

Key things to identify...

- When you read a paper
- When you listen to a lecture
- When you present a paper
- When you think of research ideas:

What is the scientific question? What's the key new idea that allows answering it? How do you measure the success of the answer?

Automated Test Generation Idea:

- Automatically generate tests for software
- Why?
 - Find bugs more quickly
- Conserve resources
- No need to write tests
- If software changes, no need to maintain tests
- No need for testers?

The Problem

- Automated testing is hard to do
- Probably impossible for whole systems
- Certainly impossible without specifications

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Pre- & Post-Conditions

- A pre-condition is a predicate

 assumed to hold before a function executes
- A post-condition is a predicate

 known to hold after a function executes
 - whenever the pre-condition also holds

Example

Pre-condition: l.contains(x)

```
List remove(LinkedList 1, Element x) {
    if (x == l.head())
        return l.tail();
    else
        return
        new LinkedList(l.head(),remove(l.tail(), x));
}
```

Post-condition: !(I.contains(x))

Does this post-condition hold? How can the pre-condition change for the post condition to hold?

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Are pre- and post-conditions a good idea?

- Most useful if they are executable

 written in the programming language itself
 a special case of assertions
- Recommended by software engineers

 and everyone who studies software engineering
- Can reduce ambiguity in specification
- May be somewhat imprecise and incomplete

 full pre- and post-conditions may be more complex than the code!
 still useful even if they do not cover every situation

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Using Pre- and Post-Conditions

- Pre-/Post-Conditions are specifications
- To perform a test:
- Generate an input (any input)
- Check that the test input satisfies the precondition
- Run test
- Check that the test result satisfies the postcondition

Helps run tests, might even help write them!

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How can we generate tests?

- Randomized testing
- Mutation Testing
- Korat

Random Testing

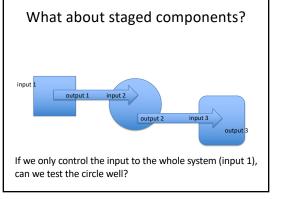
- Feed random inputs to a program

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Random Testing: Good and Bad News

- Randomization is highly effective
 - easy to implement
 - provably good coverage for enough tests
- But
 - to say anything rigorous, we must be able to characterize the distribution of inputs
 - easy for string utilities
 - harder for systems with more arcane input for example, parsers for context-free grammars

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Mutation Analysis

- · How do we know our test suite is any good?
- Idea: Test variations on the program

 for example, replace x > 0 with x < 0
 or replace i by i+1 or i-1
- If the test suite is good, it should report failed tests in the variants

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Mutation Analysis Summary

- Mutate each statement in the program in finitely many different ways
- Each modification is one mutant
- Check if a set of mutants is adequate
- Find a set of test cases that distinguishes the program from the mutants

What Justifies Mutation Testing?

- Competent programmer assumption - the program is close to correct
- Mutations are representative of common errors – off by one errors, wrong comparison errors
- It formalizes test writing

 we write tests for corner cases and off-by-one errors. There are an infinite number of them. This way, we formalize the process.
- This is a start

 testing does not stop here

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Back to automated testing

- Generate mutants of program P
- Generate tests (somehow)
- For each test t for each mutant M if M(t) ≠ P(t) mark M as killed
- · If the tests kill all mutants, the tests are adequate

What if a mutant is equivalent to the original?

- No test will kill it
- In practice, this is a real problem

 hard to solve
- We could try to prove program equivalence

 but automating this is very hard
 undecidable problem

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Generating tests

This is the hard part!

- Use weakest-preconditions

 work backwards from statement to inputs
- Take short paths through loops - try it 0 times, 1 time, 2 times
- Generate symbolic constraints on inputs that must be satisfied
- Solve for inputs

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Korat: A way to generate tests Use pre- and post-conditions to generate tests automatically

Problem Korat tackles:

- There are infinitely many tests
 which finite subset should we pick?
- And even finite subsets can be too big
 - we need a subset which yields good coverage
 - without a lot of redundancy
 - many tests will just test the same thing
 - we need a way to select a diverse test suit

Small test case hypothesis:

If there exists a test case that causes the program to fail, there exists a small test case that causes the program to fail.

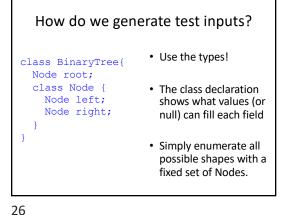
If a list function works on lists of length 0, 1, 2, and 3, it probably works on all lists.

Korat's insight

- Use the small test hypothesis
- We can often do a good job by testing all inputs up to a certain, small size

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A simple algorithm: put it all together

- User selects maximum input size k
- Generate all possible inputs up to size k
- Discard inputs where pre-condition is false
- Run the program on remaining inputs

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• Check the results using the post-condition

Example: Binary Trees

- How many binary trees are there of size <= 3?
- 3 nodes
 - 2 slots per node (left and right)
 - 4 possible values (one of the nodes or null) for
 - each slot
 - the root
- 4 * (4 * 4)^3 = 2^14 = 16,384 possible trees

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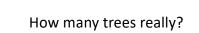
That's a lot of trees!

- The number of trees explodes rapidly
 > 1,000,000 trees of size <= 4
 > 16,000,000 trees of size <= 5
- Limits us to testing only very small input sizes
- Can we do better?

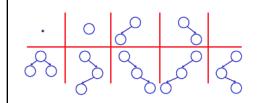
Actually, I lied

- 16,384 trees is a gross overestimate!
- Many of the shapes are not trees:
- Many trees are isomorphic





• There are only 9 distinct binary trees on 3 or fewer nodes



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Use our constraints to help us

- We want to avoid generating trees that don't satisfy the pre-condition in the first place.
- That means we must use the pre-condition to guide the generation of tests
- And use the constraints on distinctness of inputs

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Observe the pre-condition

- Instrument the pre-condition
 - add code to observe it at runtime
 - in particular, record fields of the input the precondition accesses
- Observation:
 - if the pre-condition does not access a field, then the result of the pre-condition did not depend on that field.

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Binary tree example

- Pre-condition checks
 - if the root is null
 - return false
 - all nodes must be unique
 - no cycles
 - every node has one parent (except the root, which has 0)

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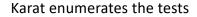
Example:

Consider the following "tree"



- The pre-condition accesses only the root

 since the root is null, every possible shape for the
 other nodes would yield the same result
- This single input eliminates 25% of the tests

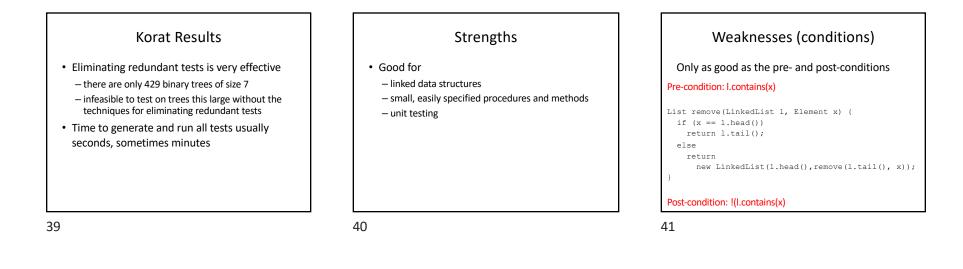


- Start with the smallest
- Next test generated by
 - expanding a null pointer field
 - backtracking if all possibilities for a field are exhausted
- Never enumerate parts of input not examined by the precondition

Error specifications

We can have two specifications:

- Normal behavior specification
- Error behavior specification under what circumstances exceptions are thrown



Weaknesses (conditions)

Only as good as the pre- and post-conditions

Pre-condition: !(I.isEmpty())

List remove(LinkedList 1, Element x) {
 if (x == l.head())
 return l.tail();
 else
 return
 new LinkedList(l.head(),remove(l.tail(), x));
}

Post-condition: l.isList()

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Weaknesses (large data structures)

- Strong when we can enumerate all possibilities
- four nodes, two edges per node
- Weaker when enumeration is weak
- integers
- floating point numbers
- strings

Weakness (nondeterminism)

Not as good for nondeterministic methods

For example, what about a condition that says "Every packet sent is eventually acknowledged by the receiver"?

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Test generation

- Automatic test generation is a good idea
- Typed languages are a plus for generation
 - C++, Java, UML (C, Lisp do not provide needed types)
- Works well for unit tests
- Being adopted in industry
- Promising future