1. [25 pts.] Do problem 8.9, page 266: prove that the Hitting-Set problem is NP complete. [Hint: To do this you must argue that Hitting-Set is in NP, and give a polynomial-time reduction from some NP complete problem to Hitting-Set. I suggest that you reduce 3-SAT to Hitting-Set. Suppose that your input is a 3-CNF formula, \( \varphi \), with \( m \) boolean variables, \( x_1, \ldots, x_m \), and \( r \) clauses, \( C_1, \ldots, C_r \). You want to compute an instance of the Hitting-Set problem, \( f(\varphi) \) such that,

\[
\varphi \in 3\text{-SAT} \iff f(\varphi) \in \text{Hitting-Set}.
\]

I suggest that you make the problem \( f(\varphi) \) have \( n = m + r \) sets to be hit.]

2. [25 pts.] Do problem 8.10, page 266: a, c, and f: show that these three problems are in NP and show that they are NP complete by explaining how they are generalizations of known NP complete problems.

3. [25 pts.] Do problem 5.33, page 154: show how to implement the given greedy algorithm (called “Stingy” in the text, §5.3) in linear time.

4. [25 pts.] Do problem 9.1, page 293: show that the backtracking algorithm for 2-SAT, with the following heuristic runs in polynomial time. The heuristic is: always choose a subproblem (CNF formula) that has a clause that is as small as possible and expand it along a variable that appears in this small clause.