

Homework 5: Generalized Tic Tac Toe

For this assignment, you will write a program that given an $n \times n$ tic-tac-toe board, determines which player will win, or if the game will be a draw. You're going to make significant use of Scala collections and learn the the *Minimax algorithm*, which is a form of *backtracking search*.

The template for this assignment is [available here](#)¹.

1 Representing a Tic Tac Toe Board

We assume you know how to play Tic Tac Toe. This section talks about the representation of tic-tac-toe boards that you will use. All the types mentioned below are in the file `src/main/scala/Provided.scala` in the template code.

The `sealed trait Player` has two constructors, `O` and `X`, that represent the two players.

A typical 3×3 board can be thought of as a 3×3 matrix, where $(0, 0)$ is the coordinate of the top-left corner and $(2, 2)$ is the coordinate of the bottom-right corner:

$(0, 0)$	$(1, 0)$	$(2, 0)$
$(0, 1)$	$(1, 1)$	$(2, 1)$
$(0, 2)$	$(1, 2)$	$(2, 2)$

The `Solution.createGame` function, which you need to implement, takes as input the player who makes the first move, the value n that specifies the dimensions of the board, and a map from coordinates to `Player`s that indicates where the pieces are.

For example:

- In generalized tic-tac-toe, either play may make the first move. Therefore, given an empty board:

¹<https://www.cs.umass.edu/~arjun/courses/cmptsci220-spring2016/hw/tictactoe.zip>

We can call the function in two ways:

```
Solution.createGame(0, 3, Map())  
Solution.createGame(X, 3, Map())
```

- This board:

X		
		O

Can be represented as:

```
Solution.createGame(X, 3, Map((0, 0) -> X, (2, 2) -> O))
```

Alternatively, we could have O make the next move.

- This board:

X		
X		O

Can be represented as:

```
Solution.createGame(X, 3, Map((0, 0) -> X, (0, 2) -> X, (2, 2) -> O))
```

Alternatively, we could have O make the next move.

- This board, which is 4×4 :

X			
		O	
			X

Can be represented as:

```
Solution.createGame(0, 4, Map((0, 0) -> X, (2, 2) -> O, (3, 3) -> X))
```

Alternatively, we could have X start first too.

2 The Minimax Algorithm

Minimax is an algorithm to determine who will win (or draw) a two-player game, if both players are playing perfectly. To do so, Minimax searches all possible game-states that are reachable from a given initial state. Here is an outline of a recursive implementation of Minimax:

```
def minimax(game: Game): Some[Player] = {  
  /*  
  If it is Xs turn:  
  
  1. If X has won the game, return Some(X).  
  2. If the game is a draw, return None. (If all squares are filled  
     and nobody has won, then the game is a draw. However, you are  
     free to detect a draw earlier, if you wish.)  
  3. Recursively apply minimax to all the successor states of game  
     - If any recursive call produces X, return Some(X)  
     - Or, if any recursive call produces None, return None  
     - Or, return Some(O)  
  
  The case for Os turn is similar.  
  */  
}
```

You can find several other descriptions of Minimax on the Web. But, Minimax is a very straightforward function to write, if you follow the programming directions below and implement (and test) everything leading up to Minimax.

3 Programming Task

Your task is to implement a representation of boards, by implementing the `GameLike` trait, provided in the template code. Your code must be able to implement arbitrary $n \times n$ boards for all $n > 2$. However, your implementation of the Minimax algorithm (the `MinimaxLike` trait) only needs to be fast enough for $n \leq 4$.²

I recommend proceeding in the following way, using `Solution.scala` as a template:

1. Add fields to the `Game` class to represent the state of the game and fill in the body of the `Solution.createGame(turn, dim, board)` function. You may assume that `dim >= 2` and that all the pieces described in `board` are within bounds. However, *The board may be in an arbitrary, even illegal state.* For example, the board may have seven Xs. Similarly, the `turn` could be either X or O.
2. Implement the `Game.isFinished` method. This method should produce `true` when there are three Xs or Os in a row or the game ends in a draw.
3. Implement the `getWinner` method.

`Provided.scala` has a class called `Matrix` that has some useful methods. You may find it easier to use a matrix to represent a board, instead of an arbitrary map or two-dimensional array.

²If you want to do better, lookup *alpha-beta pruning* on the web.

4. Implement the `nextBoards` method, which returns a list of boards that represent all the moves the next player could make.

For example, if the current board looks like this:

X	X	
	O	
X	O	O

And if it is *O*'s turn, then these are the three possible next boards:

X	X	
O	O	
X	O	O

X	X	
	O	O
X	O	O

X	X	O
	O	
X	O	O

As you implement each successive step, you may need to revisit design decisions you made earlier.

4 Hand In

From the `sbt` console, run the command `submit`. The command will create a file called `submission.tar.gz` in your assignment directory. Submit this file using Moodle.

For example, if the command runs successfully, you will see output similar to this:

```
Created submission.tar.gz. Upload this file to Moodle.  
[success] Total time: 0 s, completed Jan 17, 2016 12:55:55 PM
```

Note: The command will not allow you to submit code that does not compile. If your code doesn't compile, you will receive no credit for the assignment.