Neural Language Models

CS 685, Spring 2025 Advanced Natural Language Processing

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many slides from Richard Socher and Matt Peters

Deadlines

- 2/17: Quiz 1 due
- 2/14: HW 0 due
- 2/14: Final project group assignments due
- 3/7: Project proposals due
- 5/9: Final project reports due
- 5/9: Last day to submit extra credit
 - This Wednesday, we will have another talk (https://nlp.cs.umass.edu/seminar/)

Project Rubric

- Rubric
 - Acceptable for main NLP conferences: 100
 - Acceptable for NLP workshops: 97
 - Having one of the noticeable great attributes among Effort, Novelty, Usefulness, and Implication: 95
 - Is a complete NLP scientific report: 90
 - Have some findings but also contain some major weaknesses: 85
 - Can see that students spend some effort on the project: 80
- Policy of one project for multiple courses
 - The instructor of the other course needs to agree
 - All your group members need to agree
 - You need to indicate that in the final report for all courses
 - Your effort needs to be proportional to the number of credits



Data is the King for Maximizing Task Performances



Bitter Lesson (<u>http://www.incompleteideas.net/Incldeas/BitterLesson.html</u>) One of the most important concepts in this course, but More Data -> AGI? I personally disagree.

Multiple Token Prediction



Figure 3 | Illustration of our Multi-Token Prediction (MTP) implementation. We keep the complete causal chain for the prediction of each token at each depth.

DeepSeek V3 (<u>https://arxiv.org/pdf/2412.19437v1</u>)

Please Ask Questions if You don't Understand

language model review

• Goal: compute the probability of a sentence or sequence of words:

 $P(W) = P(w_1, w_2, w_3, w_4, w_5...w_n)$

- Related task: probability of an upcoming word: P(w₅|w₁,w₂,w₃,w₄)
- A model that computes either of these:

P(W) or P($w_n | w_1, w_2...w_{n-1}$) is called a language model or LM



Testing data: its water does

n-gram models

 $p(w_j | \text{students opened their}) = \frac{\text{count}(\text{students opened their } w_j)}{\text{count}(\text{students opened their})}$

Problems with n-gram Language Models

Sparsity Problem 1

Problem: What if *"students* opened their w_j " never occurred in data? Then w_j has probability 0!

 $p(w_j | \text{students opened their}) = \frac{\text{count}(\text{students opened their } w_j)}{\text{count}(\text{students opened their})}$

Problems with n-gram Language Models

Sparsity Problem 1

Problem: What if "students opened their w_j " never occurred in data? Then w_j has probability 0!

(Partial) Solution: Add small δ to count for every $w_j \in V$. This is called *smoothing*.

 $p(w_j | \text{students opened their}) = \frac{\text{count}(\text{students opened their } w_j)}{\text{count}(\text{students opened their})}$

Problems with n-gram Language Models



Increasing *n* makes model size huge!

another issue:

 We treat all words / prefixes independently of each other!

students opened their ____

pupils opened their ____

scholars opened their ____

Shouldn't we share information across these semantically-similar prefixes?

undergraduates opened their ____

students turned the pages of their ____

students attentively perused their ____

. . .

one-hot vectors

- n-gram models rely on the "bag-of-words" assumption
- represent each word/n-gram as a vector of zeros with a single 1 identifying its index in the vocabulary



movie = <0, 0, 0, 0, 1, 0>film = <0, 0, 0, 0, 0, 1>

what are the issues of representing a word this way?

all words are equally (dis)similar!

movie = <0, 0, 0, 0, 1, 0>
film = <0, 0, 0, 0, 0, 0, 1>
dot product is zero!
these vectors are orthogonal

What we want is a representation space in which words, phrases, sentences etc. that are semantically similar also have similar representations!

Task -> Loss -> Model -> Optimization

- Task:
 - Predict the next token
 - Prior to 2018, only a few NLP researchers studied LMs
 - Looking for ELMo's friends: Sentence-Level Pretraining Beyond Language Modeling (<u>https://openreview.net/</u> <u>forum?id=Bkl87h09FX</u>)
- Loss:
 - Maximal Likelihood / Cross-entropy
- Model:
 - Tables -> Neural Network -> Transformer
- Optimization:
 - Counting -> Gradient Descent

Enter neural networks!

Students opened their



Enter neural networks!

Students opened their

This lecture: the forward pass, or how we compute a prediction of the next word given an existing neural language model



books

Enter neural networks!

Students opened their

This lecture: the forward pass, or how we compute a prediction of the next word given an existing neural language model neural language model

Next lecture: the backward pass, or how we train a neural language model on a training dataset using the backpropagation algorithm

books

words as basic building blocks

 represent words with low-dimensional vectors called embeddings (Mikolov et al., NIPS 2013)

> king = [0.23, 1.3, -0.3, 0.43]



Male-Female

Verb tense

Country-Capital

model['nuclear']

array([0.58108	,	0.66825	,	1.0771 ,	,	0.34879	,	-0.34613	,	0.20463	,
	0.78436	,	0.11287	,	0.77594 ,	,	0.43579	,	0.18566	,	-0.20375	,
-	0.53369	,	0.55578	,	-0.099609,	,	1.1739	,	0.83277	,	1.2848	,
-	0.19772	,	0.41573	,	1.1255 ,	,	-0.31634	,	0.22493	,	-1.0348	,
	0.28462	,	-2.7709	,	0.80654 ,	,	0.24704	,	0.64272	,	0.41439	,
	2.4058	,	-1.1552	,	-1.3758 ,	,	-0.90799	,	0.20109	,	-0.29947	,
	0.10769	,	0.29975	,	-0.94256 ,	,	0.26281	,	-0.17048	,	-1.1831	,
	0.99454	,	-0.50074	,	1.0424 ,	,	0.8123	,	-0.20606	,	1.9433	,
-	-1.2817	,	-0.49774	1))							

- Each dimension is not an attribute
 - If you force non-negative embeddings during training, it will have meaning
 - Linear combination of dimensions could reveal attributes

composing embeddings

 neural networks compose word embeddings into vectors for phrases, sentences, and documents



Predict the next word from composed prefix representation



How does this happen? Let's work our way backwards, starting with the prediction of the next word



How does this happen? Let's work our way backwards, starting with the prediction of the next word



Softmax layer: convert a vector representation into a probability distribution over the entire vocabulary



$P(w_i | \text{vector for "students opened their"})$



Let's say our output vocabulary consists of just four words: "books", "houses", "lamps", and "stamps".



Low-dimensional representation of "students opened their" Let's say our output vocabulary consists of just four words: "books", "houses", "lamps", and "stamps".



We want to get a probability distribution over these four words



Low-dimensional representation of "students opened their"



Here's an example 3-d prefix vector

W is a *weight matrix*. It contains *parameters* that we can *update* to control the final probability distribution of the next word

$$\mathbf{W} = \left\{ \begin{array}{l} 1.2, -0.3, 0.9 \\ 0.2, 0.4, -2.2 \\ 8.9, -1.9, 6.5 \\ 4.5, 2.2, -0.1 \end{array} \right\}$$

x = <-2.3, 0.9, 5.4>

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product

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intuition: each row of **W** contains *feature weights* for a corresponding word in the vocabulary

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 $W = \begin{cases} 1.2, -0.3, 0.9 \\ 0.2, 0.4, -2.2 \\ 8.9, -1.9, 6.5 \\ 4.5, 2.2, -0.1 \end{cases} \stackrel{books}{\underset{anps}{}_{anps}}$

x = <-2.3, 0.9, 5.4>

intuition: each row of **W** contains *feature weights* for a corresponding word in the vocabulary

CAUTION: we can't easily *interpret* these features! For example, the second dimension of **x** likely does not correspond to any linguistic property

 $\mathbf{W} = \left\{ \begin{array}{ll} 1.2, \ -0.3, \ 0.9 \\ 0.2, \ 0.4, \ -2.2 \\ 8.9, \ -1.9, \ 6.5 \\ 4.5, \ 2.2, \ -0.1 \end{array} \right\} \begin{array}{l} books \\ houses \\ houses \\ tamps \\ stamps \\ stamps \end{array} \right.$

x = <-2.3, 0.9, 5.4>

Wx = <1.8, -11.9, 12.9, -8.9>

How did we compute this? It's just the dot product of each row of **W** with **x**!



x = <-2.3, 0.9, 5.4>

Wx = <1.8, -11.9, 12.9, -8.9>

How did we compute this? It's just the dot product of each row of **W** with **x**!





Some LMs uses Wx + b, but it doesn't matter. Why?

Okay, so how do we go from this 4-d vector to a probability distribution?

We'll use the **softmax** function!



• Wx is a vector

more numerically stable

- [Wx]_j is dimension j of Wx
- each dimension *j* of the softmaxed output represents the probability of class *j*

Wx = <1.8, -1.9, 2.9, -0.9>→Logit softmax(Wx) = <0.24, 0.006, 0.73, 0.02>

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softmax(Wx) =
$$\frac{e^{Wx}}{\sum_{j} e^{[Wx]_{j}}}$$

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We'll see the softmax function over and over again this semester, so be sure to understand it!

so to sum up...

- Given a *d*-dimensional vector representation *x* of a prefix, we do the following to predict the next word:
 - 1. Project it to a *V*-dimensional vector using a matrix-vector product (a.k.a. a "linear layer", or a "feedforward layer"), where *V* is the size of the vocabulary
 - 2. Apply the softmax function to transform the resulting vector into a probability distribution



(https://proceedings.neurips.cc/paper_files/paper/2014/file/feab05aa91085b7a8012516bc3533958-Paper.pdf)

Now that we know how to predict **"books"**, let's focus on how to compute the prefix representation **x** in the first place!



Composition functions

input: sequence of word embeddings corresponding to the tokens of a given prefix

output: single vector

- Element-wise functions
 - e.g., just sum up all of the word embeddings!
- Concatenation
- Feed-forward neural networks
- Convolutional neural networks
- Recurrent neural networks
- Transformers (our focus this semester)

Let's look first at *concatenation* + *feedforward NN*, an easy to understand but limited composition function



concatenated word embeddings

 $x = [c_1; c_2; c_3; c_4]$

words / one-hot vectors

 c_1, c_2, c_3, c_4



hidden layer $h = f(W_1x)$ concatenated word embeddings $x = [c_1; c_2; c_3; c_4]$ words / one-hot vectors c_1, c_2, c_3, c_4



f is a nonlinearity, or an element-wise nonlinear function.
 The most commonly-used choice today is the rectified linear unit (ReLu), which is just ReLu(x) = max(0, x).
 Other choices include tanh and sigmoid.



Activation Function Matter



https://arxiv.org/pdf/2002.05202v1

output distribution

 $\hat{y} = \operatorname{softmax}(W_2h)$

hidden layer

$$h = f(W_1 x)$$

concatenated word embeddings

 $x = [c_1; c_2; c_3; c_4]$

words / one-hot vectors

 c_1, c_2, c_3, c_4



This is also called Feedforward NN , MLP (multilayer perceptron), or fully connected network

how does this compare to a normal n-gram model?

Improvements over *n*-gram LM:

- No sparsity problem
- Model size is O(n) not O(exp(n))

Remaining **problems**:

- Fixed window is too small
- Enlarging window enlarges W
- Window can never be large enough!
- Each C_i uses different rows of W. We don't share weights across the window.



Recurrent Neural Networks!

word embeddings

/ \

 c_1, c_2, c_3, c_4

. _ _ .

 $the \in tridept \in \mathbb{R}^{d}$

hidden states

$$h^{(t)} = f(W_h h^{(t-1)} + W_e c_t)$$

h⁽⁰⁾ is initial hidden state!

word embeddings

/ \

 c_1, c_2, c_3, c_4

· _ _ ·



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· _ _ ·



 $oldsymbol{h}^{(0)}$

output distribution

 $\hat{y} = \operatorname{softmax}(W_2 h^{(t)})$

hidden states

$$h^{(t)} = f(W_h h^{(t-1)} + W_e c_t)$$

h⁽⁰⁾ is initial hidden state!

word embeddings

 C_1, C_2, C_3, C_4



 $\hat{\boldsymbol{y}}^{(4)} = P(\boldsymbol{x}^{(5)}|\text{the students opened their})$

 $\hat{\boldsymbol{y}}^{(4)} = P(\boldsymbol{x}^{(5)}|\text{the students opened their})$

why is this good?

RNN Advantages:

 Can process any length input

|V|

- Model size doesn't increase for longer input
- Computation for step t can (in theory) use information from many steps back
- Weights are shared across timesteps → representations are shared

RNN **Disadvantages**:

- Recurrent computation is slow
- In practice, difficult to access information from
- ___many steps back





Parameters (log scale)

Be on the lookout for...

- Next lecture on **backpropagation**, which allows us to actually train these networks to make reasonable predictions
- After that, we'll focus on attention mechanisms and build our way to the Transformer architecture, which is the most popular composition function used today