

Word Embeddings

CS 490A, Fall 2021

Applications of Natural Language Processing

https://people.cs.umass.edu/~brenocon/cs490a_f21

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Administrivia

- HW3 due this Friday, 10/29
- Project Proposal Feedback coming soon!
- Keep a lookout for Project Proposal Meeting sign-ups!
- Midterm Review: 11/4
- In-Class Midterm: 11/9

What is a *pawpaw*?


I. Look it up in a dictionary

<https://www.merriam-webster.com/>

<https://www.oed.com/>

<https://en.wiktionary.org/>



pawpaw noun

 Save Word

paw·paw

variants: *or less commonly* papaw

Definition of *pawpaw*

- 1 \ pə-'pò  \ : PAPAAYA
- 2 \ 'pä-(.)pò , 'pò-\ : a North American tree (*Asimina triloba*) of the custard-apple family with purple flowers and an edible green-skinned fruit
also : its fruit



Lemma

pawpaw noun

Save Word

paw·paw

variants: or less commonly papaw

Definition of pawpaw

Word Senses

1 \ pə-'pò \ : PAPAAYA

2 \ 'pä-(.)pò , 'pò- \ : a North American tree (*Asimina triloba*) of the custard-apple family with purple flowers and an edible green-skinned fruit

also : its fruit

Definition



II. Look it at how its used

“Pawpaw, Most Neglected American Fruit.” — NYTimes 1922

“Pawpaw Recommended by U.S. Food Experts, Along With Persimmon, as War Nutrition” — NYTimes 1942

“The pawpaw is also pollinated by flies and other insects rather than by honeybees...” — NYTimes 2020

“Many people also cook with ripe pawpaws, making bread, beer, ice cream, or this pawpaw pudding...” — NYTimes 2020

II. Look it at how its used

“*Pawpaw*, Most Neglected **American Fruit**.” — NYTimes 1922

“*Pawpaw* Recommended by U.S. Food Experts, Along With **Persimmon**, as War **Nutrition**” — NYTimes 1942

“The *pawpaw* is also **pollinated** by **flies** and other insects rather than by honeybees...” — NYTimes 2020

“Many people also **cook** with **ripe** *pawpaws*, making **bread**, **beer**, **ice cream**, or this *pawpaw* **pudding**...” — NYTimes 2020

Word Relations

Synonyms

- couch / sofa
- oculist / eye-doctor
- car / automobile
- water / H₂O
- draft / draught

Antonyms

- yes / no
- dark / light
- hot / cold
- up / down
- clip / clip

Word Relations

Similarity

- cat / dog
- cardiologist / pulmonologist
- car / bus
- sheep / goat
- glass / mug

Relatedness

- coffee / cup
- waiter / menu
- farm / cow
- house / roof
- theater / actor

Quantifying Similarity

Ask humans how *similar* two words are on a scale of 1-10

Word 1	Word 2	SimLex-999
area	region	9.47
horse	mare	8.33
water	ice	6.7
hill	cliff	4.28
absence	presence	0.4
princess	island	0.3

Task Design is Difficult

Similarity and **Relatedness** do not capture the same relations

Word 1	Word 2	SimLex-999	WordSim-353
coast	shore	8.83	9.10
clothes	closet	3.27	8.00

...but what about computers?

Word Embeddings

Represent each word as a **vector**

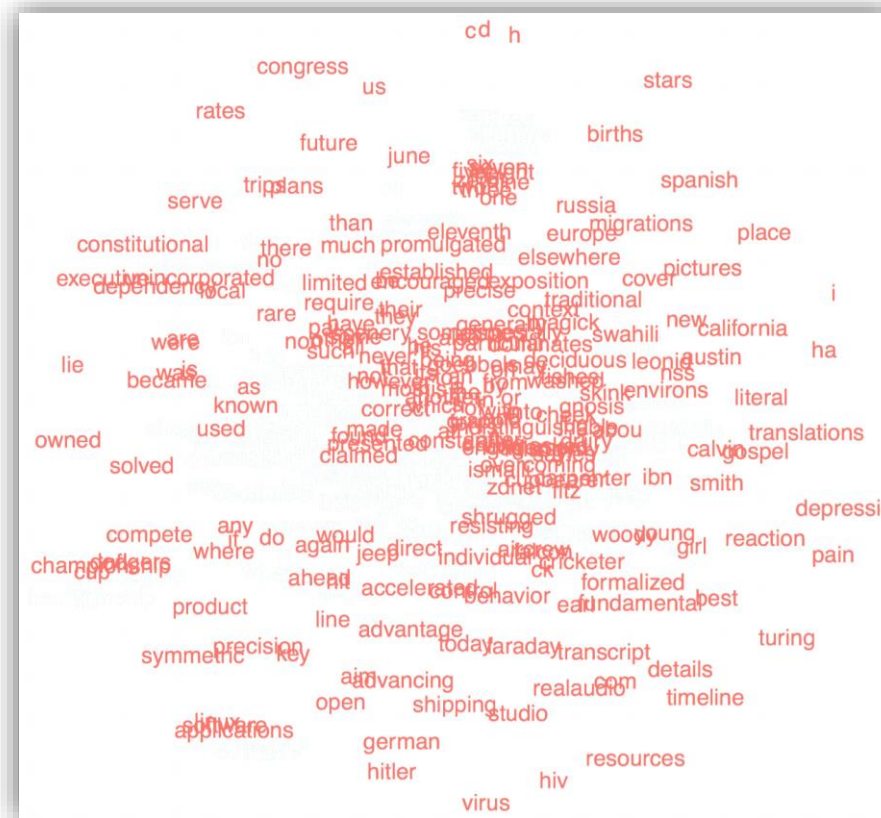
On Vectors:

- A **vector** is a list of numbers
- A **vector** can also be considered a **point** in a k -dimensional space

Capturing Word Similarity

Operationalize word similarity by computationally **comparing** vectors

Distance reflects
semantic
relationships



Closer vectors
represent
more similar words

More distant
vectors represent
less similar words



Q pawpaw



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Scott BaroooOooOOooooOooo 🟡 @sbarolo · Jul 7



#Fruitbracket Match #36:
PAPAYA vs. KIWIFRUIT



376 votes · Final results



1



4



[Show this thread](#)



Scott BaroooOooOOooooOooo 🟡 @sbarolo · Jul 5



Big Pawpaw is coming out swinging



Jeff L'épouvantail @letourjeff · Jul 5

twitter.com/sbarolo/status...

Issue:

taste



A custard-like texture



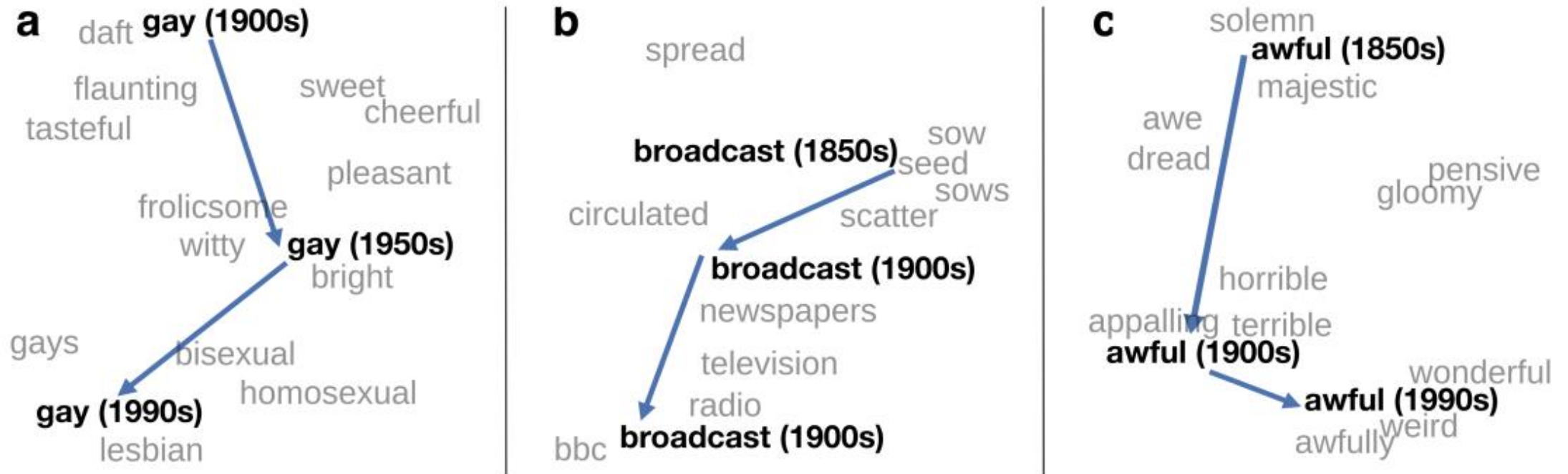
2



24



Study word use over time



One-Hot Vectors

Each word is represented by a vector with a 1 in the word's index in the vocabulary and 0's elsewhere

Term	Vector
i	$\langle 1, 0, 0, 0, 0, 0 \rangle$
hate	$\langle 0, 1, 0, 0, 0, 0 \rangle$
love	$\langle 0, 0, 1, 0, 0, 0 \rangle$
the	$\langle 0, 0, 0, 1, 0, 0 \rangle$
movie	$\langle 0, 0, 0, 0, 1, 0 \rangle$
film	$\langle 0, 0, 0, 0, 0, 1 \rangle$

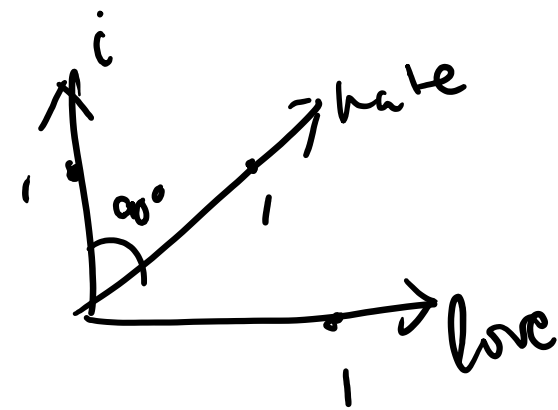
Sparsity!

Q: What are some issues with these representations?

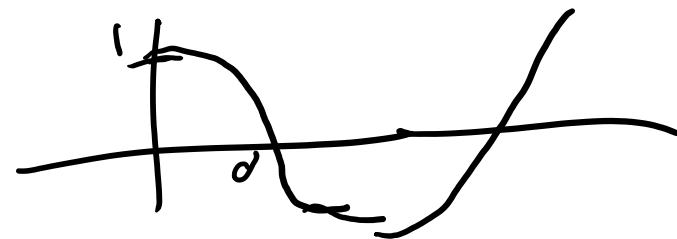
Q: What are some issues with these representations?

① Vocabularies are large!

② They're all equidistant



$$\cosine(90^\circ) = 0$$



Distributional Semantics

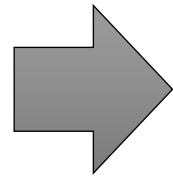
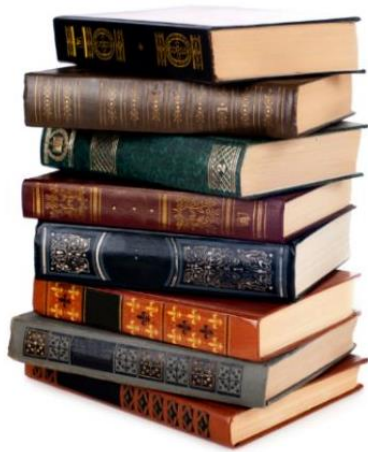
“You shall know a word by the company it keeps!” — Firth (1957)

Intuitions: Harris (1954)

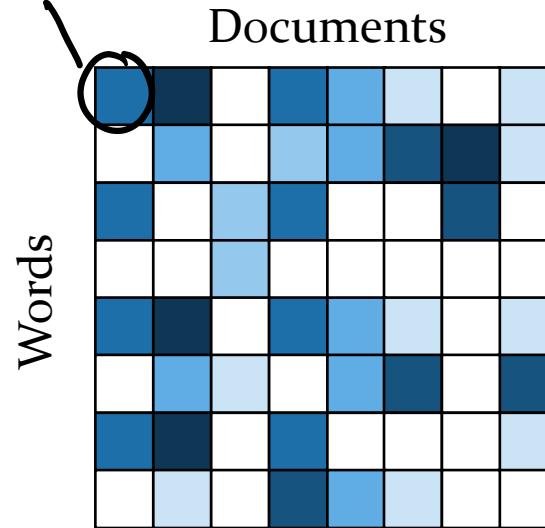
“If A and B have almost identical environments except chiefly sentences which contain both, we say they are synonyms: *oculist* and *eye-doctor*.”

petrol, gas

Build vectors based on context



words in d_i



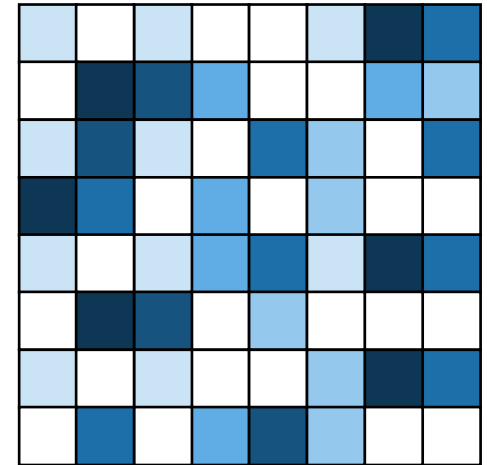
"Focus"



Words

"Context"

Words



Q: What are some issues with these representations?

Q: What are some issues with these representations?

- Still size of vocab!
- These are sparse

Trouble with raw frequency

Words occur at different frequencies irrespective of context

So, raw frequency does not necessarily correspond to significant, informative use.

Peach, Fruit → relationship

the, Fruit

the, Peach

→ not so meaningful

Move away from raw frequency

Term-Document Matrix

Apply tf-idf weighting

$$= \frac{\textit{term frequency}}{\textit{document frequency}}$$

tf : raw count
"freq" $\frac{\text{raw count}}{\text{total}}$

Word-Context Matrix

Use PPMI (Positive Pointwise Mutual Information)

$$= \max(\textit{PMI}(w_a, w_b), 0)$$

$$= \max\left(\log_2 \frac{P(w_a, w_b)}{P(w_a)P(w_b)}, 0\right)$$

Move to smaller, dense embeddings

Use **matrix factorization** to build a more compact representation

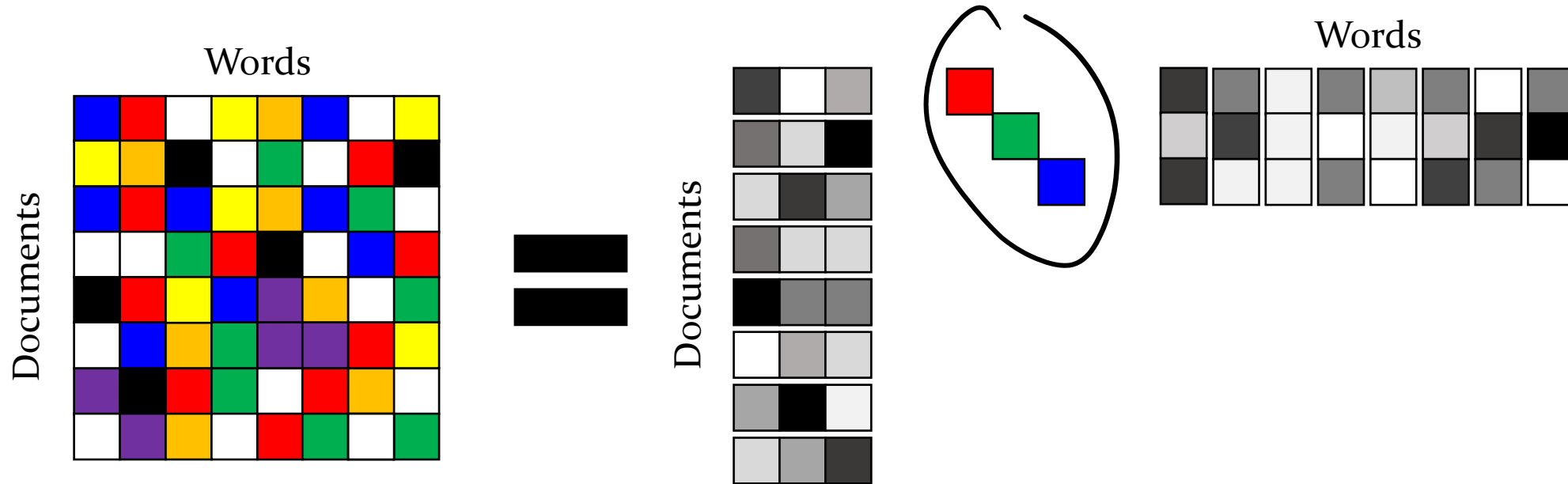
Matrix factorization *decomposes* a matrix into the product of several (smaller) matrices

E.g., Singular Value
Decomposition (SVD)

$$\mathbf{M}_{m \times n} = \mathbf{U}_{m \times m} \mathbf{\Sigma}_{m \times n} \mathbf{V}^*_{n \times n}$$

\downarrow
 k

Latent Semantic Analysis (LSA)

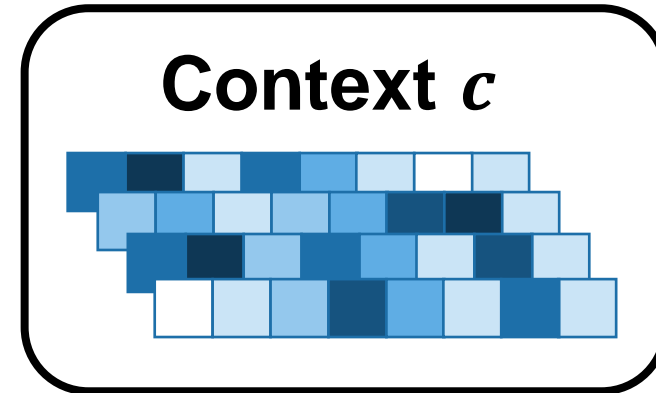
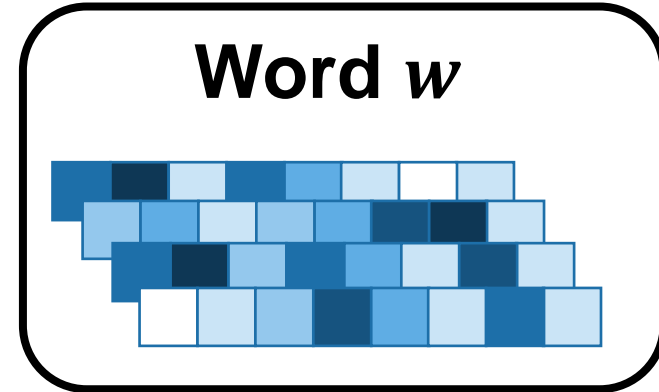
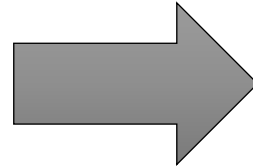
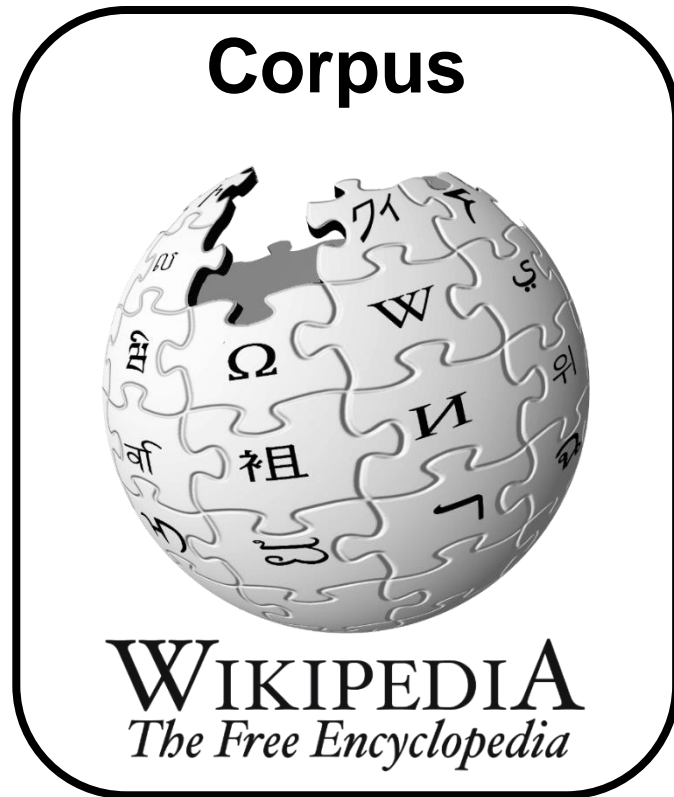


Newer, neural models also use matrix factorization

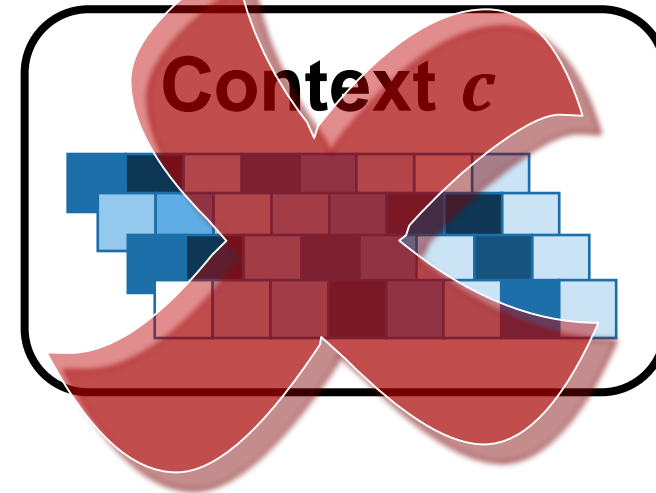
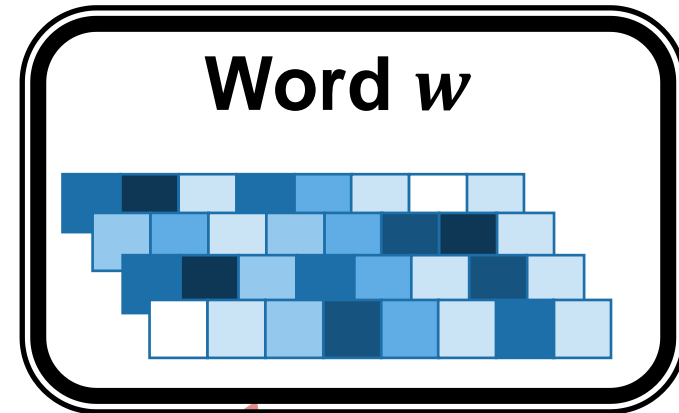
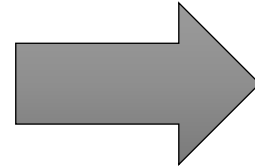
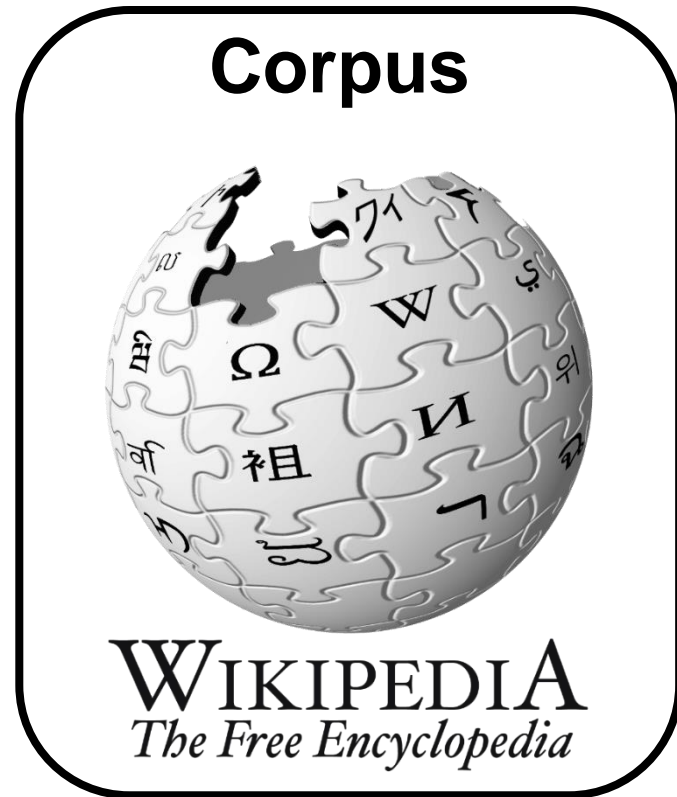
E.g., GloVE and SGNS

word2vec

Neural Word Embeddings



Neural Word Embeddings



Skip-Gram with Negative Sampling (SGNS)

The brown fox jumps over the lazy dog.



SGNS: Skip-Gram Model

The brown fox **jumps** over the lazy dog.



SGNS: Skip-Gram Model

The brown fox jumps over the lazy dog.

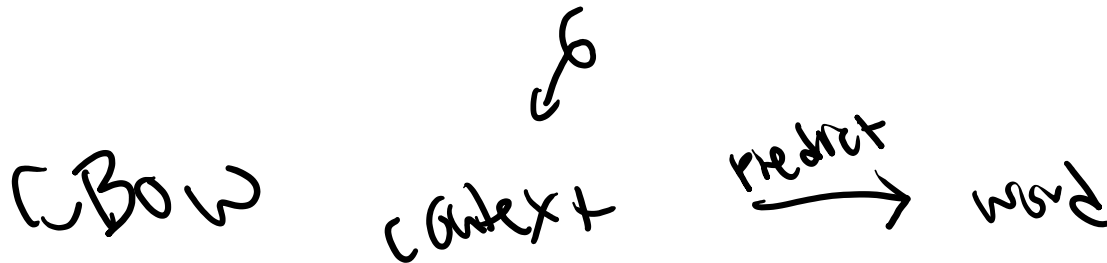
Context Window Size = 2

SGNS: Skip-Gram Model

The brown fox **jumps** over the lazy dog.

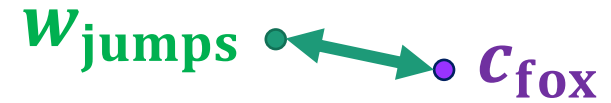
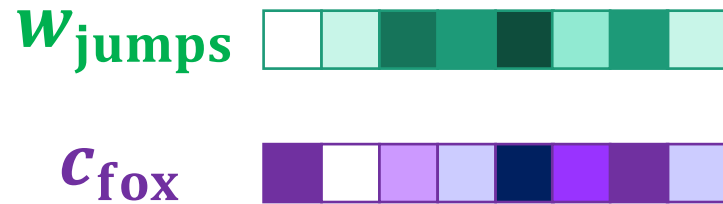
Context Window Size = 2

jumps → { brown, fox, over, the }



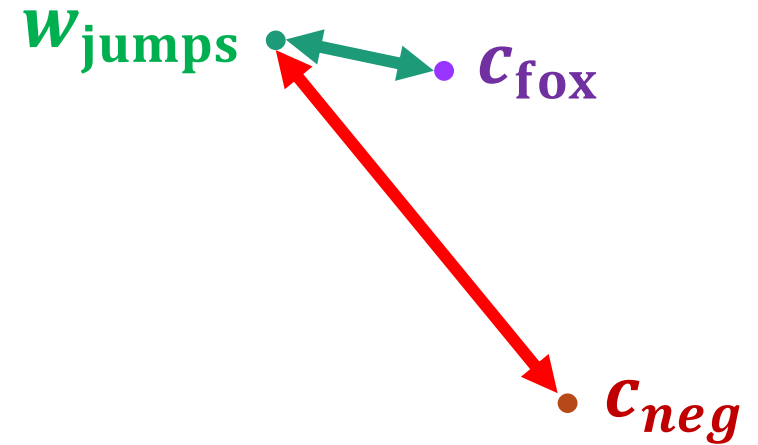
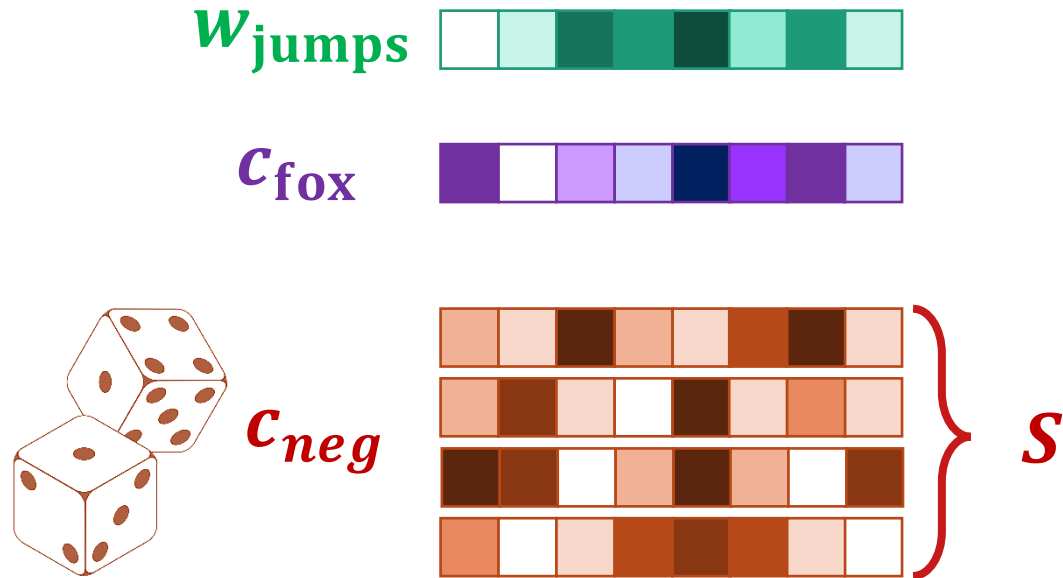
SGNS: Negative Sampling

Co-occurrence **jumps**, **fox**:



SGNS: Negative Sampling

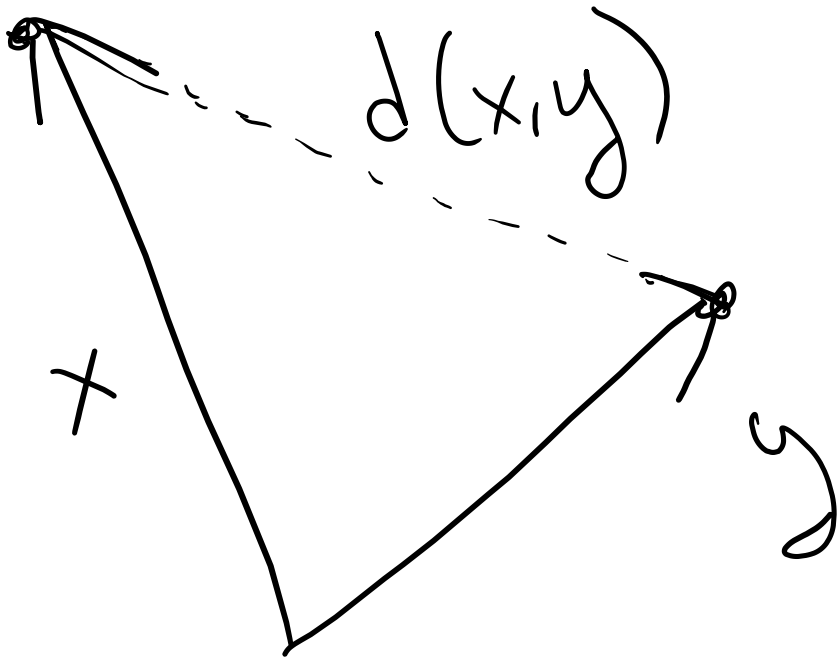
Co-occurrence **jumps**, **fox**:



How do we compare vectors?

- Similarity measurements
 - Larger values \rightarrow similar vectors \rightarrow similar words
 - Smaller values \rightarrow dissimilar vectors \rightarrow dissimilar words
- Distance / dissimilarity measurements
 - Note: distance metric requires triangle inequality
 - Larger values \rightarrow dissimilar vectors \rightarrow dissimilar words
 - Smaller values \rightarrow similar vectors \rightarrow similar words

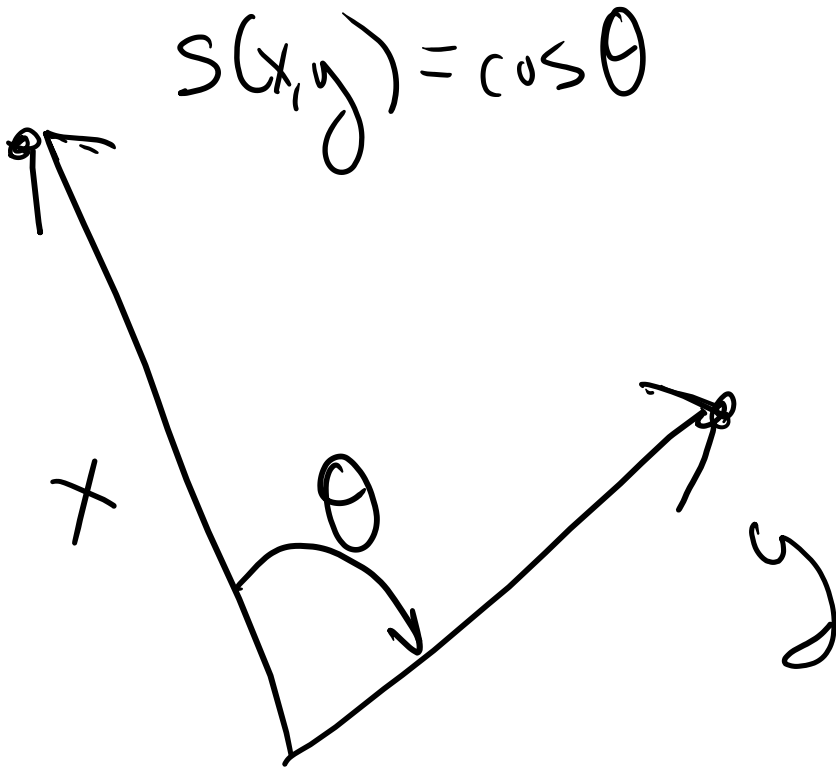
Euclidean Distance



$$d(x, y) = \sqrt{\sum_i (x_i - y_i)^2}$$

Issue: Vector length depends on frequency. More frequent words will have longer vectors.

Cosine Similarity

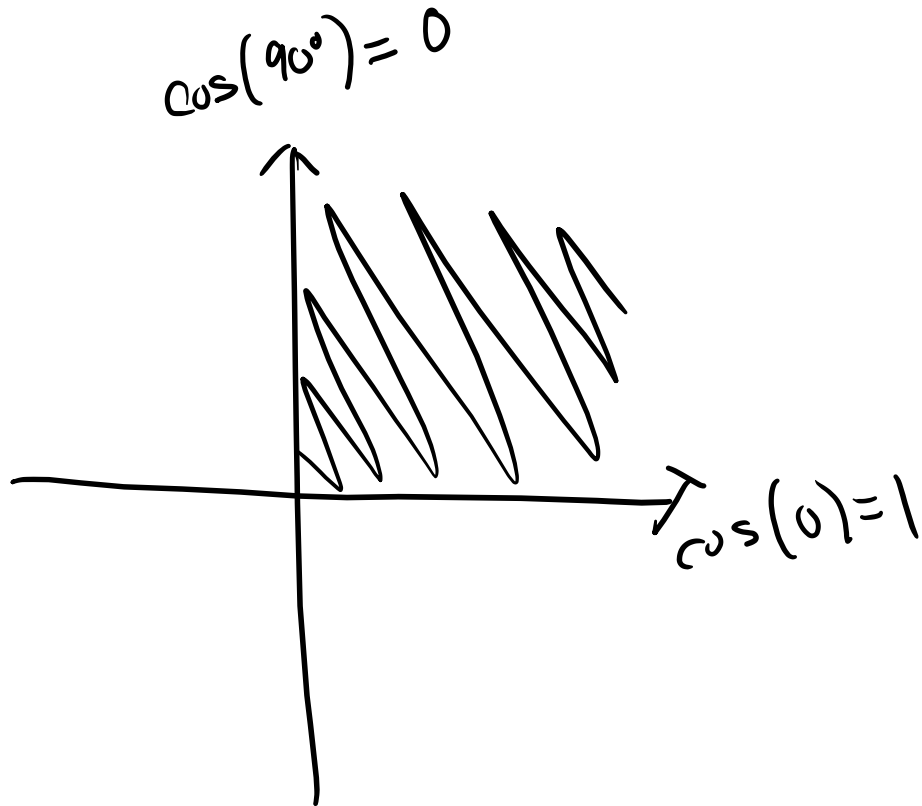


$$s(x, y) = \frac{x \cdot y}{|x||y|}$$

Only depends on vector angle

Range: [-1, 1]

Non-negative vectors & cosine similarity



If all vectors have non-negative values, then their cosine similarity will be between 0 and 1

