Lecture 5

1 Required Reading

Read Chapters 16 and 17 of Programming in Scala.

2 Partial Functions and Signalling Errors

Many functions are not defined on all inputs. For example, if you’re reading input from a keyboard (i.e., a string) and want to parse the string as a number, you can apply `Integer.parseInt`:

```scala
scala> val n = Integer.parseInt("10")
n: Int = 10
```

But, if the string is not a numeral, you get an exception:

```scala
scala> val n = Integer.parseInt("ten")
java.lang.NumberFormatException: For input string: "ten"
```

You’ve encountered other ways of signalling errors. For example, if you lookup an unbound key in a hashtable, Java (and Scala) produce `nulls`:

```scala
scala> val ht = new java.util.Hashtable[Int, String]()
ht: java.util.Hashtable[Int, String] = {}
scala> ht.put(10, "hello")
scala> val r = ht.get(20)
r: String = null
```

Finally, here is a more insidious example. The following function calculates the point where two lines, defined by \( y = m_1 x + b_1 \) and \( y = m_2 x + b_2 \), intersect. The function is not defined when the two lines are parallel (i.e., when their slopes are the same, or \( m_1 = m_2 \)):

```scala
case class Point(x: Double, y: Double)
def inter(m1: Double, b1: Double, m2: Double, b2: Double): Point = {
    val x = (b2 - b1) / (m1 - m2)
    Point(x, m1 * x + b1)
}
```

When the slopes are the same, the denominator, \( m_1 - m_2 \) is 0. So, you might expect a divide-by-zero `ArithmeticException`. That’s `not`: what happens:

```scala
scala> 1.0 / 0.0
res0: Double = Infinity
```

So you can’t even catch this error with an exception handler, since no exception is raised:

```scala
scala> val r = inter(0, 0, 0, 0)
r: Point = Point(NaN,NaN)
```
All these mechanisms for signalling errors share similar flaws:

1. **Exceptions**: you have to remember to catch them, or your program will crash. You can’t tell if a function will throw an exception without carefully reading its code, which may not even be possible if it is in a library.

2. **Producing null**: even worse than exceptions, because your program will will not crash on an error. When it does crash, you’ll spend a lot of time trying to figure out what produced the null.

3. **Producing other null-like values**: see above.

The real problem is that the types of all these functions are not useful:

- The type of `Integer.parseInt` is `String => Int`, but it may throw an exception instead of producing an `Int`.
- The type of `ht.get` is `Any => String`, but it may produce a `null`.
- The type of `inter` is `(Double, Double, Double, Double) => Point`, but it can produce `Point(NaN, NaN)`, which is clearly not what we had in mind.

**A Solution**  Let’s use `inter` as an example and modify the function so that its type makes it obvious that it may not always return a `Point`. We introduce the following sealed trait:

```scala
sealed trait OptionalPoint
case class SomePoint(pt: Point) extends OptionalPoint
case class NoPoint() extends OptionalPoint
```

And we modify `inter` to produce `NoPoint` instead of a malformed-Point:

```scala
def inter(m1: Double, b1: Double, m2: Double, b2: Double): OptionalPoint = {
  if (m1 - m2 == 0) {
    NoPoint()
  } else {
    val x = (m1 - m2) / (b2 - b1)
    Point(x, m1 * x + b1)
  }
}
```

With this new type, any program that applies `inter` will be forced to check if if a point was produced:

```scala
inter(10, 3, 10, 3) match {
  case NoPoint => println("no intersection")
  case SomePoint(Point(x,y)) => println(s"intersection at ($x, $y)"

Consider another example: a type that represents an alarm clock. An alarm clock needs to track the current time and the alarm time if the alarm is set:

```scala
case class Time(h: Int, m: Int, s: Int)
case class AlarmClock(time: Time, alarm: Time, alarmOn: Boolean)
```

But, with this representation, it is easy to make simple errors. For example, you may accidentally trigger the alarm when `time == alarm`, if you forget to check `alarmOn` first. A cleaner representation is to use the same pattern we used above:
sealed trait OptionalAlarm
case class NoAlarm() extends OptionalAlarm
case class AlarmSet(time: Time) extends OptionalAlarm

case class AlarmClock(time: Time, alarm: OptionalAlarm)

In both \texttt{inter} and \texttt{AlarmClock}, it is completely obvious from the type that a point is not always produced and that an alarm is not always set. Partial functions are \textit{pervasive} in computing and this pattern will make your programs more robust.

But, it is annoying to define a new type such as \texttt{OptionalPoint} and \texttt{OptionalAlarm} for each type.

\subsection*{2.1 The Option Type}
Scala has a builtin generic type called \texttt{Option} that abtracts the pattern we discussed above. For example, here is \texttt{inter} rewritten to use \texttt{Option}:

\begin{verbatim}
def inter(m1: Double, b1: Double, m2: Double, b2: Double): Option[Point] = {
  if (m1 - m2 == 0) {
    None
  } else {
    val x = (m1 - m2) / (b2 - b1)
    Some(Point(x, m1 * x + b1))
  }
}
\end{verbatim}

\section*{3 Built-in List methods}
Scala's \texttt{List} type has dozens of useful methods. For example, these methods correspond to the higher-order functions we've seen so far:

- We can map over a list:
  \begin{verbatim}
  assert(List(10, 20, 30).map(x => x + 1) == List(11, 21, 31))
  \end{verbatim}

- We can filter a list:
  \begin{verbatim}
  assert(List(1, 2, 3, 4).filter(x => x % 2 == 0) == List(2, 4))
  \end{verbatim}

- We can fold over a list:
  \begin{verbatim}
  assert(List(10, 20, 30).foldRight(0)((x, acc) => x + acc) == 60)
  \end{verbatim}

Notice that the syntax of \texttt{foldRight} is unusual. We'll get into the details how it works later. For now, there is no need to write sums and products using folds. Scala's lists have methods that do these directly:

\begin{verbatim}
assert(List(10, 20, 30).sum == 60)
assert(List(10, 20, 30).product == 6000)
\end{verbatim}

There are several other useful methods. For example:

- \texttt{lst.take(n)} produces a list with first \texttt{n} elements of \texttt{lst}. Similarly, \texttt{lst.drop(n)} produces a list without the first \texttt{n} elements of \texttt{lst}.  

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val lst = List("X", "Y", "Z", "A", "B", "C")
assert(lst.take(3) == List("X", "Y", "Z"))
assert(lst.drop(3) == List("A", "B", "C"))
assert(lst.take(3) ::: lst.drop(3) == lst)

In the last line, the :: operator (pronounced “append”) append two lists.

Notation  We emphasize that :: is an ordinary method, even though it is written
using funny symbols and appears to be an infix operator. We could append lists
using conventional method-application syntax:

assert(lst:::(lst) == lst :::: lst)

In fact, all operators on objects are actually ordinary methods. E.g., we could
write 2.+(3.*(6)), to do arithmetic using conventional method-application syn-
tax. However, the usual notation of 2 + (3 * 6) is typically easier to read.

- `lst.exists(f)` produces `true` if there exists any element in the list on which `f` produces `true`.
  
  assert(List(1, 2, 3, 4).exists(n => n == 2) == true)
  assert(List(1, 2, 3, 4).exists(n => n == 5) == false)

- `lst.forall(f)` checks that all elements in `lst` satisfy `f`:

  assert(List(2, 4, 6, 8).forall(x => x % 2 == 0) == true)
  assert(List(2, 3, 4).forall(x => x % 2 == 0) == false)

There are several other useful functions. You should explore the List API to learn more
about them.

4  Sets and Maps

Sets

The Scala standard library also defines sets and maps, which are two other data structures
that are very common. Note that these represent mathematical sets, so they don’t have
duplicate elements and are not ordered. I.e., the three definitions below are the same:

Set(1, 2, 3)
Set(1, 2, 2, 3)
Set(3, 2, 1)

Sets have methods for calculating set union, set intersection, set difference, testing empti-

ness, and so on:

assert(Set(1, 2, 3).union(Set(2, 3, 4)) == Set(1, 2, 3, 4))
assert(Set(1, 2, 3).intersect(Set(2, 3, 4)) == Set(2, 3))
assert(Set(1, 2).intersect(Set(3, 4)).isEmpty == true)

We can also map and filter the elements of sets, similar to lists:

assert(Set(1, 2, 3, 4).filter(x => x % 2 == 0) == Set(2, 4))
assert(Set(1, 2, 3, 4, 5).map(x => x % 2) = Set(0, 1))

There are severy other useful methods in the Set API.
Maps  The Map data-structure (which is not the same as the map function) is a finite map from keys to values. For example:

```scala
val dueDates = Map(
  1 -> "Jan 28",
  2 -> "Feb 4",
  3 -> "Feb 11")
```

**Notation**  $X \rightarrow Y$ is just another notation for the tuple $(X, Y)$, but is commonly used with maps to suggest that it “maps $X$ to $Y$”. Therefore, we could have written

```scala
val dueDates = Map(
  (1, "Jan 28"),
  (2, "Feb 4"),
  (3, "Feb 11"))
```

We can lookup a key in two ways. First, we can simply apply the map to a key, just like a function:

```scala
assert (dueDates(1) == "Feb 4")
```

However, if the key is not found, this throws an exception. An alternative is to apply the get methods, which produces Some($v$) if the key is mapped to a value and None otherwise:

```scala
dueDates.get(x) match {
  case Some(v) => v
  case None => "Unknown assignment"
}
```

We can augment maps using the following syntax:

```scala
val moreDueDates = dueDates + (4 -> "Feb 18")
```

We emphasize that this produces a new map with all the contents of dueDates and the key mapping for 4. The original map is not modified.

**Notation**  The notation $m + (k \rightarrow v)$ seems to be something new, but we know how to unpack it. We just learned the arrow notation is another way of writing tuples, we can first rewrite it as $m + (k, v)$. We also learned that all operators on objects are actually methods, so can rewrite it again as $m.+(k, v)$.

Therefore, we can conclude that maps have a method called + that takes one argument. This argument is a tuple where the first component is a key $k$ and the second component is the value $v$. The result of applying this method is a new map where $k$ is mapped to $v$.

It is often get the set of keys in a map:

```scala
assert (dueDates.keys == Set(1, 2, 3))
```

Similarly, we can get an iterator over the values. Typically, you’ll want to turn the iterator into a list immediately:

```scala
assert (dueDates.values.toList == List("Jan 28", "Feb 4", "Feb 11"))
```

As usual, there are dozens of handy methods over maps. You should explore the Map API.
5 Conversions

It is sometimes necessary and easy to convert lists, sets, and maps to each other. These objects have methods called `toList`, `toSet`, and `toMap` that do exactly what their names suggest. For example:

```java
assert(Map("X" -> 10, "Y" -> 20).toList == List(("X", 10), ("Y", 20)))
assert(List(("X", 10), ("Y", 20)).toMap == Map("X" -> 10, "Y" -> 20))
```