

Constituency Parsing: CKY

CS 485, Fall 2023

Applications of Natural Language Processing

https://people.cs.umass.edu/~brenocon/cs485_f23/

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Context-Free Grammar

- CFG describes a generative process for an (infinite) set of strings

- 1. Nonterminal symbols
 - “S”: START symbol / “Sentence” symbol
- 2. Terminal symbols: word vocabulary
- 3. Rules (a.k.a. Productions). Practically, two types:

Noun → flight
Noun → breeze
 ...

“Grammar”: one NT expands to ≥ 1 NT
 always one NT on left side of rule

Lexicon: NT expands to a terminal

<i>S</i>	→	<i>NP VP</i>	I + want a morning flight
<i>NP</i>	→	<i>Pronoun</i>	I
		<i>Proper-Noun</i>	Los Angeles
		<i>Det Nominal</i>	a + flight
<i>Nominal</i>	→	<i>Nominal Noun</i>	morning + flight
		<i>Noun</i>	flights
<i>VP</i>	→	<i>Verb</i>	do
		<i>Verb NP</i>	want + a flight
		<i>Verb NP PP</i>	leave + Boston + in the morning
		<i>Verb PP</i>	leaving + on Thursday
<i>PP</i>	→	<i>Preposition NP</i>	from + Los Angeles

<i>Noun</i>	→	<i>flights</i> <i>breeze</i> <i>trip</i> <i>morning</i> ...
<i>Verb</i>	→	<i>is</i> <i>prefer</i> <i>like</i> <i>need</i> <i>want</i> <i>fly</i>
<i>Adjective</i>	→	<i>cheapest</i> <i>non-stop</i> <i>first</i> <i>latest</i> <i>other</i> <i>direct</i> ...
<i>Pronoun</i>	→	<i>me</i> <i>I</i> <i>you</i> <i>it</i> ...
<i>Proper-Noun</i>	→	<i>Alaska</i> <i>Baltimore</i> <i>Los Angeles</i> <i>Chicago</i> <i>United</i> <i>American</i> ...
<i>Determiner</i>	→	<i>the</i> <i>a</i> <i>an</i> <i>this</i> <i>these</i> <i>that</i> ...
<i>Preposition</i>	→	<i>from</i> <i>to</i> <i>on</i> <i>near</i> ...
<i>Conjunction</i>	→	<i>and</i> <i>or</i> <i>but</i> ...

Constituent Parse Trees

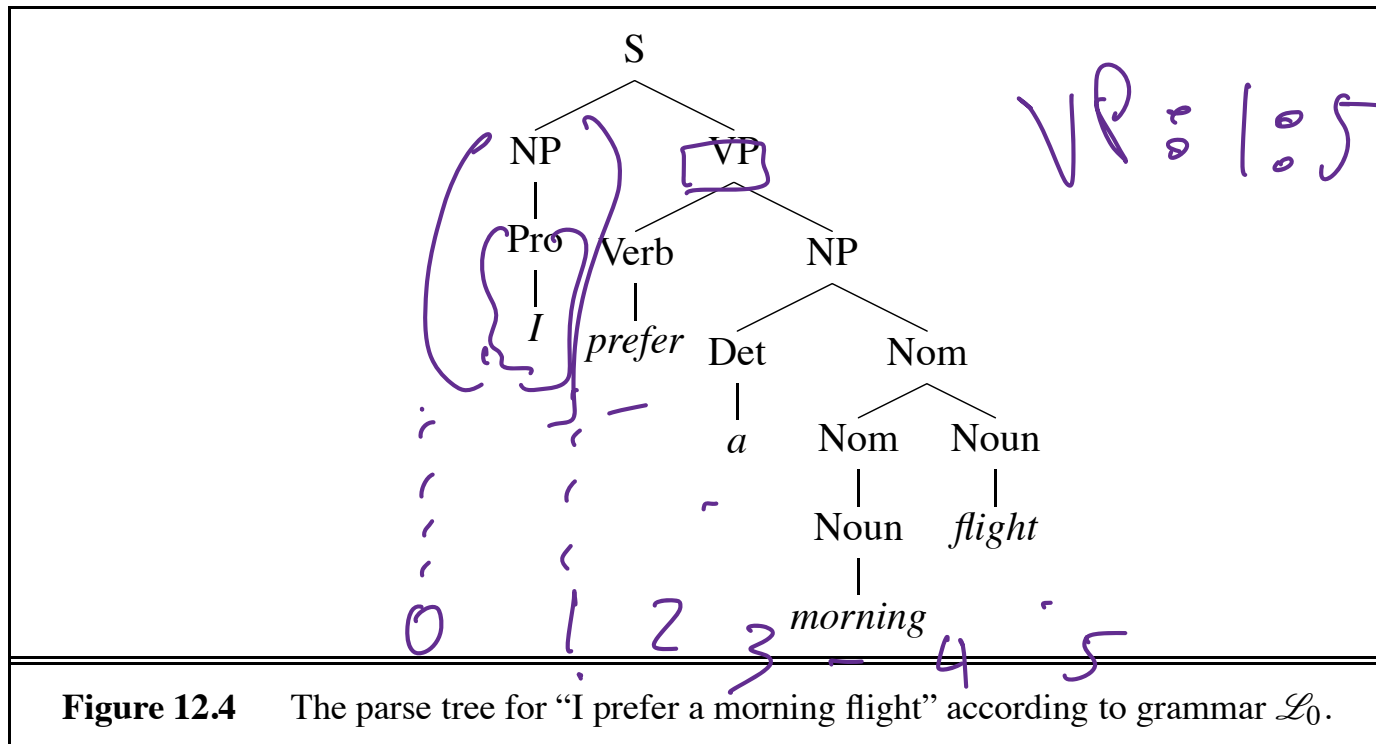


Figure 12.4 The parse tree for “I prefer a morning flight” according to grammar \mathcal{L}_0 .

Bracket notation

(12.2)

$[S [NP [Pro I]] [VP [V prefer] [NP [Det a] [Nom [N morning] [Nom [N flight]]]]]]]$

$\langle \Rightarrow \rangle$ Set of non-terminal spans (start, end positions)

$\{(NP, 0, 1), (VP, 1, 5), (NP, 2, 5), \dots\}$

Can you have a set that's illegal as tree? Yes.

Parsing with a CFG

- Task: given text and a CFG, answer:

- Does there exist at least one parse?
- Enumerate parses (backpointers)

\Leftrightarrow

is the string (text) grammatical (in this CFG)?

- Problem: extremely high number of possible trees for a sentence, and even a large number of *legal* trees (licensed by the grammar) for a sentence

- Many parsing algorithms have been invented to tackle this

- Cocke-Kasami-Younger algorithm (CKY)

- Bottom-up dynamic programming:

Find possible nonterminals for short spans of sentence, then possible combinations for higher spans

- *Maintains* local ambiguity, representing many subtrees for each span. ("Packed forest" representation)

- Provably finds all possible parse trees (legal derivations), and correctly says when none exist.

- Requires converting to Chomsky Normal Form (binarization)

Chomsky Normal Form

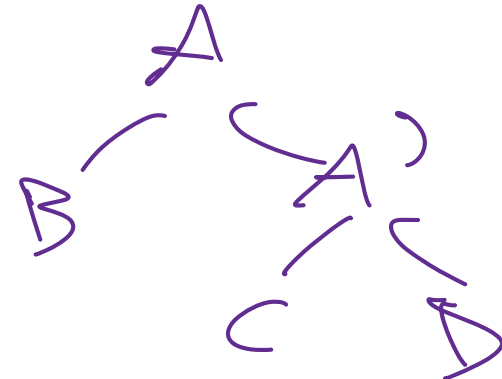
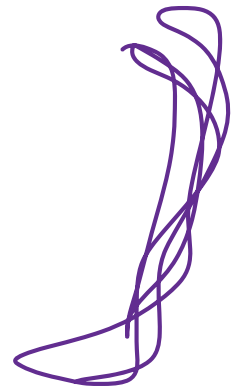
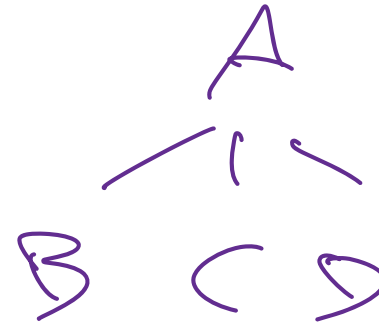
(binarized grammar)



(orig) $A \rightarrow B C D$



(now CNF)
 $A \rightarrow B A'$
 $A' \rightarrow C D$



binarized tree

CKY

Grammar

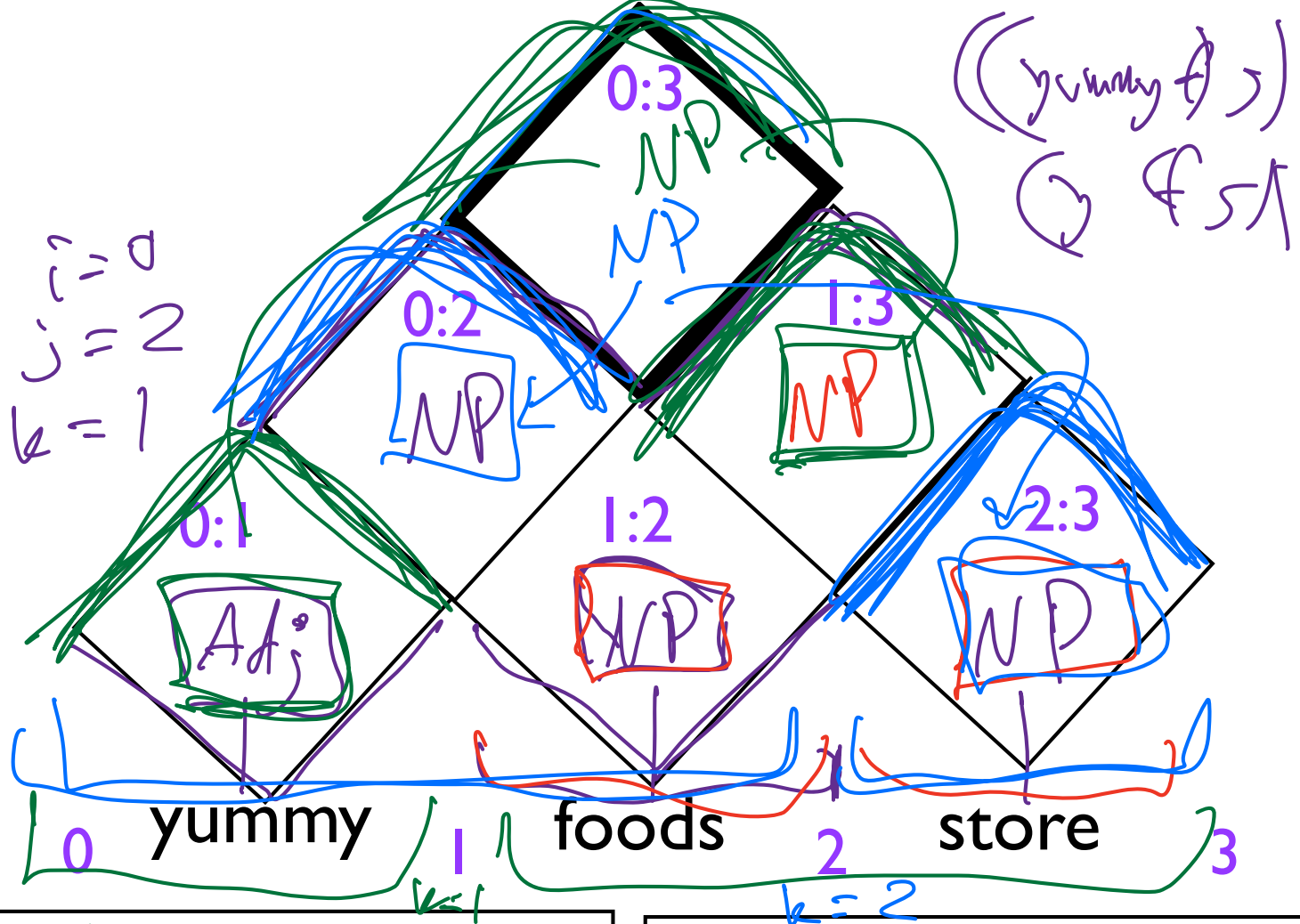
Adj \rightarrow yummy

NP \rightarrow foods

NP \rightarrow store

NP \rightarrow NP NP

NP \rightarrow Adj NP



For cell $[i,j]$ (loop through them bottom-up)

For possible splitpoint $k=(i+1)..(j-1)$:

For every B in $[i,k]$ and C in $[k,j]$,

If exists rule $A \rightarrow B C$,

add A to cell $[i,j]$ (Recognizer)

... or ...

add (A,B,C, k) to cell $[i,j]$ (Parser)

Recognizer: per span, record list of possible nonterminals

Parser: per span, record possible ways the nonterminal was constructed.

CKY

Grammar

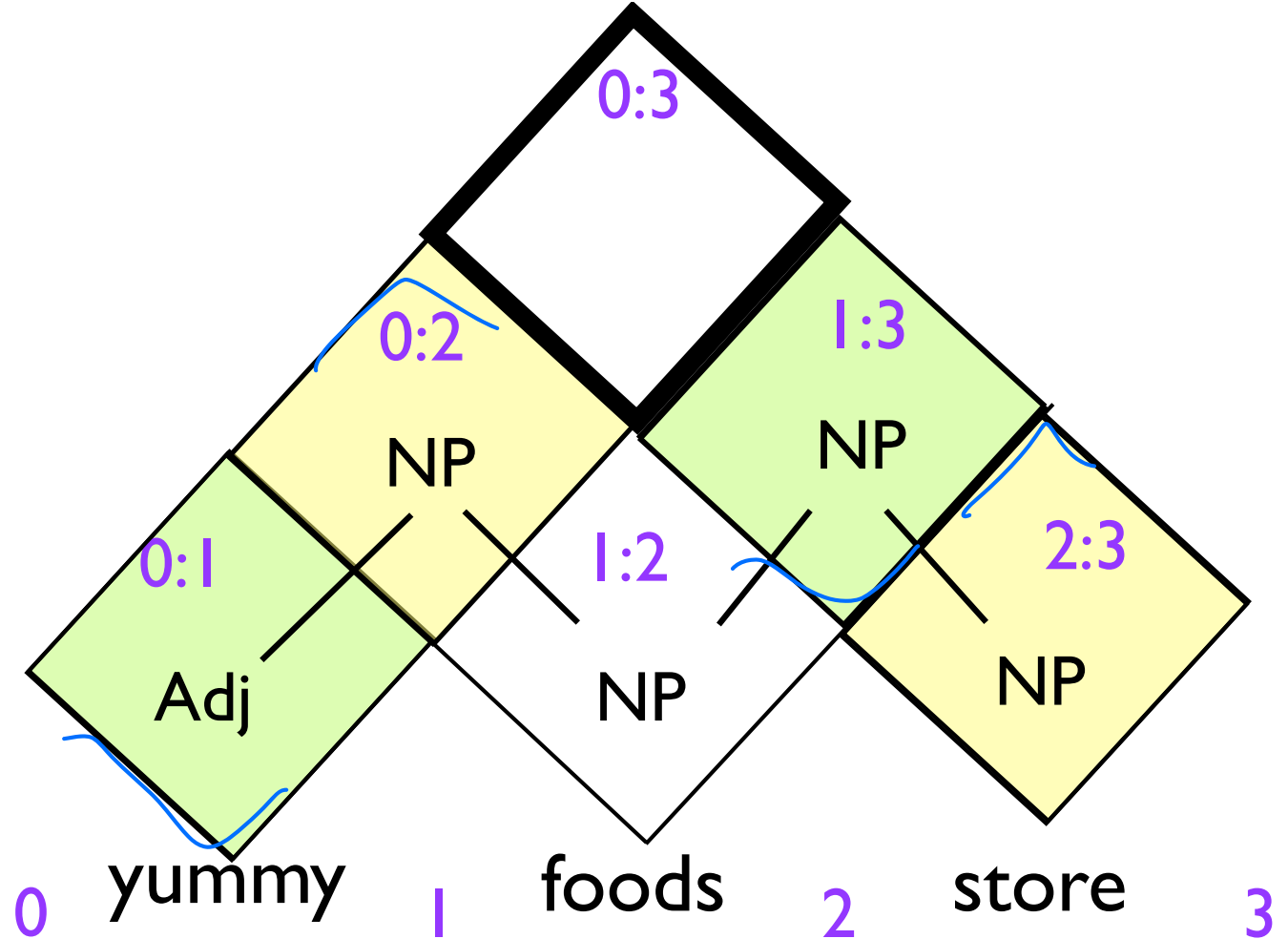
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CKY

Grammar

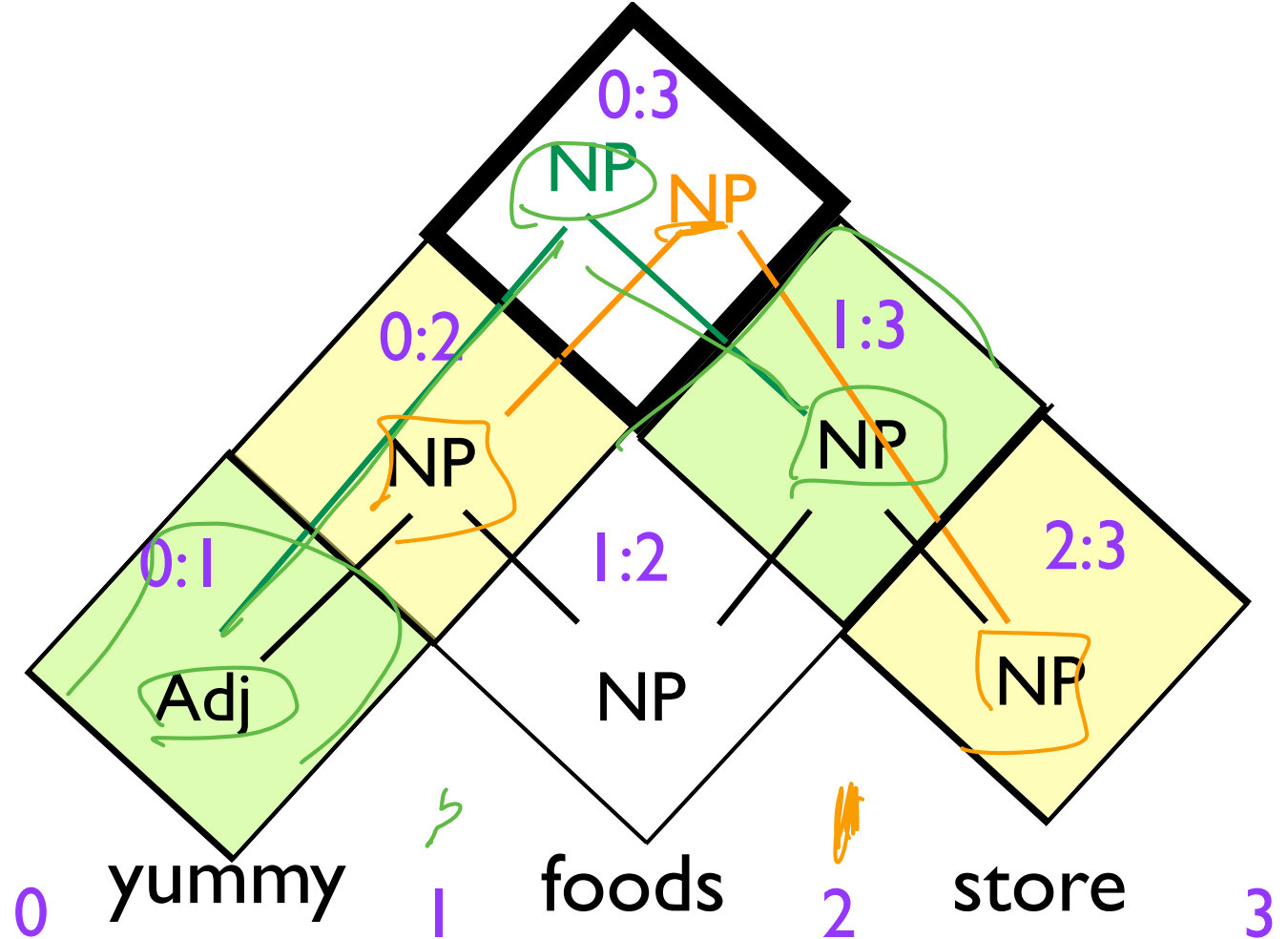
Adj -> yummy

NP -> foods

NP -> store

NP -> NP NP

NP -> Adj NP



For cell $[i,j]$ (loop through them bottom-up)

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S → NP VP

NP → NP PP

VP → V NP

VP → VP PP

PP → P NP

NP → she

NP → fish

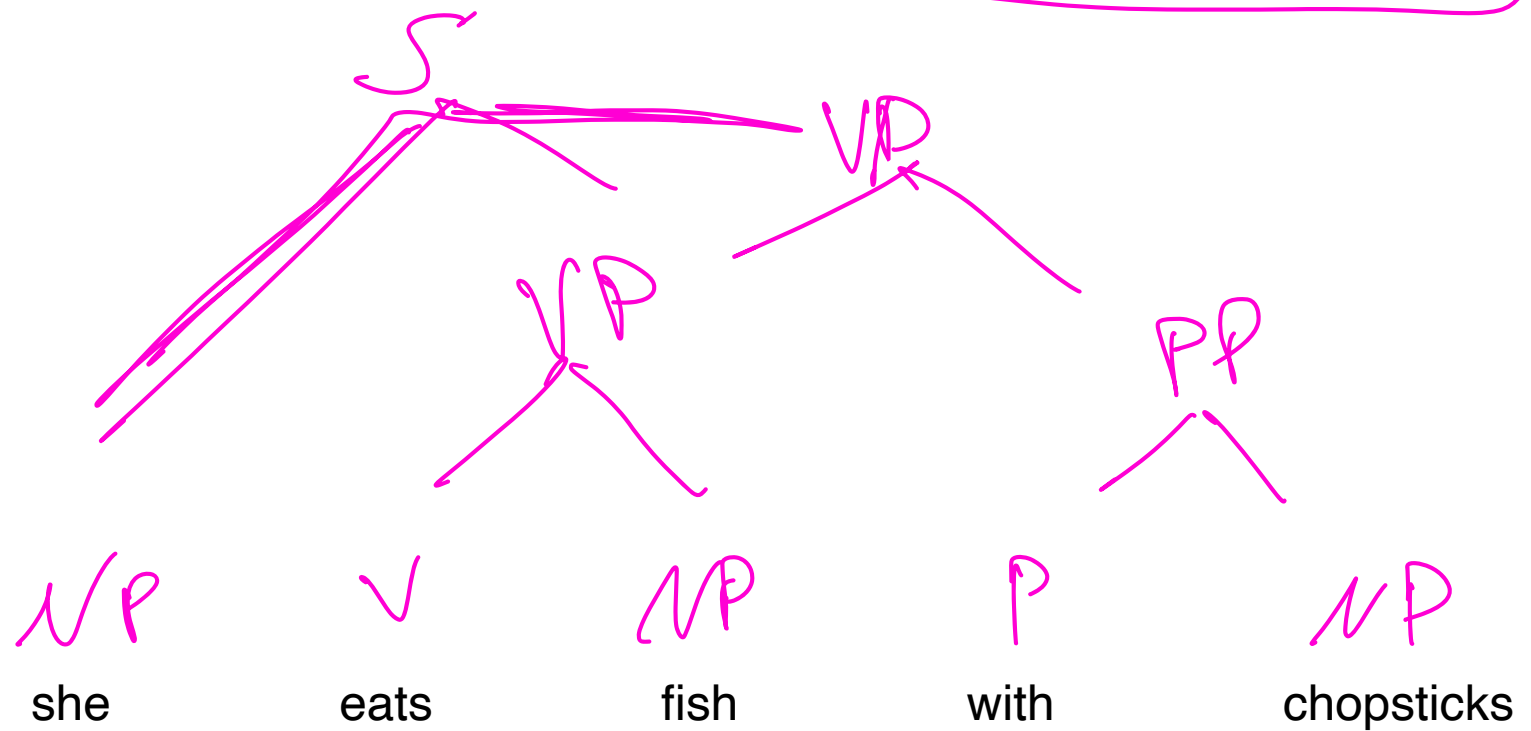
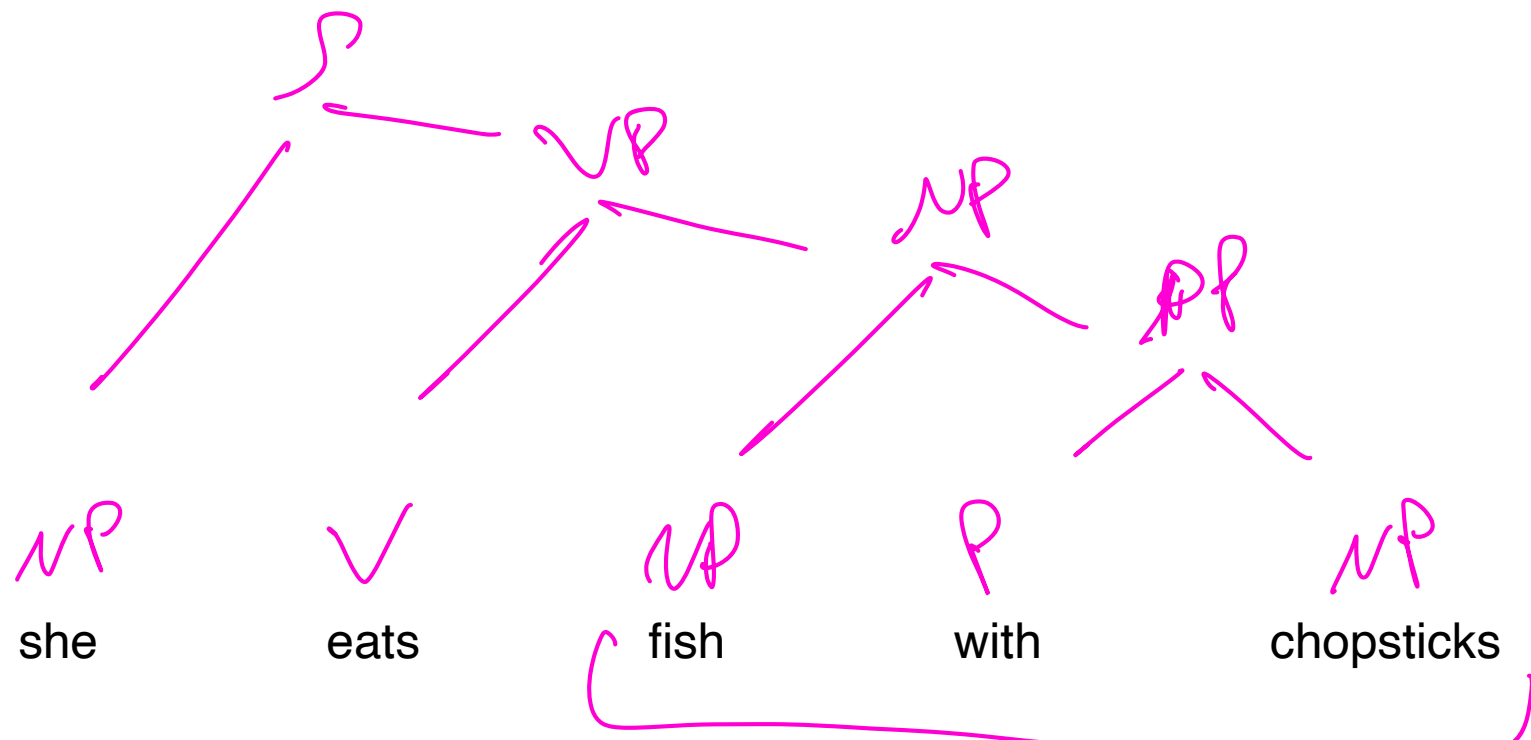
NP → fork

NP → chopsticks

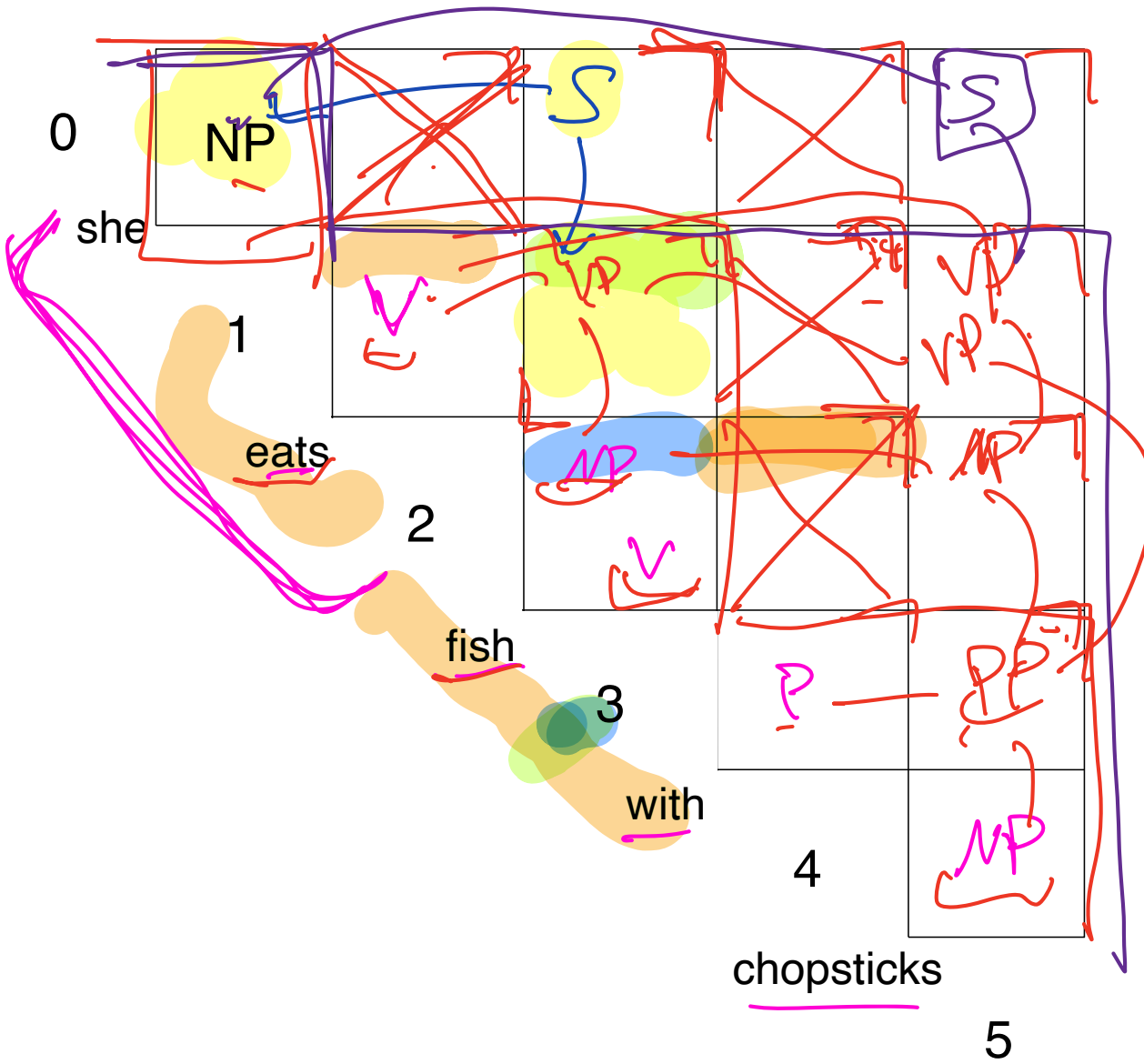
V → eats

V → fish

P → with



Fill in the CYK dynamic programming table to parse the sentence below. In the bottom right corner, draw the two parse trees. Show the possible nonterminals in each cell. Optional: draw the backpointers too.

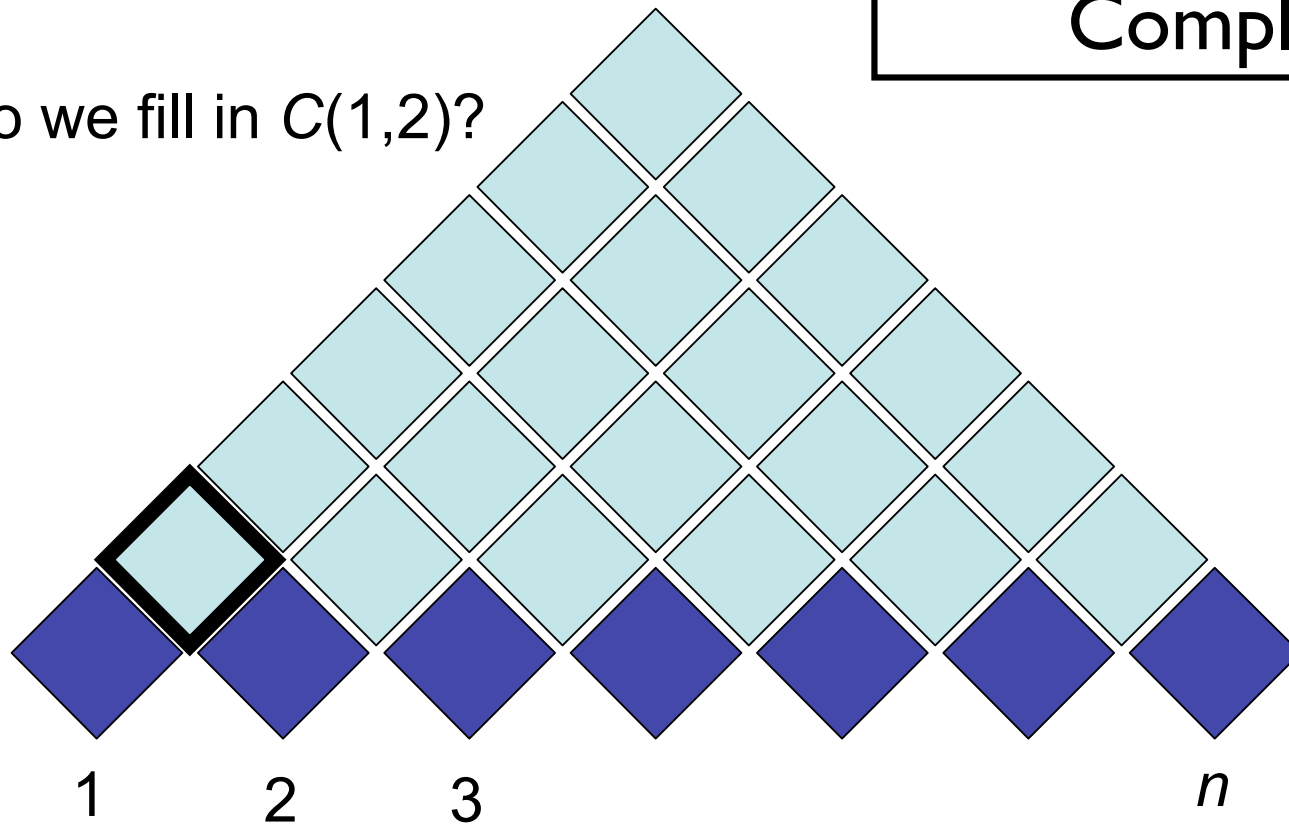


- S → NP VP
 - NP → NP PP
 - VP → V NP
 - VP → ~~VP PP~~
 - PP → P NP
- NP → she
 - NP → fish
 - NP → fork
 - NP → chopsticks
 - V → eats
 - V → fish
 - P → with

For cell $[i,j]$
For possible splitpoint $k=(i+1)..(j-1)$:
For every B in $[i,k]$ and C in $[k,j]$,
If exists rule $A \rightarrow B C$,
add A to cell $[i,j]$

Computational
Complexity ?

How do we fill in $C(1,2)$?



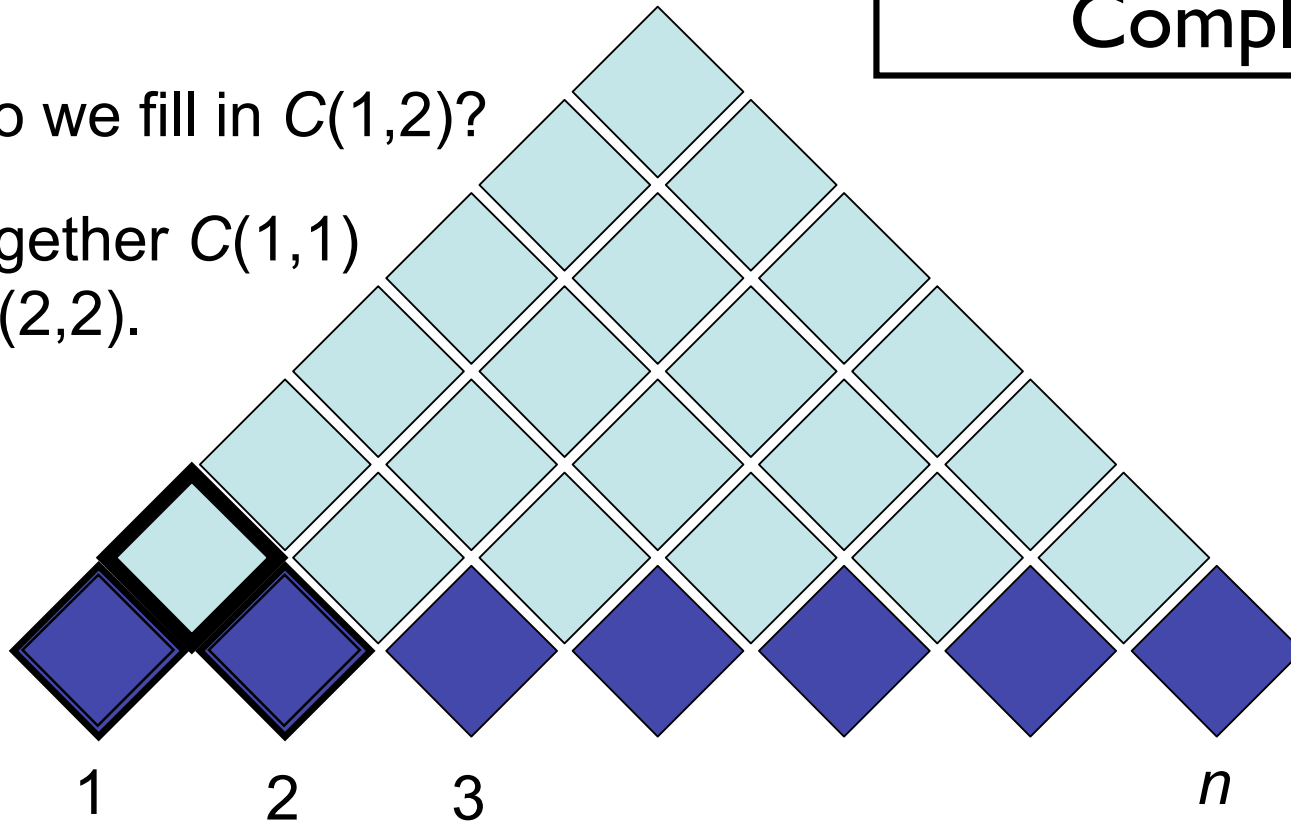
[Example from Noah Smith]

For cell $[i,j]$
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Computational
Complexity ?

How do we fill in $C(1,2)$?

Put together $C(1,1)$
and $C(2,2)$.

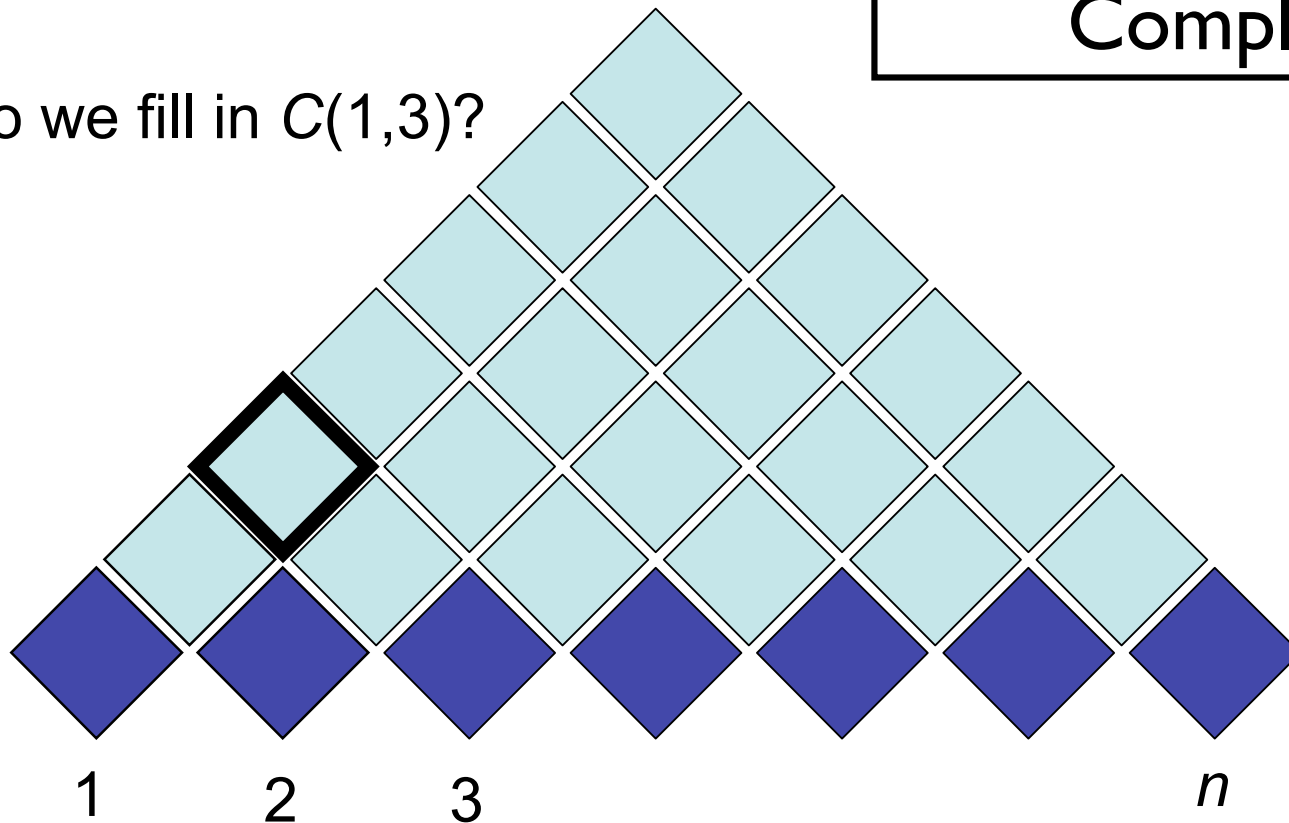


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Computational
Complexity ?

How do we fill in $C(1,3)$?



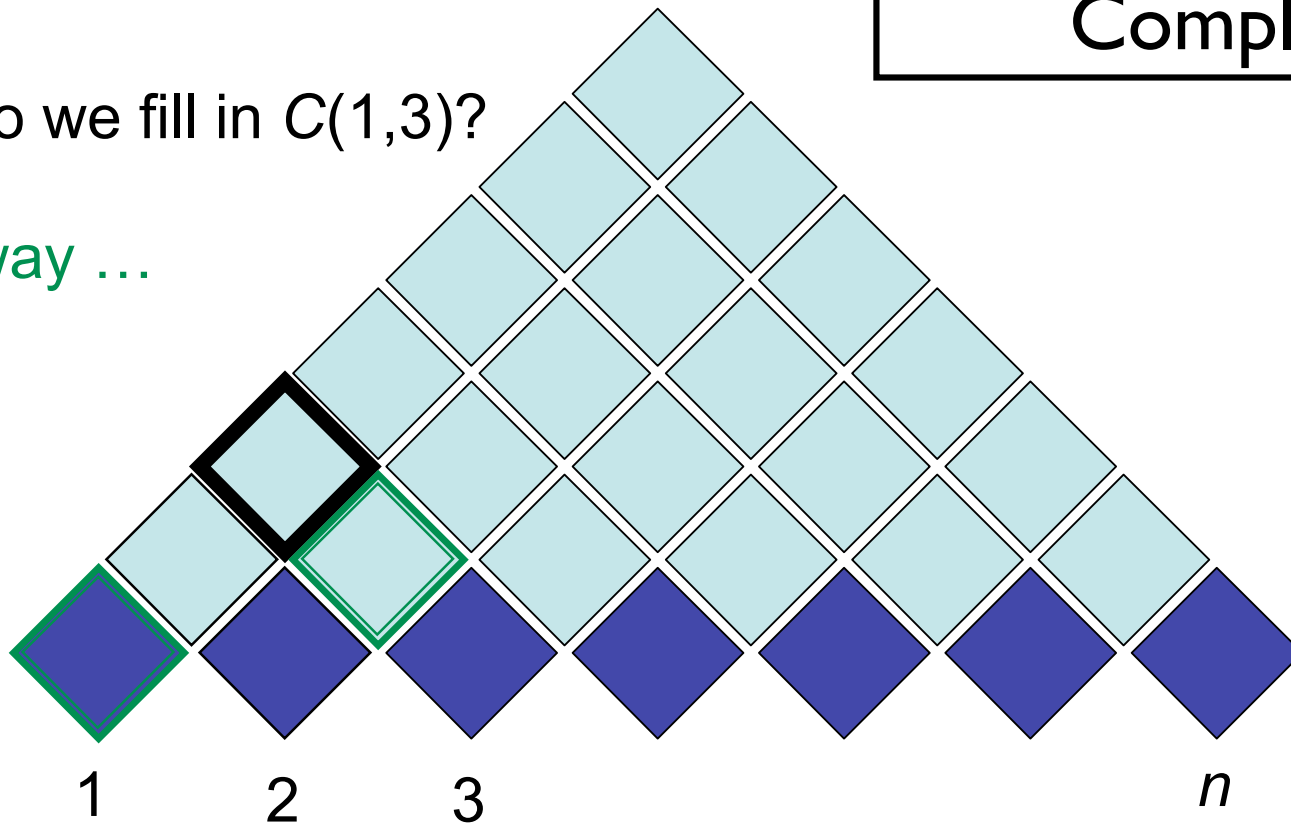
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Computational
Complexity ?

How do we fill in $C(1,3)$?

One way ...



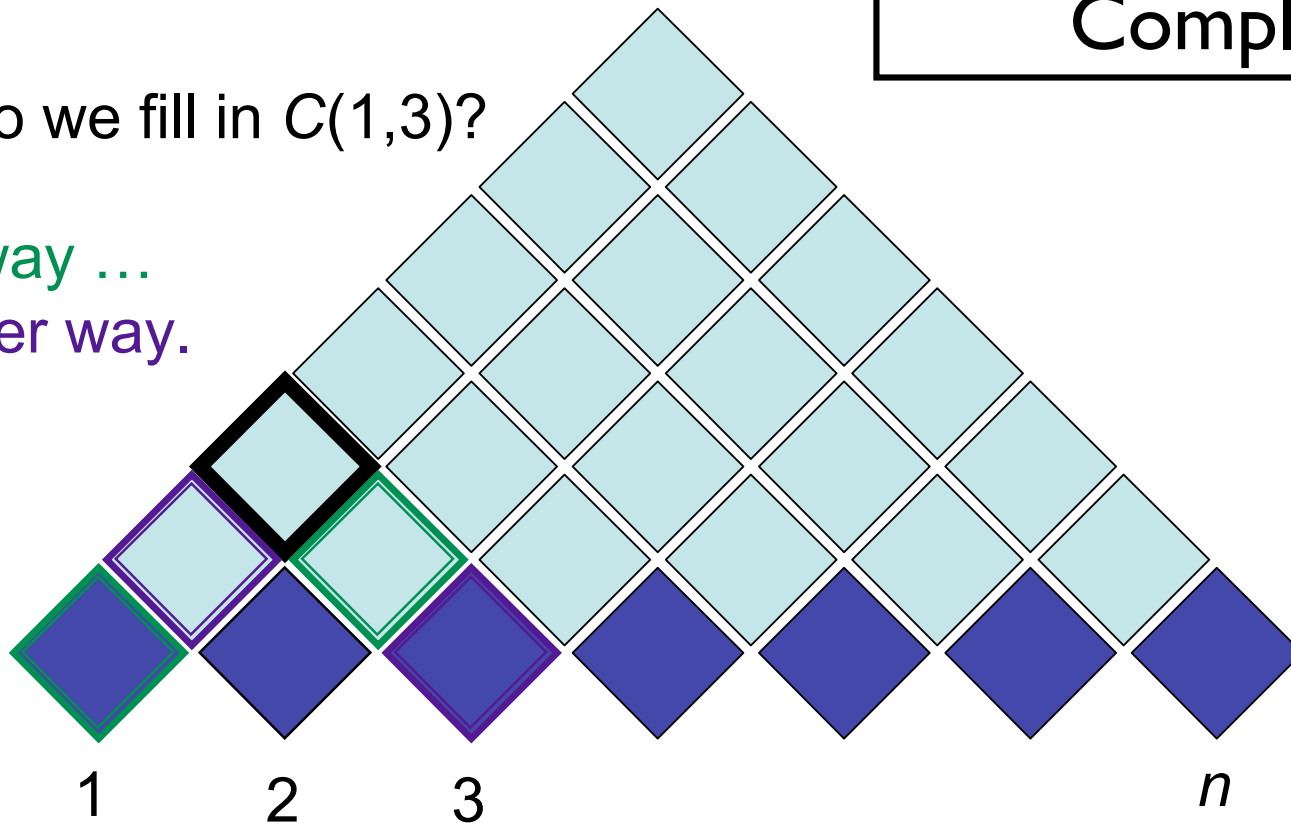
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Computational
Complexity ?

How do we fill in $C(1,3)$?

One way ...
Another way.

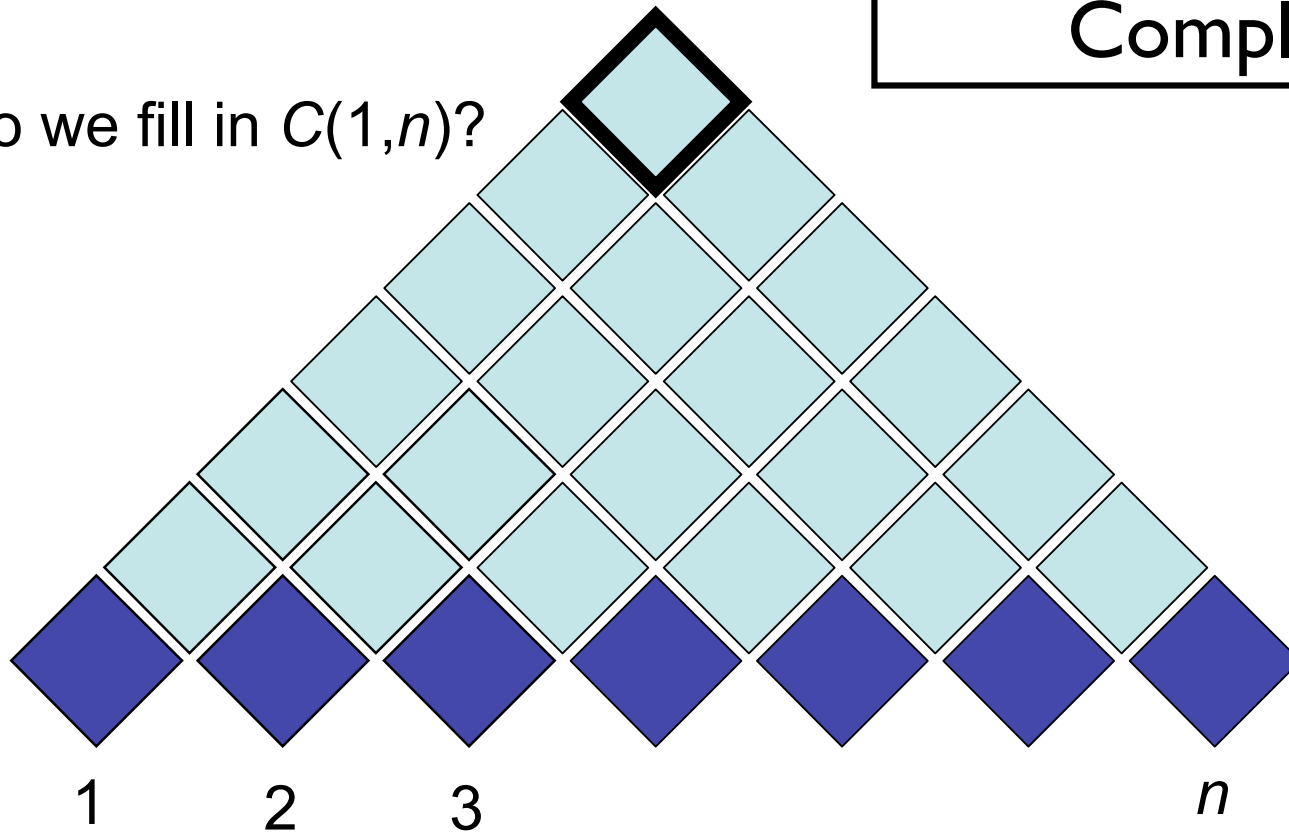


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Computational
Complexity ?

How do we fill in $C(1,n)$?



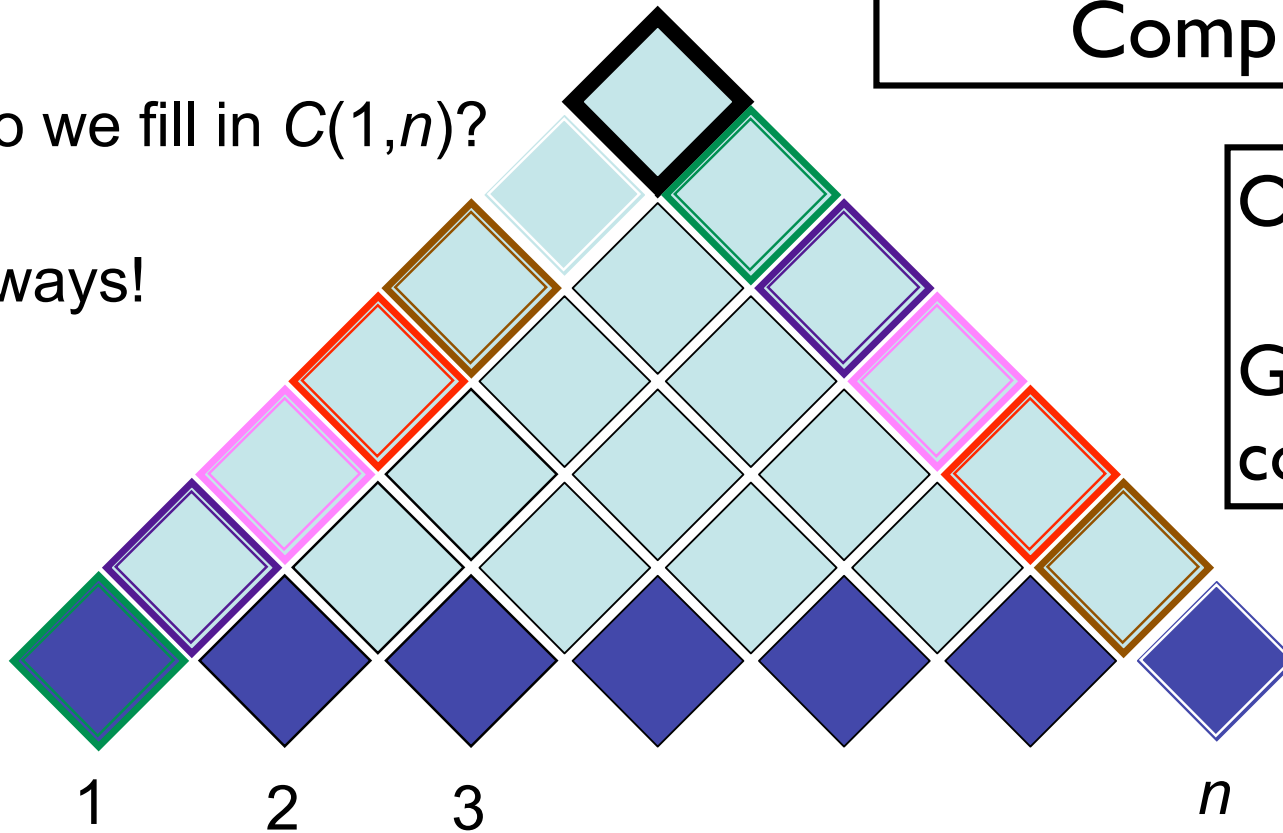
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Computational
Complexity ?

How do we fill in $C(1,n)$?

$n - 1$ ways!



$O(G n^3)$

$G =$ grammar
constant

[Example from Noah Smith]

Probabilistic CFGs

$S \rightarrow NP VP$	[.80]	$Det \rightarrow that$	[.10]		a	[.30]		the	[.60]
$S \rightarrow Aux NP VP$	[.15]	$Noun \rightarrow book$	[.10]		$flight$	[.30]			
$S \rightarrow VP$	[.05]				$meal$	[.15]		$money$	[.05]
$NP \rightarrow Pronoun$	[.35]				$flights$	[.40]		$dinner$	[.10]
$NP \rightarrow Proper-Noun$	[.30]	$Verb \rightarrow book$	[.30]		$include$	[.30]			
$NP \rightarrow Det Nominal$	[.20]				$prefer;$	[.40]			
$NP \rightarrow Nominal$	[.15]	$Pronoun \rightarrow I$	[.40]		she	[.05]			
$Nominal \rightarrow Noun$	[.75]				me	[.15]		you	[.40]
$Nominal \rightarrow Nominal Noun$	[.20]	$Proper-Noun \rightarrow Houston$	[.60]						
$Nominal \rightarrow Nominal PP$	[.05]				TWA	[.40]			
$VP \rightarrow Verb$	[.35]	$Aux \rightarrow does$	[.60]		can	[.40]			
$VP \rightarrow Verb NP$	[.20]	$Preposition \rightarrow from$	[.30]		to	[.30]			
$VP \rightarrow Verb NP PP$	[.10]				on	[.20]		$near$	[.15]
$VP \rightarrow Verb PP$	[.15]				$through$	[.05]			
$VP \rightarrow Verb NP NP$	[.05]								
$VP \rightarrow VP PP$	[.15]								
$PP \rightarrow Preposition NP$	[1.0]								

- Defines a probabilistic generative process for words in a sentence
- (How to learn? Fully supervised with a treebank...)

Penn Treebank

```

( (S
  (NP-SBJ (NNP General) (NNP Electric) (NNP Co.) )
  (VP (VBD said)
    (SBAR (-NONE- 0)
      (S
        (NP-SBJ (PRP it) )
        (VP (VBD signed)
          (NP
            (NP (DT a) (NN contract) )
            (PP (-NONE- *ICH*-3) ))
            (PP (IN with)
              (NP
                (NP (DT the) (NNS developers) )
                (PP (IN of)
                  (NP (DT the) (NNP Ocean) (NNP State) (NNP Power) (NN project) ))))
            (PP-3 (IN for)
              (NP
                (NP (DT the) (JJ second) (NN phase) )
                (PP (IN of)
                  (NP
                    (NP (DT an) (JJ independent)
                      (ADJP
                        (QP ($ $) (CD 400) (CD million) )
                        (-NONE- *U*) )
                      (NN power) (NN plant) )
                    (, ,)
                    (SBAR
                      (WHNP-2 (WDT which) )
                      (S
                        (NP-SBJ-1 (-NONE- *T*-2) )
                        (VP (VBZ is)
                          (VP (VBG being)
                            (VP (VBN built)
                              (NP (-NONE- *-1) )
                              (PP-LOC (IN in)
                                (NP
                                  (NP (NNP Burrillville) )
                                  (, ,)
                                  (NP (NNP R.I) ))))))))))))))))
          )
        )
      )
    )
  )
)

```

PCFG as LM

Is a PCFG a *good* LM? Yes...

Is a PCFG a *good* LM? No...

(P)CFG model, (P)CKY algorithm

- CKY: given CFG and sentence w
 - Does there exist at least one parse?
 - Enumerate parses (backpointers)
- Probabilistic CKY: given PCFG and sentence w
 - Likelihood of sentence $P(w)$
 - Most probable parse (“Viterbi parse”)
 $\operatorname{argmax}_y P(y \mid w) = \operatorname{argmax}_y P(y, w)$

- Parsing model accuracy: lots of ambiguity!!
 - PCFGs lack lexical information to resolve ambiguities (sneak in world knowledge?)
 - Modern constituent parsers: enrich PCFG with lexical information and fine-grained nonterminals
 - Modern dependency parsers: effectively the same trick
- Parsers' computational efficiency
 - Grammar constant; pruning & heuristic search
 - $O(N^3)$ for CKY (ok? depends...)
 - $O(N)$ left-to-right incremental algorithms
- What was the syntactic training data?