



# Parsing World's Skylines using Shape-constrained MRFs

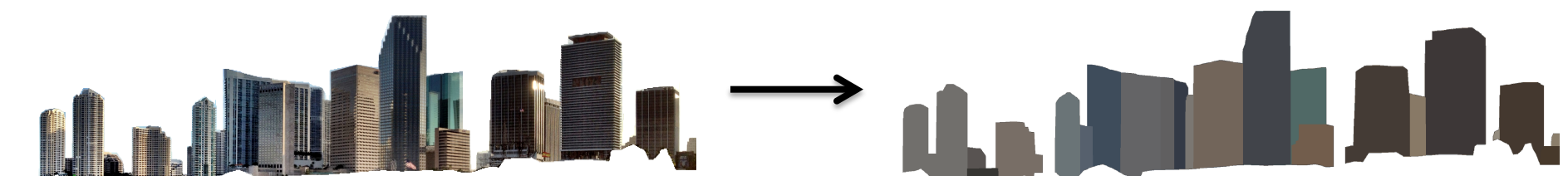
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## Problem and contributions

An approach for **segmenting** buildings in skyline images



We use priors on **topology** and **shape** of the buildings to develop a MRF solver that is **10x faster** and **more accurate** than a graph-cut based approach.

## Energy minimization formulation (MRF)

For a set of pixels  $P$  and set of possible labels  $L$ , energy of labeling  $F: P \rightarrow L$ , is defined as:

$$E(F) = \sum_{p \in P} D_p(F_p) + \sum_{p, q \in N} V_{pq}(F_p, F_q)$$

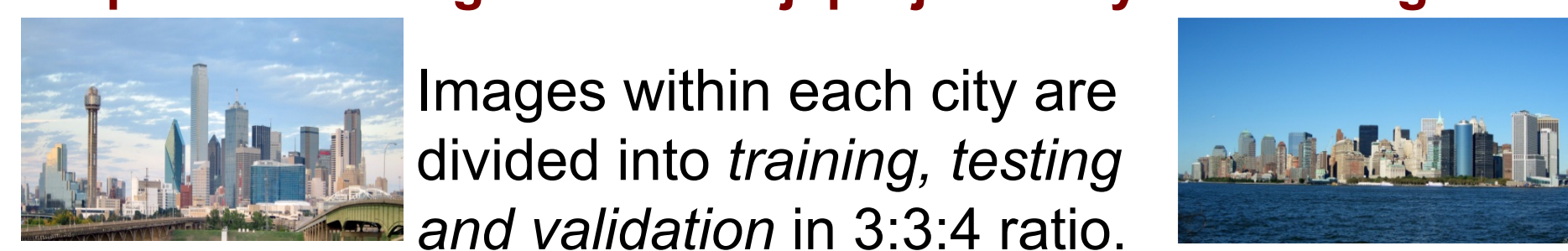
Where  $V_{pq}(a, b) = \lambda \exp(-\gamma(I_p - I_q)^2) \cdot 1(a \neq b)$  and  $I_p$  denotes image intensity at pixel  $p$ . The optimal labeling can be obtained by,  $F^* = \text{argmin}_f E(f)$

## Skyline-12 dataset

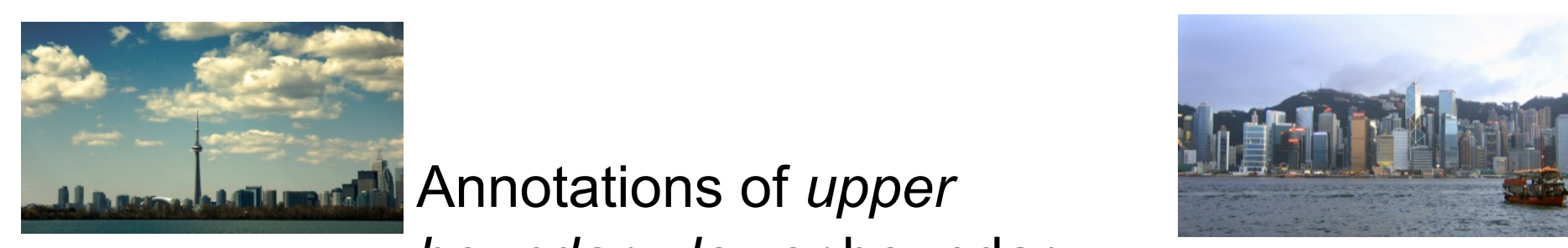
Consisting of **120** high resolution skyline images, with **10** images from each of the **12** cities - Chicago, Dallas, Frankfurt, Hong Kong, Miami, New York, Philadelphia, Seattle, Shanghai, Singapore, Tokyo and Toronto.

Code and dataset available at:

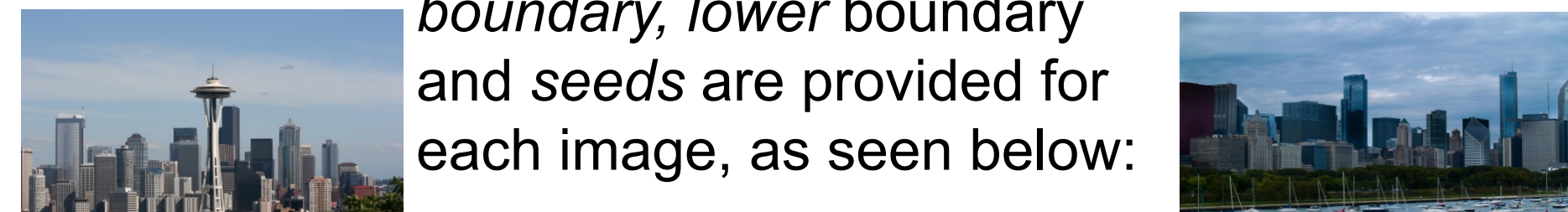
<http://ttic.uchicago.edu/~smaji/projects/skylineParsing>



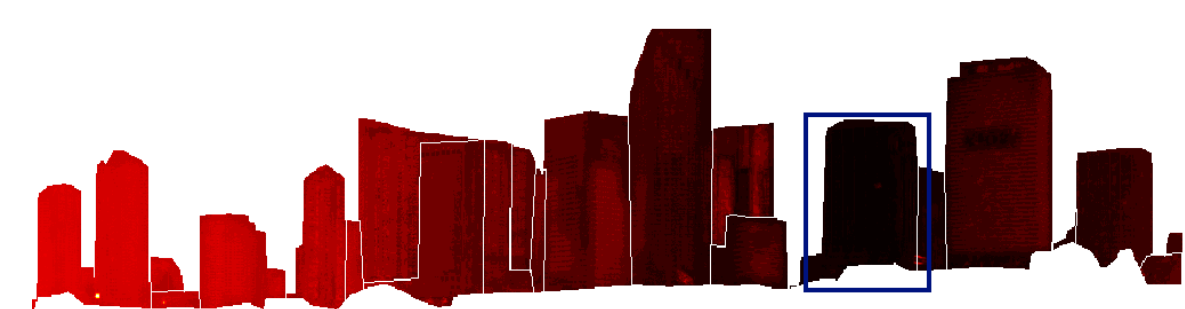
Images within each city are divided into *training*, *testing* and *validation* in 3:3:4 ratio.



Annotations of *upper boundary*, *lower boundary* and *seeds* are provided for each image, as seen below:

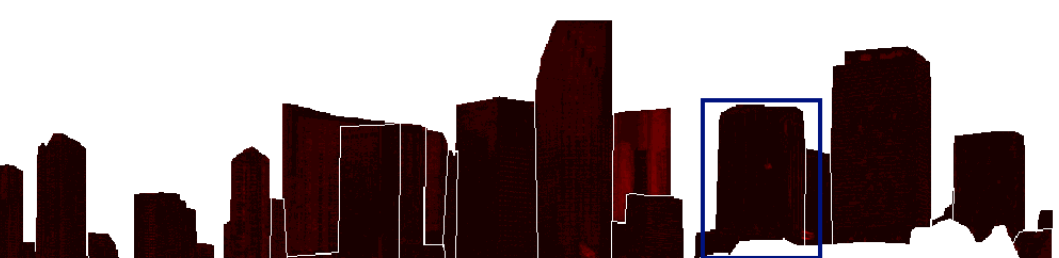


## Region representation

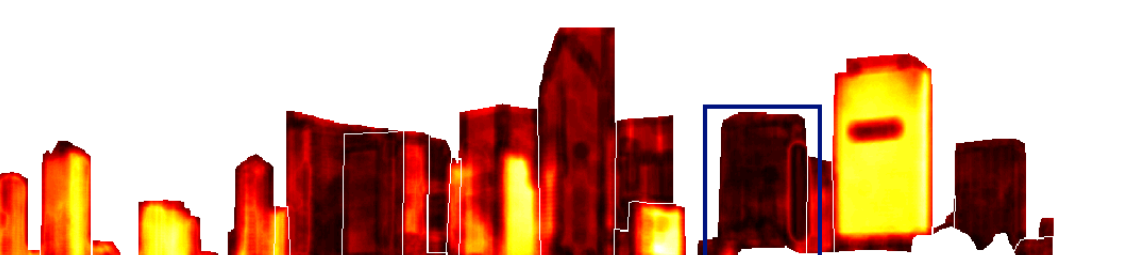


$$D_p(b) = \alpha \left( \beta \min_k C_p(b, k) + (1 - \beta) \min_k T_p(b, k) \right) + (1 - \alpha) S_p(b)$$

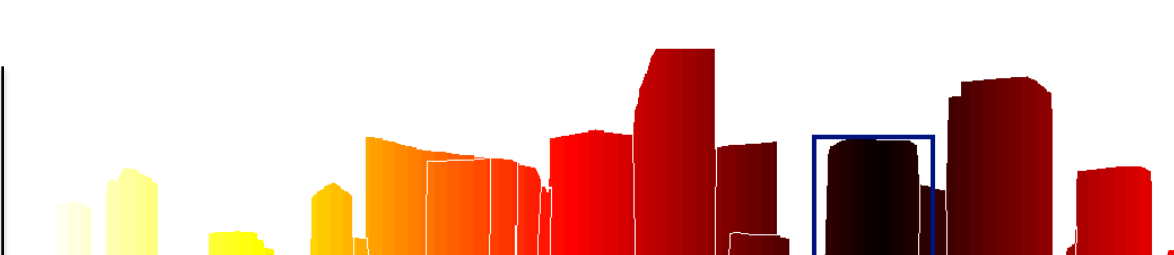
Unary term  $D_p(b)$  for pixel  $p$ , building  $b$ .



Color  $C_p(b, k)$  modeled with Gaussian Mixture Models representing color contribution at pixel  $p$  in the  $k^{th}$  cluster in building  $b$ .



Texture  $T_p(b, k)$  is modeled as  $\chi^2$  distance of the local histogram at pixel  $p$  from the mean histogram at  $k^{th}$  cluster center for building  $b$ .

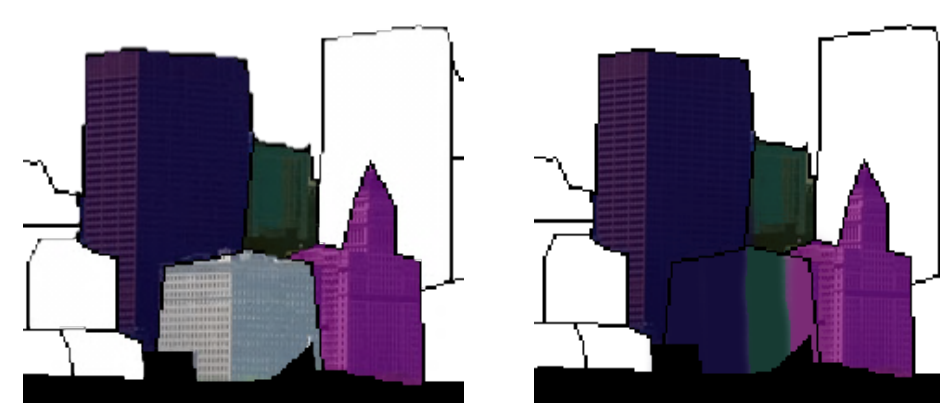


Spatial  $S_p(b)$  modeled as horizontal distance of pixels  $p$  from center of the building  $b$ .

## Approach

### Topological structure

Given label  $\alpha$ , background beneath it can be obtained by copying labels *top to bottom*, allowing us to simultaneously expand and contract regions with label  $\alpha$ , i.e. only the upper boundary needs to be estimated per building.



Foreground  $\alpha$  and background

### Input to the algorithm



image, upper/lower boundary, seeds

**Method** (1) Order the buildings based on the lowest seed pixel. (2) Iteratively refine upper boundary.

### Algorithm 1 Greedy skyline segmentation

**Require:** data  $D$ , pairwise  $V$ , boundary  $(l, u)$   
1: Initialize, initial labeling  $F$  from unary labels  
2: **for** iter := 1 to  $K$  **do**  
3: Initialize, frontier  $f \leftarrow l$   
4: **for**  $\alpha := 1$  to  $N$  **do**  
5:  $\Omega_\alpha \leftarrow \text{upperBoundary}(\alpha, F, D, V, f, u)$   
6:  $f \leftarrow \max(f, \Omega_\alpha)$   
7:  $F \leftarrow \text{updateLabels}(F, \Omega_\alpha)$   
8: **end for**  
9: **end for**

We propose three fast methods to obtain the upper boundary – **rectangle MRF**, **tiered MRF** and **refined MRF**. Each one solves a *binary segmentation problem*, as in  $\alpha$ -expansion. Standard solver using graph-cuts requires  $O(m^3n^3)$  time for a  $m \times n$  image.

## Rectangle MRF $O(mn^2)$

Upper boundary is a rectangle parameterized by (*left, right, top*). Brute-force search for optimal rectangle can be done in  $O(1)$  time per value using integral images, hence optimal can be found in  $O(mn^2)$  time. Additionally can enforce width, height and aspect constraints.



## Tiered MRF $O(m^2n)$

Upper boundary is 'x-monotonic', i.e. intersects each column only once. Optimal path can be computed using dynamic programming in  $O(m^2n)$  time [1,2]. Fast, but cannot enforce shape priors efficiently.



## Refined MRF $O(mn^2 + m^2d)$

Only *refine* the upper boundary *within* the width of the building. Constrains the overall segmentation and *improves* accuracy. Given a building of width  $d$  the refinement can be computed in  $O(m^2d)$  time, for a total of  $O(mn^2 + m^2d)$  per building.



## References

1. P. F. Felzenszwalb and O. Veksler. *Tiered scene labeling with dynamic programming*, CVPR, 2010
2. Y. Zheng, S. Gu, and C. Tomasi. *Fast tiered labeling with topological priors*, ECCV, 2012
3. R. Achanta, A. Shaji, K. Smith, A. Lucchi, P. Fua, and S. Su'sstrunk. *SLIC Superpixels compared to state-of-the-art superpixel methods*, IEEE PAMI, 2012
4. P. F. Felzenszwalb and D. P. Huttenlocher. *Efficient graph-based image segmentation*, IJCV, 2004
5. P. Arbelaez, M. Maire, C. Fowlkes, and J. Malik. *Contour detection and hierarchical image segmentation*. IEEE PAMI, 2011

## Experimental evaluation

### Evaluation metric

Let  $G_I$  and  $P_I$  denote ground truth and predicted labeling. Let  $G_I^i$  and  $P_I^i$  denote the set of pixels labeled as building  $i$ . The average overlap for the image with  $N$  buildings is defined as:

$$AO(G_I, P_I) = \frac{1}{N} \sum_{i=1}^N \frac{G_I^i \cap P_I^i}{G_I^i \cup P_I^i}$$

We report mean average overlap (MAO) scores over the *test* set.

### Interactive setting

Seeds are provided as input along with upper/lower boundary

### Automatic setting

Only the upper/lower boundaries are provided, i.e., no seeds. We start with several automatic segmentation algorithms and *improve* over them using the shape and topological priors we proposed.

For evaluation we first perform a matching between the ground truth and segmented labels  $m: N \rightarrow M$ . Accuracy is measured under this matching:

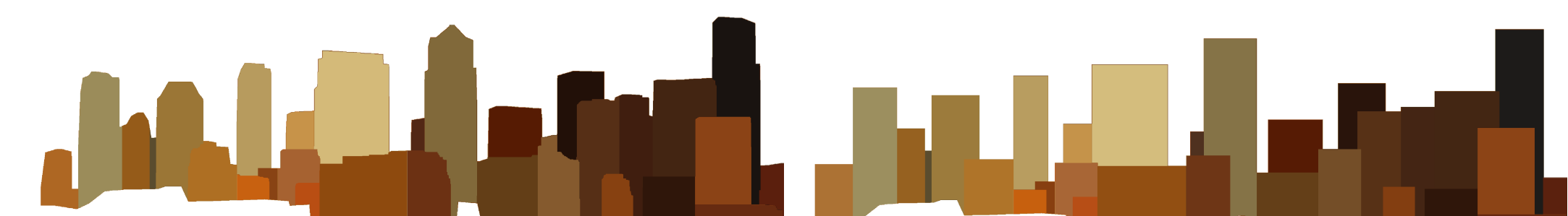
$$AO(G_I, P_I) = \max_{m \in M} \frac{1}{N} \sum_{i=1}^N \frac{G_I^i \cap P_I^{m(i)}}{G_I^i \cup P_I^{m(i)}}$$

| Method        | Interactive Setting |           | Automatic Setting |                |         |
|---------------|---------------------|-----------|-------------------|----------------|---------|
|               | MAO                 | Speed/img | SLIC[3]           | Graph based[4] | gPb[5]  |
| Standard MRF  | 62.3 %              | 69.5 s    | 24.56 %           | 20.17 %        | 26.35 % |
| Tiered MRF    | 59.4 %              | 7.5 s     | 27.22 %           | 25.86 %        | 31.51 % |
| Rectangle MRF | 62.0 %              | 5.5 s     | 27.33 %           | 27.87 %        | 32.79 % |
| Refined MRF   | 63.4 %              | 9.2 s     | 27.30 %           | 27.42 %        | 33.13 % |



Original Skyline

Ground Truth



Refined MRF

Rectangle MRF



Tiered MRF

Automatic Refined MRF