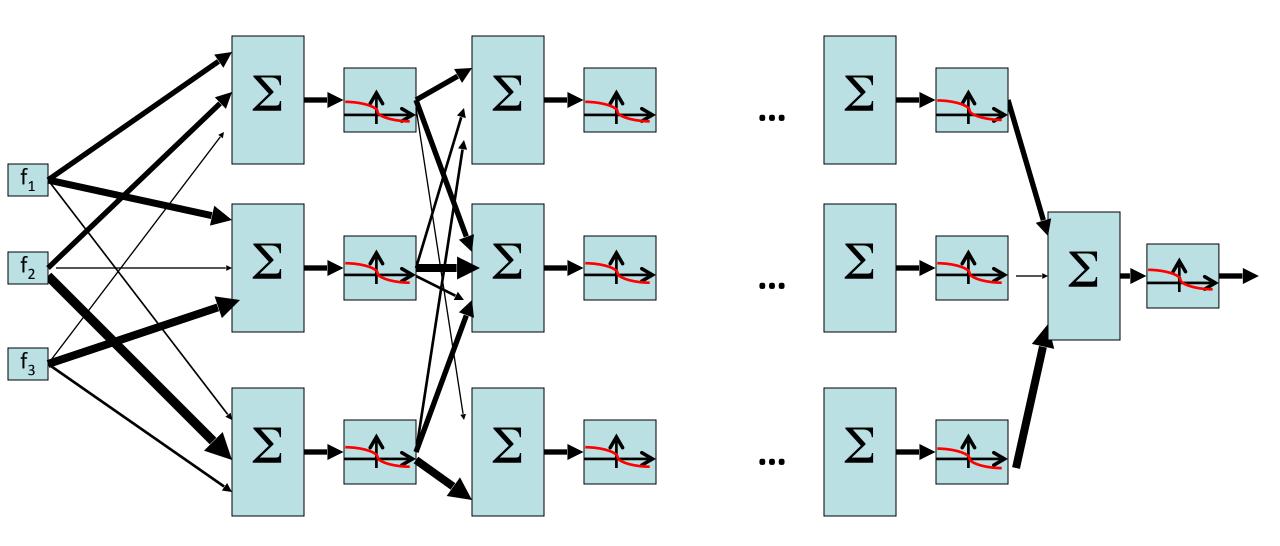
• Probability of label:  $p(y = 1|f(x); w) = \frac{e^{w^{\top}f(x^{(i)})}}{e^{w^{\top}f(x)} + e^{-w^{\top}f(x)}}$   $p(y = -1|f(x); w) = \frac{e^{-w^{\top}f(x)}}{e^{w^{\top}f(x)} + e^{-w^{\top}f(x)}}$ 



#### **Two-Layer Neural Network**



## **N-Layer Neural Network**



## **Our Status**

# • Our objective ll(w)

- Changes smoothly with changes in w
- Doesn't suffer from the same plateaus as the perceptron network

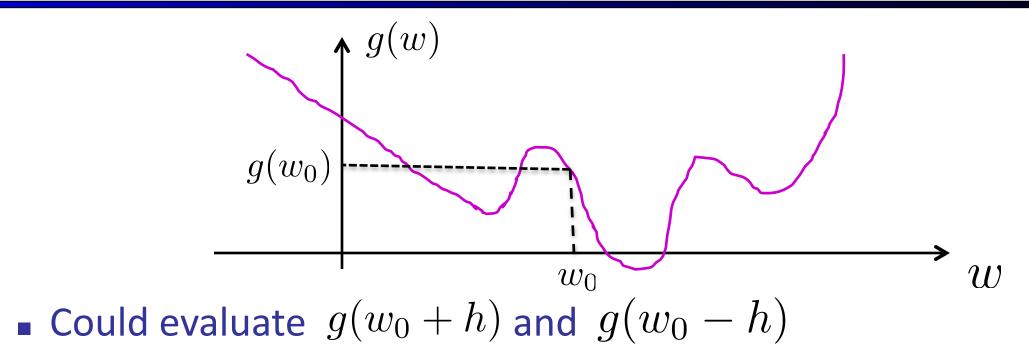
#### Challenge: how to find a good w ?

$$\max_{w} ll(w)$$

Equivalently:

$$\min_{w} -ll(w$$

# 1-d optimization

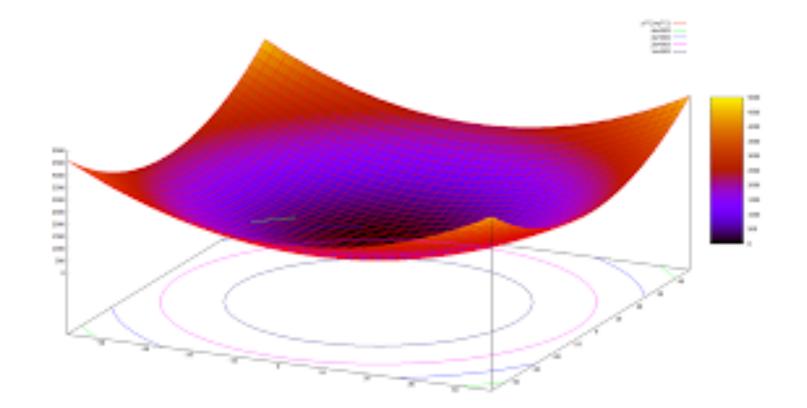


Then step in best direction

• Or, evaluate derivative: 
$$\frac{\partial g(w_0)}{\partial w} = \lim_{h \to 0} \frac{g(w_0 + h) - g(w_0 - h)}{2h}$$

Tells which direction to step in

# 2-D Optimization



Source: Thomas Jungblut's Blog

#### Steepest Descent

Idea:

- Start somewhere
- Repeat: Take a step in the steepest descent direction

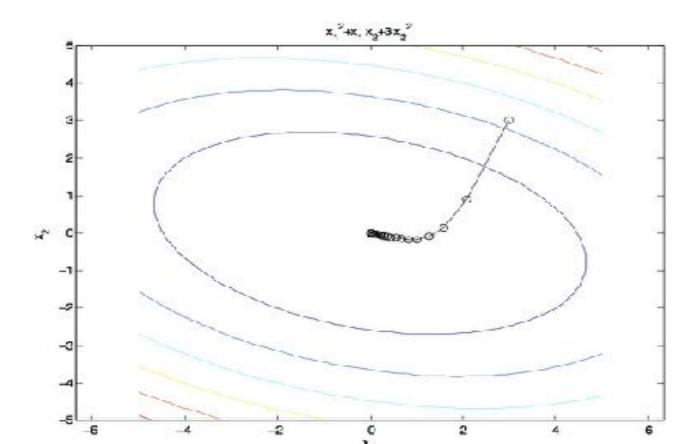


Figure source: Mathworks

#### What is the Steepest Descent Direction?

#### What is the Steepest Descent Direction?

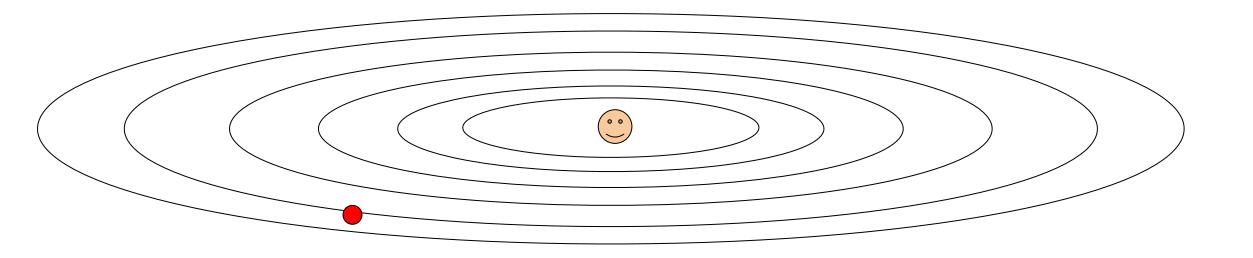
Steepest Direction = direction of the gradient

$$\nabla g = \begin{bmatrix} \frac{\partial g}{\partial w_1} \\ \frac{\partial g}{\partial w_2} \\ \cdots \\ \frac{\partial g}{\partial w_n} \end{bmatrix}$$

# **Optimization Procedure 1: Gradient Descent**

Init: 
$$w$$
  
For i = 1, 2, ...  
 $w \leftarrow w - \alpha * \nabla g(w)$ 

- *α*: learning rate --- tweaking parameter that needs to be chosen carefully
- How? Try multiple choices
  - Crude rule of thumb: update changes w about 0.1 1 %

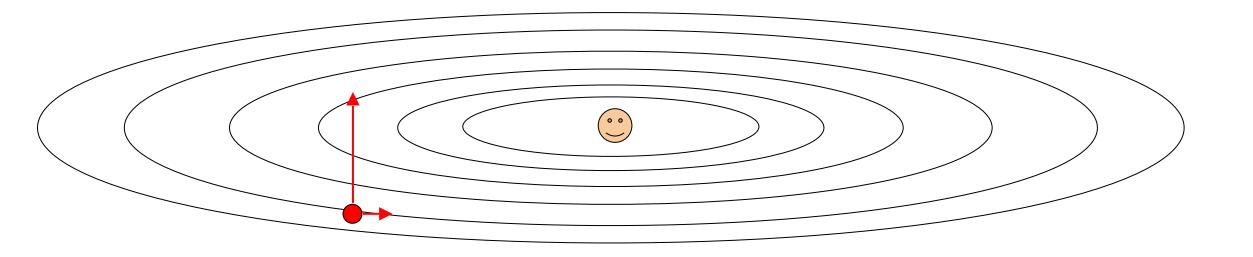


# Q: What is the trajectory along which we converge towards the minimum with Gradient Descent?

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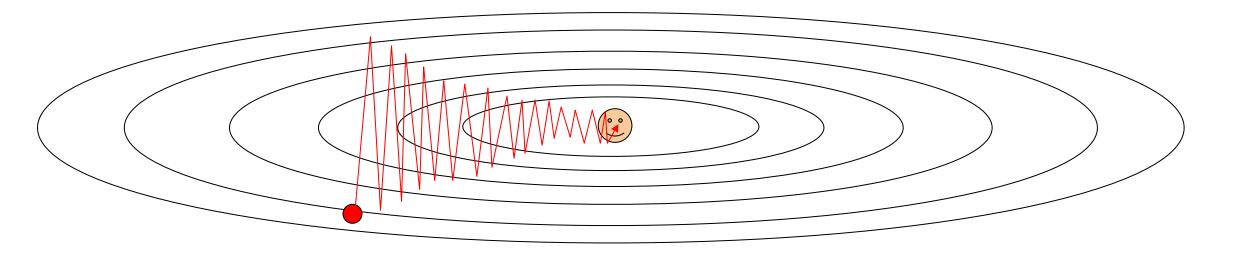


# Q: What is the trajectory along which we converge towards the minimum with Gradient Descent?

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Q: What is the trajectory along which we converge towards the minimum with Gradient Descent? very slow progress along flat direction, jitter along steep one

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# **Optimization Procedure 2: Momentum**

Gradient Descent

Init: w

■ For i = 1, 2, ...

$$w \leftarrow w - \alpha * \nabla g(w)$$

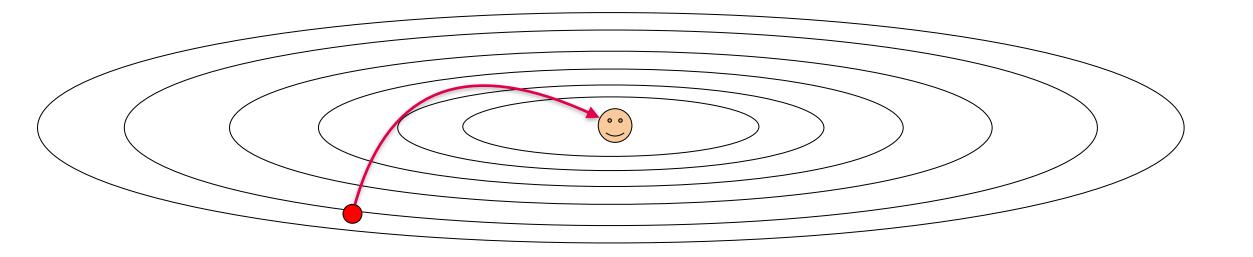
Init: 
$$w$$
For i = 1, 2, ...
$$v \leftarrow \mu * v - \alpha * \nabla g(w)$$

$$w \leftarrow w + v$$

Momentum

- Physical interpretation as ball rolling down the loss function + friction (mu coefficient).

- mu = usually ~0.5, 0.9, or 0.99 (Sometimes annealed over time, e.g. from 0.5 -> 0.99)



# Q: What is the trajectory along which we converge towards the minimum with Momentum?

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How do we actually compute gradient w.r.t. weights?

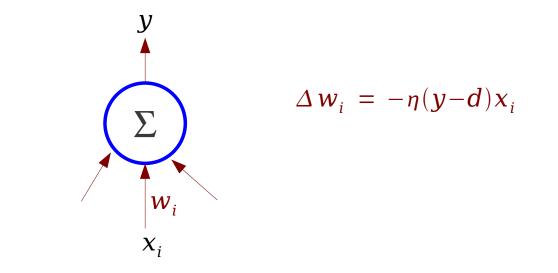
# Backpropagation!

### **Backpropagation Learning**

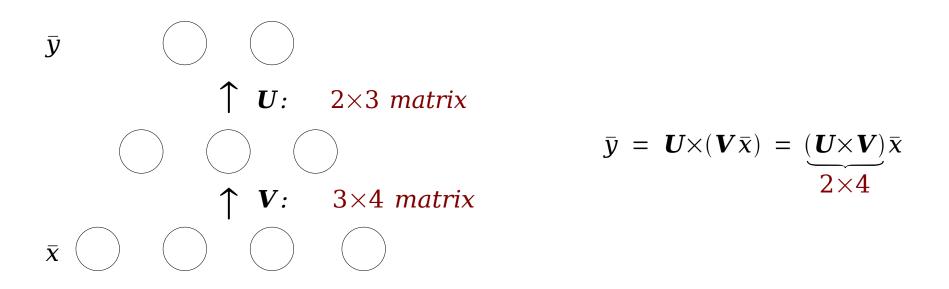
15-486/782: Artificial Neural Networks David S. Touretzky

Fall 2006

#### LMS / Widrow-Hoff Rule



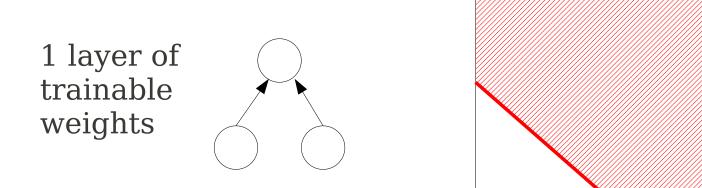
Works fine for a single layer of trainable weights. What about multi-layer networks? With Linear Units, Multiple Layers Don't Add Anything



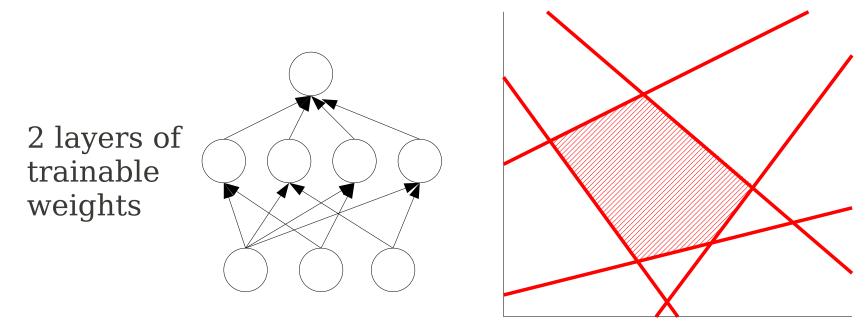
Linear operators are closed under composition. Equivalent to a single layer of weights  $W=U\times V$ 

But with non-linear units, extra layers add computational power.

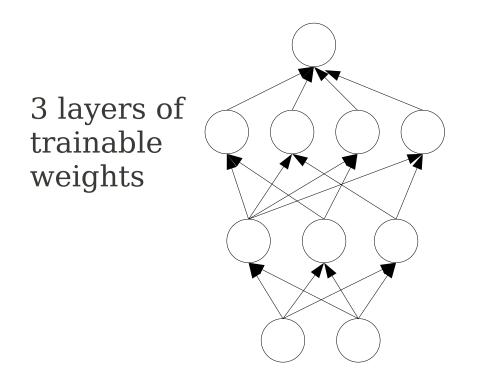
### What Can be Done with Non-Linear (e.g., Threshold) Units?

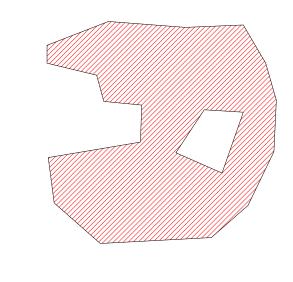


separating hyperplane



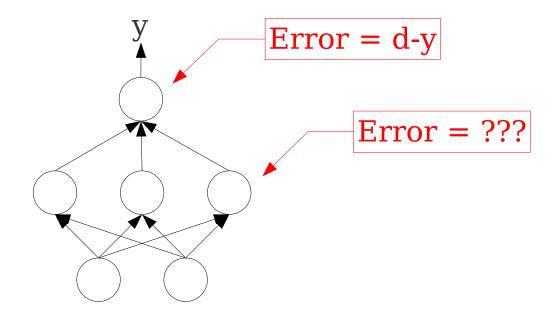
#### convex polygon region





composition of polygons: non convex regions

### How Do We Train A Multi-Layer Network?

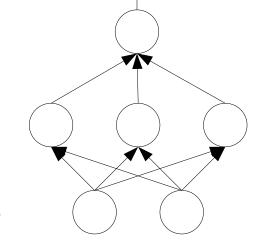


Can't use perceptron training algorithm because we don't know the 'correct' outputs for hidden units.

### How Do We Train A Multi-Layer Network?

*Define sum-squared error:* 

$$E = \frac{1}{2} \sum_{p} (d^p - y^p)^2$$

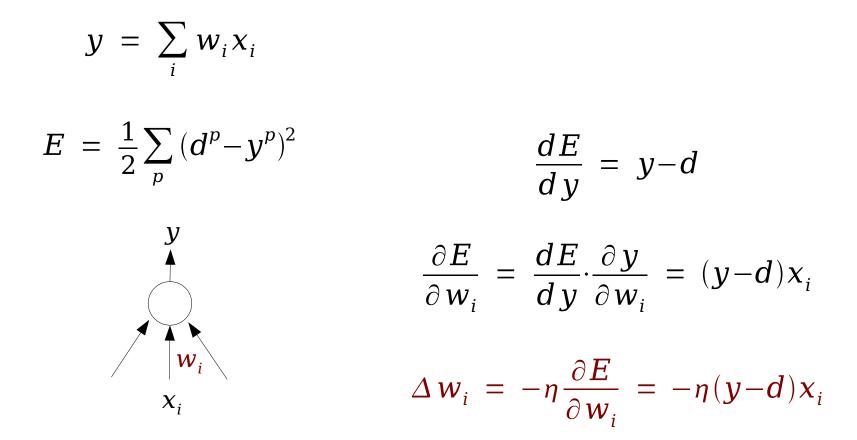


Use gradient descent error minimization:

$$\Delta w_{ij} = -\eta \frac{\partial E}{\partial w_{ij}}$$

Works if the nonlinear transfer function is differentiable.

#### Deriving the LMS or "Delta" Rule As Gradient Descent Learning



How do we extend this to two layers?

#### Switch to Smooth <u>Nonlinear</u> Units

$$\operatorname{net}_{j} = \sum_{i} w_{ij} y_{i}$$

 $y_j = g(net_j)$  g must be differentiable

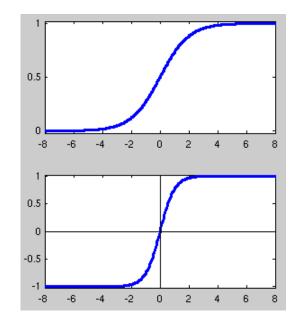
Common choices for g:  

$$g(x) = \frac{1}{1 + e^{-x}}$$

$$g'(x) = g(x) \cdot (1 - g(x))$$

$$g(x) = \tanh(x)$$

$$g'(x) = \frac{1}{\cosh^2(x)}$$



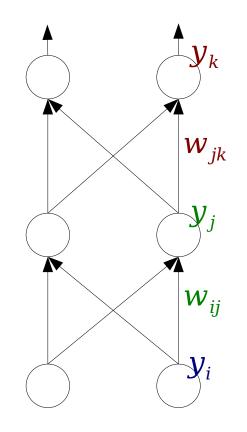
#### Gradient Descent with Nonlinear Units

$$x_{i} \xrightarrow{w_{i}} \tanh(\Sigma w_{i} x_{i}) \longrightarrow y$$
$$y = g(net) = \tanh\left(\sum_{i} w_{i} x_{i}\right)$$

$$\frac{dE}{dy} = (y - d), \qquad \frac{dy}{dnet} = 1/\cosh^2(net), \qquad \frac{\partial net}{\partial w_i} = x_i$$

$$\frac{\partial E}{\partial w_i} = \frac{dE}{dy} \cdot \frac{dy}{dnet} \cdot \frac{\partial net}{\partial w_i}$$
$$= (y-d)/\cosh^2 \left(\sum_i w_i x_i\right) \cdot x_i$$

#### Now We Can Use The Chain Rule



$$\frac{\partial E}{\partial y_{k}} = (y_{k} - d_{k})$$

$$\delta_{k} = \frac{\partial E}{\partial net_{k}} = (y_{k} - d_{k}) \cdot g'(net_{k})$$

$$\frac{\partial E}{\partial w_{jk}} = \frac{\partial E}{\partial net_{k}} \cdot \frac{y_{b}}{\partial net_{k}} = \delta_{k} \cdot y_{j}$$

$$\frac{W_{jk}}{\sqrt{\frac{\partial E}{\partial y_{j}}}} = \sum_{k} \sqrt{\frac{\partial E}{\partial net_{k}}} \cdot \frac{\partial net_{k}}{\partial y_{j}}$$

$$\delta_{j} = \frac{\partial E}{\partial net_{j}} = \frac{\partial E}{\partial y_{j}} \cdot g'(net_{j})$$

$$W_{ij} = \frac{\partial E}{\partial w_{ij}} = y_{i}$$

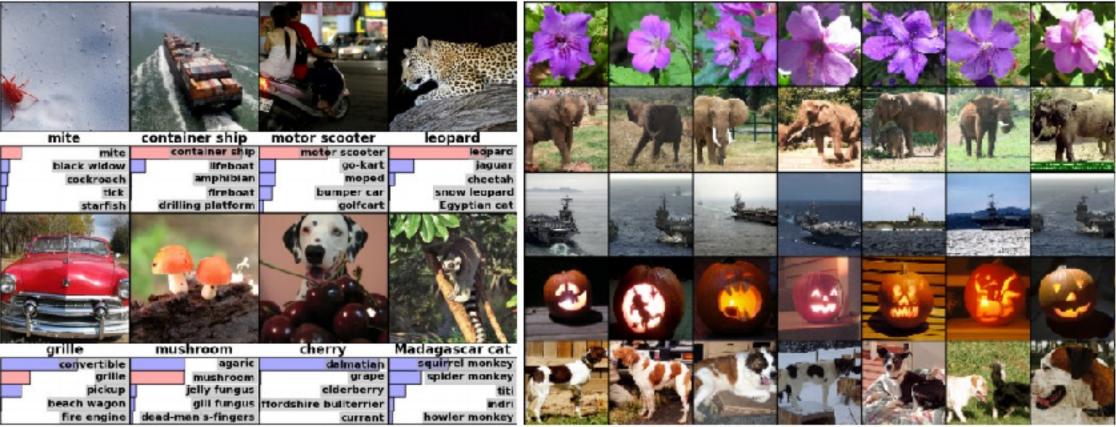
## Weight Updates

$$\frac{\partial E}{\partial w_{jk}} = \frac{\partial E}{\partial net_k} \cdot \frac{\partial net_k}{\partial w_{jk}} = \delta_k \cdot y_j$$
$$\frac{\partial E}{\partial w_{ij}} = \frac{\partial E}{\partial net_j} \cdot \frac{\partial net_j}{\partial w_{ij}} = \delta_j \cdot y_i$$

$$\Delta w_{jk} = -\eta \cdot \frac{\partial E}{\partial w_{jk}} \qquad \Delta w_{ij} = -\eta \cdot \frac{\partial E}{\partial w_{ij}}$$

#### Classification

Retrieval



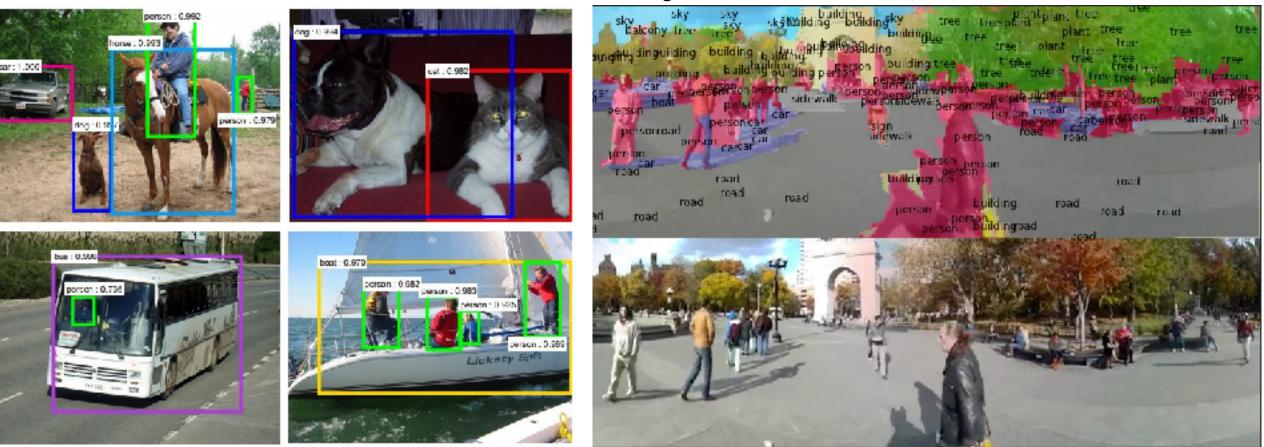
<sup>[</sup>Krizhevsky 2012]

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Segmentation

Detection



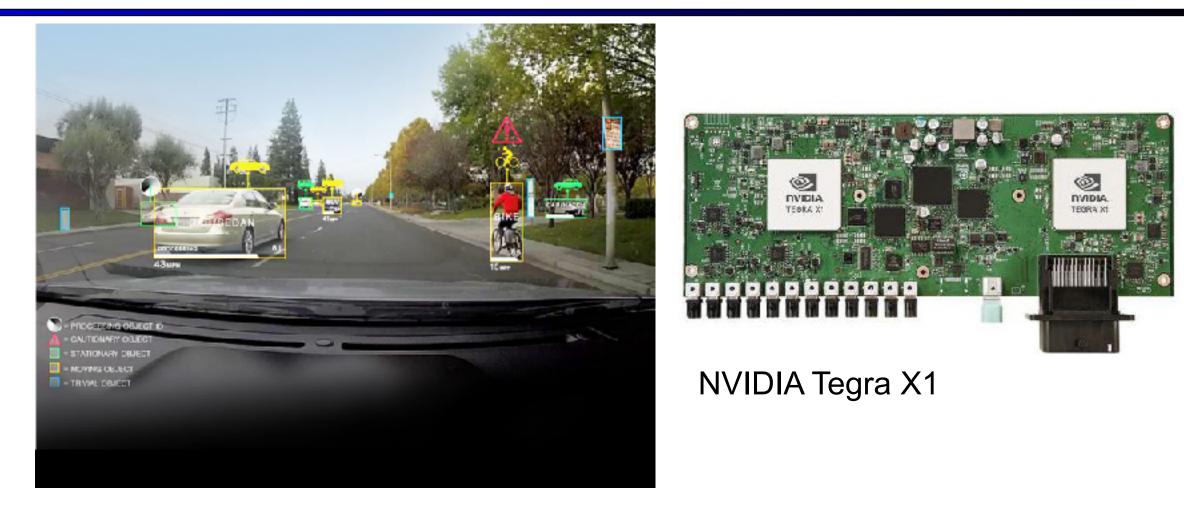
[Faster R-CNN: Ren, He, Girshick, Sun 2015]

[Farabet et al., 2012]

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self-driving cars

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[Toshev, Szegedy 2014]

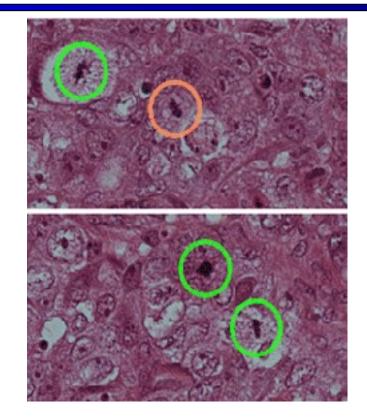


[Mnih 2013]

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着 n M 节纸志 EJ.

[Ciresan et al. 2013]



[Sermanet et al. 2011] [Ciresan et al.]

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#### **Describes without errors**

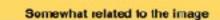


A person riding a motorcycle on a dirt road.



**Describes with minor errors** 

Two dogs play in the grass.





A skateboarder does a trick on a ramp.



Unrelated to the image

A dog is jumping to catch a frisbee.



A refrigerator filled with lots of food and drinks.



A yellow school bus parked in a parking lot.

#### Image Captioning



A group of young people playing a game of frisbee.



Two hockey players are fighting over the puck.



A little girl in a pink hat is blowing bubbles.



A red motorcycle parked on the side of the road.



A herd of elephants walking across a dry grass field.



A close up of a cat laying on a couch.