

# Authenticated Encryption

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Based on <http://cseweb.ucsd.edu/~mihir/cse107/>

# Motivation

In practice we often want **both** privacy and authenticity.

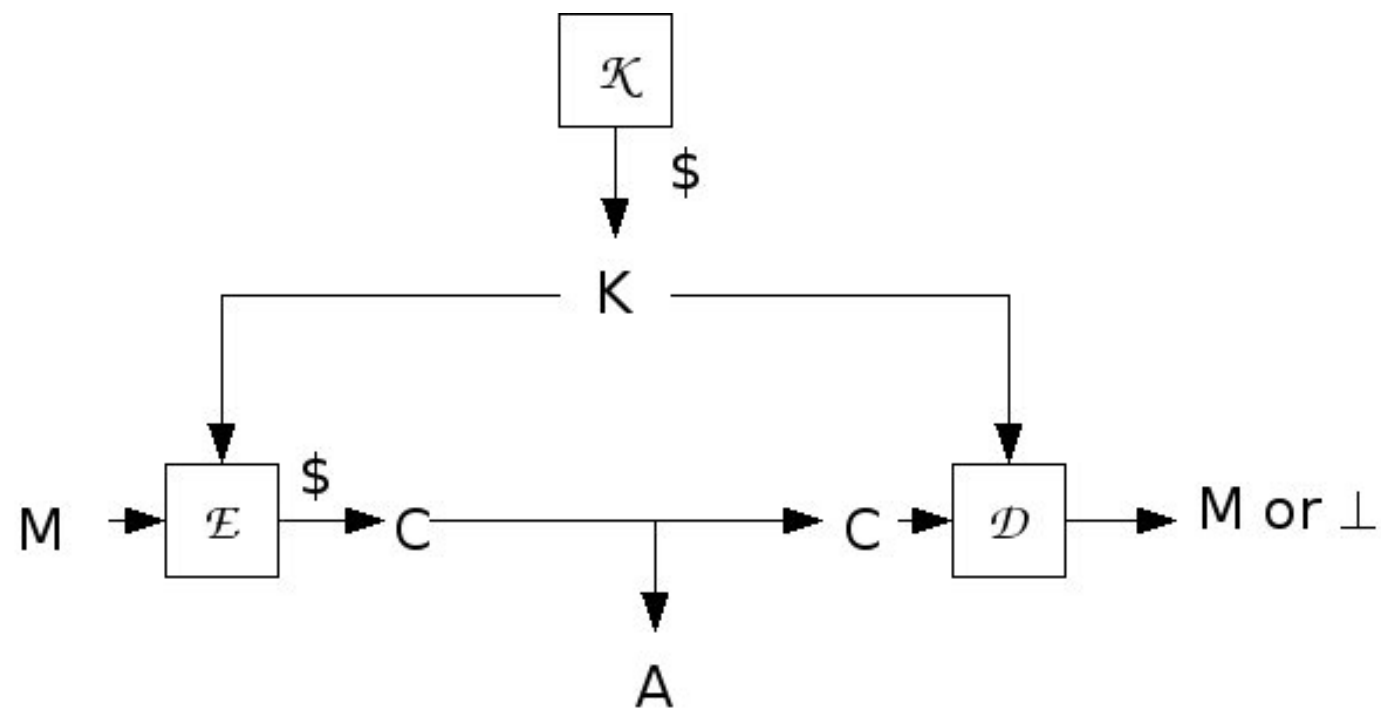
**Example:** A doctor wishes to send medical information  $M$  about Alice to the medical database. Then

- We want **data privacy** to ensure Alice's medical records remain **confidential**.
- We want **authenticity** to ensure the person sending the information is really the doctor and the information was **not modified** in transit.

We refer to this as **authenticated encryption**.

# Syntax

Syntactically, an authenticated encryption scheme is just a symmetric encryption scheme  $\mathcal{AE} = (\mathcal{K}, \mathcal{E}, \mathcal{D})$  where



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- For **authenticity**, the adversary's goal is to get the receiver to accept a “non-authentic” ciphertext (i.e., not actually transmitted by the sender)

# INT-CTXT

Let  $\mathcal{AE} = (\mathcal{K}, \mathcal{E}, \mathcal{D})$  be a symmetric encryption scheme and  $A$  an adversary.

Game  $\text{INTCTXT}_{\mathcal{AE}}$

**procedure Initialize**

$K \xleftarrow{\$} \mathcal{K} ; S \leftarrow \emptyset$

**procedure Enc( $M$ )**

$C \xleftarrow{\$} \mathcal{E}_K(M)$

$S \leftarrow S \cup \{C\}$

Return  $C$

**procedure Finalize( $C$ )**

$M \leftarrow \mathcal{D}_K(C)$

if  $(C \notin S \wedge M \neq \perp)$  then

    return true

Else return false

The int-ctxt advantage of  $A$  is

$$\mathbf{Adv}_{\mathcal{AE}}^{\text{int-ctxt}}(A) = \Pr[\text{INTCTXT}_{\mathcal{AE}}^A \Rightarrow \text{true}]$$

# Integrity + Privacy

The goal of authenticated encryption is to provide both integrity and privacy. We will be interested in IND-CPA + INT-CTXT.

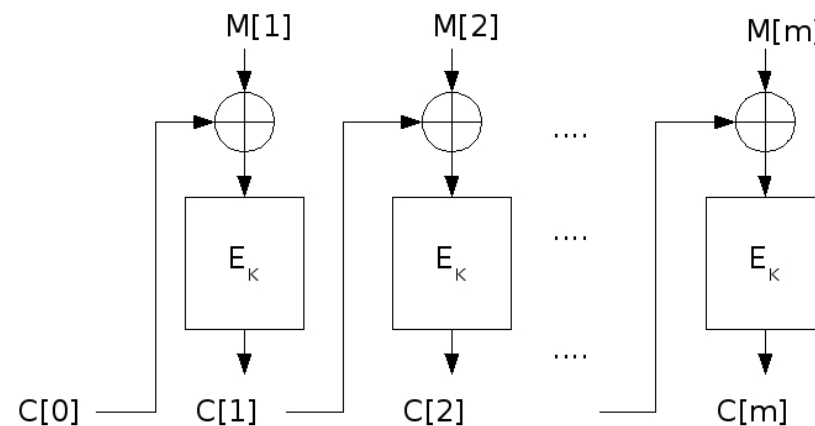
# Plain Encryption: CBC\$

## Alg $\mathcal{E}_K(M)$

$C[0] \xleftarrow{\$} \{0, 1\}^n$   
For  $i = 1, \dots, m$  do  
     $C[i] \leftarrow E_K(C[i-1] \oplus M[i])$   
Return  $C$

## Alg $\mathcal{D}_K(C)$

For  $i = 1, \dots, m$  do  
     $M[i] \leftarrow E_K^{-1}(C[i]) \oplus C[i-1]$   
Return  $M$



**Question:** Is CBC\$ encryption INT-CTXT secure?



# Plain Encryption Does Not Provide Integrity

Alg  $\mathcal{E}_K(M)$

$C[0] \xleftarrow{\$} \{0, 1\}^n$   
For  $i = 1, \dots, m$  do  
     $C[i] \leftarrow E_K(C[i-1] \oplus M[i])$   
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Alg  $\mathcal{D}_K(C)$

For  $i = 1, \dots, m$  do  
     $M[i] \leftarrow E_K^{-1}(C[i]) \oplus C[i-1]$   
Return  $M$

adversary  $A$

$C[0]C[1]C[2] \xleftarrow{\$} \{0, 1\}^{3n}$   
Return  $C[0]C[1]C[2]$

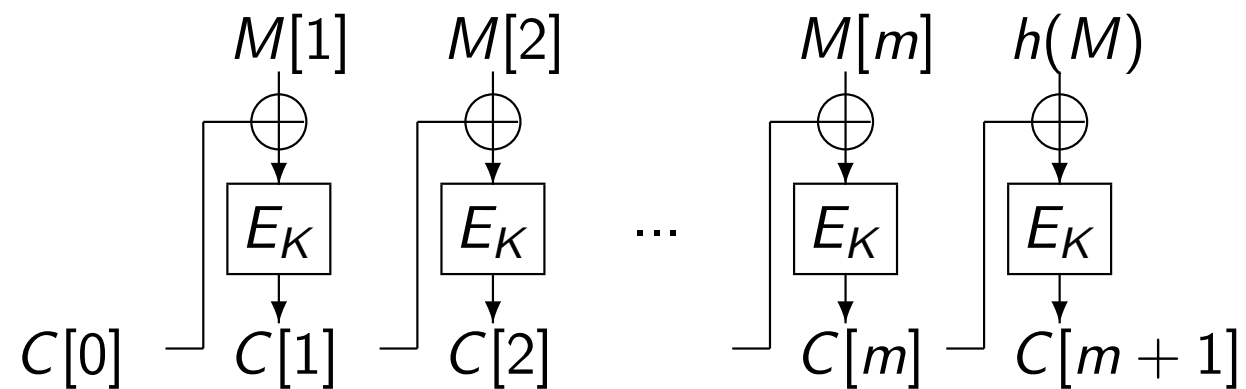
Then

$$\mathbf{Adv}_{\mathcal{SE}}^{\text{int-ctxt}}(A) = 1$$

This violates INT-CTXT.

A scheme whose decryption algorithm **never** outputs  $\perp$  **cannot** provide **integrity!**

# Encryption with Redundancy

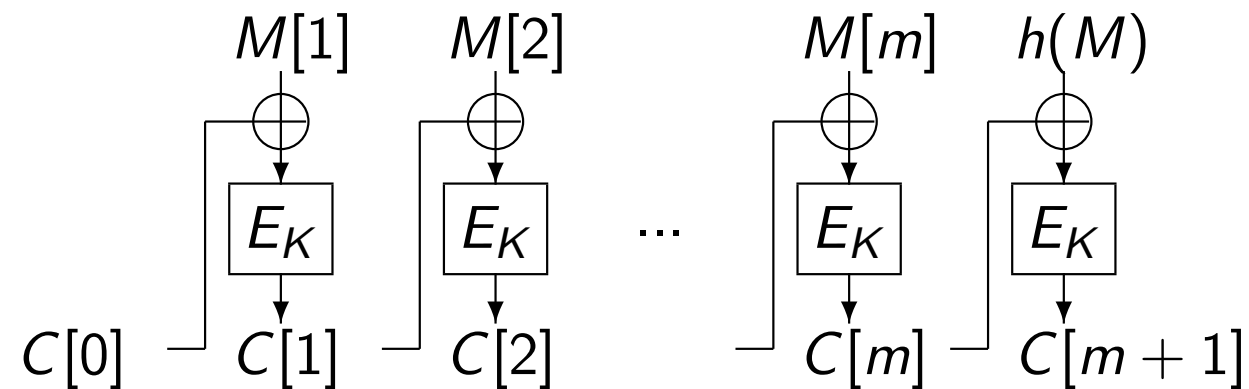


Here  $E: \{0, 1\}^k \times \{0, 1\}^n \rightarrow \{0, 1\}^n$  is our block cipher and  $h: \{0, 1\}^* \rightarrow \{0, 1\}^n$  is a “redundancy” function, for example

- $h(M[1] \dots M[m]) = 0^n$
- $h(M[1] \dots M[m]) = M[1] \oplus \dots \oplus M[m]$
- A CRC
- $h(M[1] \dots M[m])$  is the first  $n$  bits of  $\text{SHA1}(M[1] \dots M[m])$ .

The redundancy is verified upon decryption.

# Encryption with Redundancy



Let  $E: \{0, 1\}^k \times \{0, 1\}^n \rightarrow \{0, 1\}^n$  be our block cipher and  $h: \{0, 1\}^* \rightarrow \{0, 1\}^n$  a redundancy function. Let  $\mathcal{SE} = (\mathcal{K}, \mathcal{E}', \mathcal{D}')$  be CBC\$ encryption and define the encryption with redundancy scheme  $\mathcal{AE} = (\mathcal{K}, \mathcal{E}, \mathcal{D})$  via

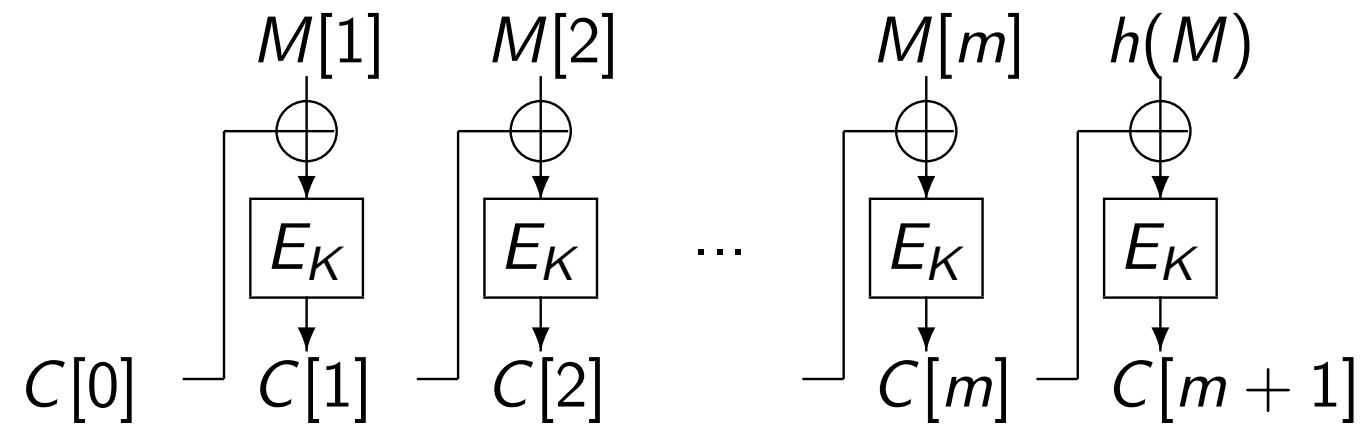
## Alg $\mathcal{E}_K(M)$

$M[1] \dots M[m] \leftarrow M$   
 $M[m+1] \leftarrow h(M)$   
 $C \xleftarrow{\$} \mathcal{E}'_K(M[1] \dots M[m]M[m+1])$   
 return  $C$

## Alg $\mathcal{D}_K(C)$

$M[1] \dots M[m]M[m+1] \leftarrow \mathcal{D}'_K(C)$   
 if  $(M[m+1] = h(M))$  then  
     return  $M[1] \dots M[m]$   
 else return  $\perp$

# Does it Work?



The adversary will have a hard time producing the last enciphered block of a new message.

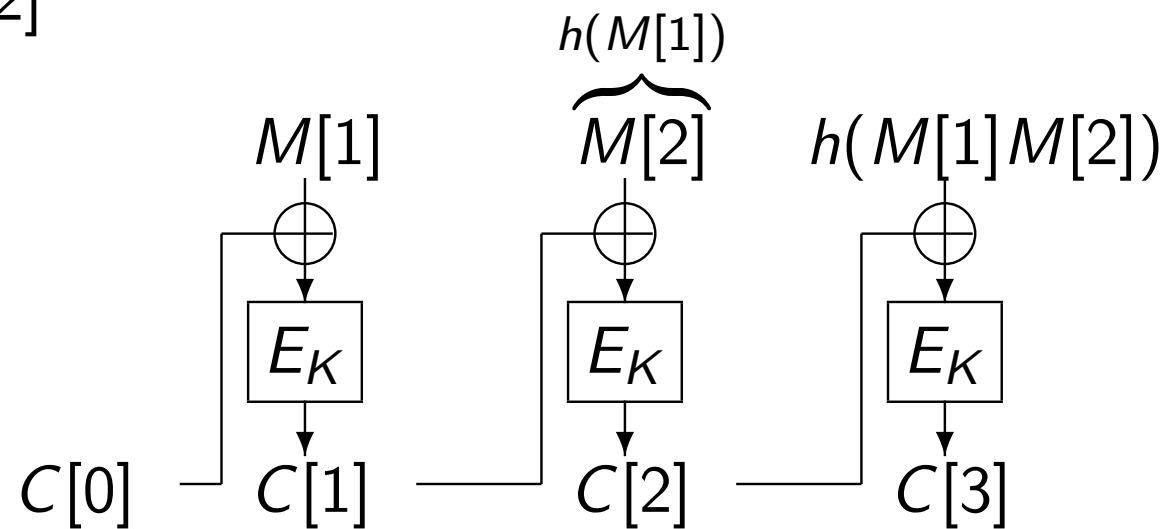
# Attacks

## adversary A

$M[1] \xleftarrow{\$} \{0, 1\}^n ; M[2] \leftarrow h(M[1])$

$C[0]C[1]C[2]C[3] \xleftarrow{\$} \mathbf{Enc}(M[1]M[2])$

Return  $C[0]C[1]C[2]$



This attack succeeds for any (not secret-key dependent) redundancy function  $h$ .

# WEP Attack

A “real-life” rendition of this attack broke the 802.11 WEP protocol, which instantiated  $h$  as CRC and used a stream cipher for encryption [BGW].

What makes the attack easy to see is having a clear, strong and formal security model.

# Generic Composition

Build an authenticated encryption scheme  $\mathcal{AE} = (\mathcal{K}, \mathcal{E}, \mathcal{D})$  by combining

- a given IND-CPA symmetric encryption scheme  $\mathcal{SE} = (\mathcal{K}', \mathcal{E}', \mathcal{D}')$
- a given PRF  $F : \{0, 1\}^k \times \{0, 1\}^* \rightarrow \{0, 1\}^n$

	CBC\$-AES	CTR\$-AES	...
HMAC-SHA1			
CMAC			
ECBC			
⋮			

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- a given IND-CPA symmetric encryption scheme  $\mathcal{SE} = (\mathcal{K}', \mathcal{E}', \mathcal{D}')$
- a given PRF  $F : \{0, 1\}^k \times \{0, 1\}^* \rightarrow \{0, 1\}^n$

A key  $K = K_e || K_m$  for  $\mathcal{AE}$  always consists of a key  $K_e$  for  $\mathcal{SE}$  and a key  $K_m$  for  $F$ :

**Alg  $\mathcal{K}$**

$K_e \xleftarrow{\$} \mathcal{K}'; K_m \xleftarrow{\$} \{0, 1\}^k$

Return  $K_e || K_m$



# Generic Composition

The [order](#) in which the primitives are applied is important. Can consider

Method	Usage
Encrypt-and-MAC (E&M)	SSH
MAC-then-encrypt (MtE)	SSL/TLS
Encrypt-then-MAC (EtM)	IPSec

# Encrypt-and-MAC

$\mathcal{AE} = (\mathcal{K}, \mathcal{E}, \mathcal{D})$  is defined by

**Alg**  $\mathcal{E}_{K_e||K_m}(M)$

$C' \xleftarrow{\$} \mathcal{E}'_{K_e}(M)$

$T \leftarrow F_{K_m}(M)$

Return  $C' || T$

**Alg**  $\mathcal{D}_{K_e||K_m}(C' || T)$

$M \leftarrow \mathcal{D}'_{K_e}(C')$

If  $(T = F_{K_m}(M))$  then return  $M$

Else return  $\perp$

Security	Achieved?
IND-CPA	
INT-CTXT	

# MAC-then-Encrypt

$\mathcal{AE} = (\mathcal{K}, \mathcal{E}, \mathcal{D})$  is defined by

**Alg**  $\mathcal{E}_{K_e||K_m}(M)$

$T \leftarrow F_{K_m}(M)$

$C \xleftarrow{\$} \mathcal{E}'_{K_e}(M||T)$

Return  $C$

**Alg**  $\mathcal{D}_{K_e||K_m}(C)$

$M||T \leftarrow \mathcal{D}'_{K_e}(C)$

If  $(T = F_{K_m}(M))$  then return  $M$

Else return  $\perp$

Security	Achieved?
IND-CPA	
INT-CTXT	

# Encrypt-then-MAC

$\mathcal{AE} = (\mathcal{K}, \mathcal{E}, \mathcal{D})$  is defined by

**Alg**  $\mathcal{E}_{K_e||K_m}(M)$

$C' \xleftarrow{\$} \mathcal{E}'_{K_e}(M)$

$T \leftarrow F_{K_m}(C')$

Return  $C' || T$

**Alg**  $\mathcal{D}_{K_e||K_m}(C' || T)$

$M \leftarrow \mathcal{D}'_{K_e}(C')$

If  $(T = F_{K_m}(C'))$  then return  $M$

Else return  $\perp$

Security	Achieved?
IND-CPA	
INT-CTXT	

# Two keys?

We have used separate keys  $K_e, K_m$  for the encryption and message authentication. However, these can be derived from a single key  $K$  via  $K_e = F_K(0)$  and  $K_m = F_K(1)$ , where  $F$  is a PRF such as a block cipher, the CBC-MAC or HMAC.

Trying to directly use the same key for the encryption and message authentication is error-prone, but works if done correctly.

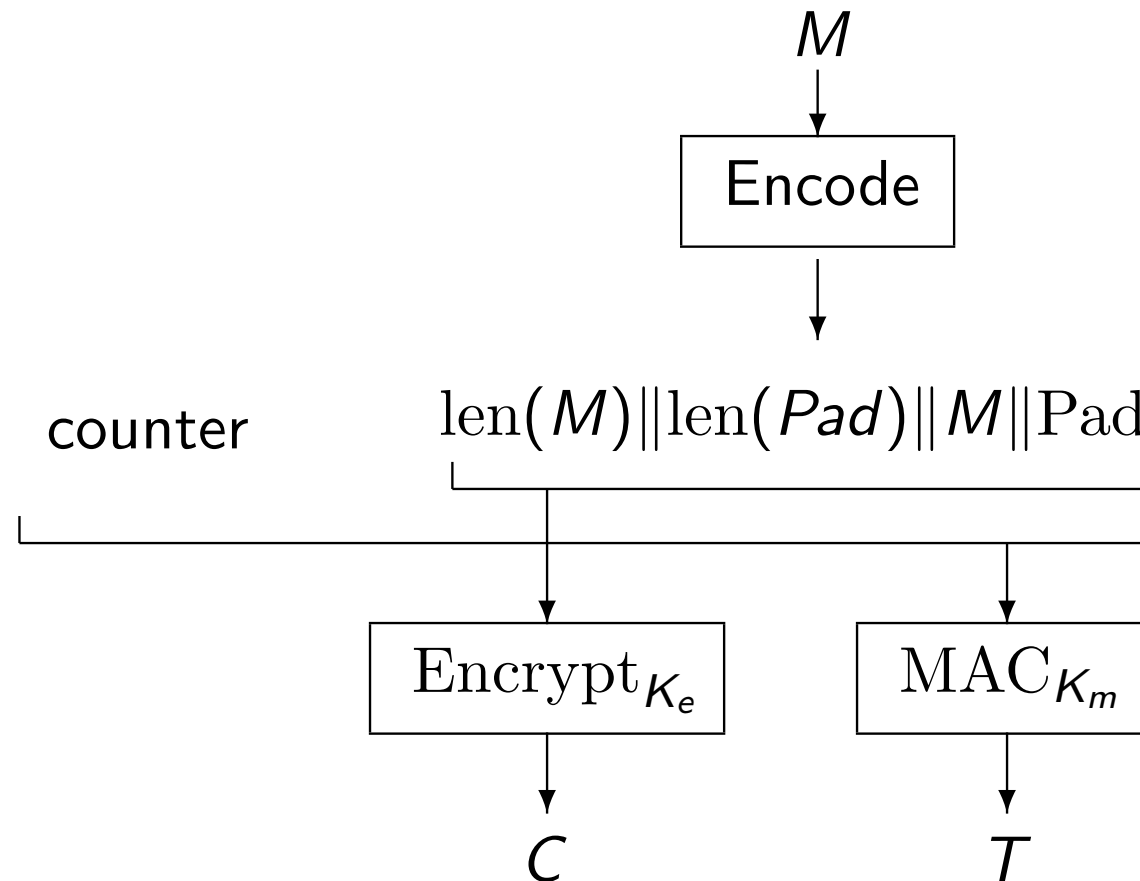
# Generic Composition in Practice

AE in	is based on	which in general is	and in this case is
SSH	E&M	insecure	secure
SSL	MtE	insecure	insecure
SSL + RFC 4344	MtE	insecure	secure
IPSec	EtM	secure	secure
WinZip	EtM	secure	insecure

Why?

- Encodings
- Specific “E” and “M” schemes
- For WinZip, disparity between usage and security model

# AE in SSH



SSH2 encryption uses inter-packet chaining which is insecure [D, BKN]. RFC 4344 [BKN] proposed fixes that render SSH provably IND-CPA + INT-CTXT secure. Fixes recommended by Secure Shell Working Group and included in OpenSSH since 2003. Fixes included in PuTTY since 2008.