

# Supplementary Material: Modeling Addiction in terms of fluctuating neurotransmitters within the reward system

## 1. General

The bounding function  $\sigma(x)$  is defined as follow:

$$\sigma(x) = \begin{cases} 0 + |\epsilon| & \text{if } x < 0 \\ x & \text{if } x \in [0, 1] \\ 1 - |\epsilon| & \text{if } x > 1 \end{cases}$$

where  $\epsilon$  is a random value,  $\epsilon \in [-0.05, 0.05]$ .

**Notations** Unless otherwise specified, the following holds for the entire document:

$d$  is a time steps counter used by the continuous processes, which resets to 1 at every time  $t$  where the value  $G(t)$  changes from a state  $G(t) = 0, < 0, \text{ or } > 0$  to another state

$t_G$  is the time when  $G(t)$  last changed state

$\epsilon_X$  is a random value applied to process  $X$ ,  $\epsilon_X \in [-0.05, 0.05]$

$\tau_G$  is a binary variable, defined as:

$\tau_G = 0$  if maladaptive behavior where never expressed

$\tau_G = 1$  if maladaptive behavior where already expressed at least once

$\omega_X$  is the weight of the process  $X$ ,  $\omega_X \in [0, 1]$

$M_X$  is the upper bound asymptote of the process  $X$ ,  $M_X \in ]\mu_X, 1] \subseteq ]0, 1]$

$\mu_X$  is the lower bound asymptote of the process  $X$ ,  $\mu_X \in [0, M_X[ \subseteq [0, 1[$

$\Pi_X$  is a temporal constant which influences the behavior of the process  $X$ ,  $\in \mathbb{N}^+$

$\beta$ ,  $\gamma$  and  $\gamma_n$  are constants  $\in \mathbb{R}^+$

$P_X(t)$  is the uniformly distributed random function of process  $X$ ,  $P_X(t) \in [0, 1]$

$\theta_X$  is the constant probability that the discrete process  $X$  occurs at time  $t$ ,  $\theta_X \in [0, 1]$

$d_\Delta$  is a time steps counter used by the discrete processes, which resets to 1 when a discrete process is triggered (each discrete process has a distinct counter of this type)

$\delta_X$  is a constant for the discrete process  $X$ ,  $\in \mathbb{N}^+$

$\rho_X$  is a constant for the discrete process,  $\rho_X \in [0, 1]$

$\Delta_i$  and  $\Delta_d$  are the constant magnitudes of the discrete process's memories increases and decreases,  $\{\Delta_i, \Delta_d\} \in \mathbb{N}^+$  (different for each process)

**Table 1:** Behaviors of the continuous processes with respect to  $G(t)$  and  $d$ , when  $\tau_G = 1$ . The sign  $\rightarrow$  stands for constant, and the signs  $\nearrow$  and  $\searrow$  stand for exponentially increasing and decreasing.

	$G(t-1) = 0$	$G(t-1) < 0$	$G(t-1) > 0$	
	$\forall d$	$\forall d$	$d \leq \Pi_X$	$d > \Pi_X$
$DA_b(t)$	$\rightarrow$	$\nearrow$	$\searrow$	
$GL_{PFC,b}(t)$	$\rightarrow$	$\searrow$	$\searrow$	$\nearrow$
$DA_p(t)$	$\rightarrow$	$\searrow$	$\searrow$	$\nearrow$
$GL_{PFC,p}(t)$	$\rightarrow$	$\searrow$	$\searrow$	$\nearrow$
$GL_{PFC,c}(t)$	$\rightarrow$	$\searrow$	$\searrow$	$\nearrow$
$GL_{Amg,c}(t)$	$\rightarrow$	$\searrow$	$\searrow$	$\nearrow$
$GL_{HPC,c}(t)$	$\rightarrow$	$\searrow$	$\searrow$	$\nearrow$
$DA_c(t)$		$\rightarrow$	$\searrow$	$\nearrow$
$GL_{PFC,ic}(t)$	$\rightarrow$	$\searrow$		$\nearrow$

**About the continuous processes** In Table 1 are summarized the continuous processes with respect to  $G(t)$  and the counter  $d$ , when  $\tau_G = 1$ .

The tendency of drug-seeking behavior  $G(t)$  is the output of the model, the variable  $\tau_G$  describe whether the virtual subject already expressed maladaptive behavior, and the counter  $d$  is reset to 1 at every time  $t$  where the value  $G(t)$  changes state, from  $G(t) = 0$ ,  $G(t) < 0$ , or  $G(t) > 0$  to another state.

When  $\tau_G = 0$  these processes stay constant over time ( $\rightarrow$ ).

**About the discrete processes** The following list describe when these processes can be triggered:

- $\Lambda_{DP}$  can be triggered at time  $t$  if  $\tau_G = 1$ ,  $G(t-1) \geq 0$ , and  $P_{DP} \leq \theta_{DP}$   
This process influences  $DA_p(t)$  and  $GL_{PFC,p}(t)$
- $\Lambda_{DC}$  can be triggered at time  $t$  if  $\tau_G = 1$ , and  $P_{DC} \leq \theta_{DC}$   
This process influences  $GL_{PFC,c}(t)$ ,  $GL_{Amg,c}(t)$ ,  $GL_{HPC,c}(t)$ , and  $DA_c(t)$
- $\Lambda_S$  can be triggered at time  $t$  if  $\tau_G = 1$ ,  $G(t-1) \geq 0$ , and  $P_S \leq \theta_S$   
This process influences  $DA_p(t)$  and  $GL_{PFC,p}(t)$
- $\Lambda_R$  can be triggered at time  $t$  if  $\tau_G = 1$ ,  $G(t-1) \leq 0$ , and  $P_R \leq \theta_R$   
This process influences  $GL_{PFC,ic}(t)$

## 2. Continuous processes

### 2.1 DA<sub>b</sub> - Basal Extracellular DA from the VTA

$$DA_b(t) \equiv X(t) = \begin{cases} \sigma[X(t-1) + \epsilon_X] & \text{if } \tau_G=0 \\ & \text{or } \tau_G=1 \text{ and } G(t-1)=0 \\ \sigma[[X(t_G) - \mu_X] \cdot e^{-\gamma_n \cdot d} + \mu_X + \epsilon_X] & \text{if } \tau_G=1 \text{ and } G(t-1) < 0 \\ \sigma[X(t_G) \cdot e^{\beta \cdot d} + \epsilon_X] & \text{if } \tau_G=1 \text{ and } G(t-1) > 0 \end{cases}$$

### 2.2 GL<sub>PFC,b</sub> - Basal Extracellular Glutamate from the PFC

$$GL_{PFC,b}(t) \equiv X(t) = \begin{cases} \sigma[X(t-1) + \epsilon_X] & \text{if } \tau_G=0 \\ & \text{or } \tau_G=1 \text{ and } G(t-1)=0 \\ \sigma[[X(t_G) - \mu_X] \cdot e^{-\gamma_n \cdot d} + \mu_X + \epsilon_X] & \text{if } \tau_G=1 \text{ and} \\ & \text{with } \gamma_n = \gamma_1 \quad G(t-1) < 0 \\ & \text{with } \gamma_n = \gamma_2 \quad G(t-1) > 0 \text{ and } d \leq \Pi_X \\ \sigma[X(t_G) \cdot e^{\beta \cdot d} + \epsilon_X] & \text{if } \tau_G=1 \\ & \text{and } G(t-1) > 0 \text{ and } d > \Pi_X \end{cases}$$

### 2.3 DA<sub>p</sub> - Drug-Induced DA from the VTA

$$DA_p(t) \equiv X(t) = \begin{cases} \sigma[X(t-1) + \epsilon_X] & \text{if } \tau_G=0 \\ & \text{or } \tau_G=1 \text{ and } G(t-1)=0 \\ \sigma[M_X - [M_X - X(t_G)] \cdot e^{-\gamma_n \cdot d} + \epsilon_X] & \text{if } \tau_G=1 \text{ and} \\ & \text{with } \gamma_n = \gamma_1 \quad G(t-1) < 0 \\ & \text{with } \gamma_n = \gamma_2 \quad G(t-1) > 0 \text{ and } d \leq \Pi_X \\ \sigma[M_X - [M_X - X(t_G + \Pi_X)] \cdot e^{\beta \cdot d} + \epsilon_X] & \text{if } \tau_G=1 \\ & \text{and } G(t-1) > 0 \text{ and } d > \Pi_X \end{cases}$$

## 2.4 $GL_{PFC,p}$ - Drug-Induced Glutamate from the PFC

$$GL_{PFC,p}(t) \equiv X(t) = \begin{cases} \sigma[X(t-1) + \epsilon_X] & \text{if } \tau_G=0 \\ & \text{or } \tau_G=1 \text{ and } G(t-1)=0 \\ \\ \sigma[M_X - [M_X - X(t_G)] \cdot e^{-\gamma_n d} + \epsilon_X] & \text{if } \tau_G=1 \text{ and} \\ \quad \text{with } \gamma_n = \gamma_1 & \quad G(t-1) < 0 \\ \quad \text{with } \gamma_n = \gamma_2 & \quad G(t-1) > 0 \text{ and } d \leq \Pi_X \\ \\ \sigma[M_X - [M_X - X(t_G + \Pi_X)] \cdot e^{\beta d} + \epsilon_X] & \text{if } \tau_G=1 \\ & \text{and } G(t-1) > 0 \text{ and } d > \Pi_X \end{cases}$$

## 2.5 $GL_{N,c}$ - Saliency of Drug-Associated Cues (Glutamate)

$$GL_{N,c} = \{GL_{PFC,c}, GL_{Amg,c}, GL_{HPC,c}\}$$

$$GL_{N,c}(t) \equiv X(t) = \begin{cases} \sigma[X(t-1) + \epsilon_X] & \text{if } \tau_G=0 \\ & \text{or } \tau_G=1 \text{ and } G(t-1)=0 \\ \\ \sigma[M_X - [M_X - X(t_G)] \cdot e^{-\gamma_n d} + \epsilon_X] & \text{if } \tau_G=1 \text{ and} \\ \quad \text{with } \gamma_n = \gamma_1 & \quad G(t-1) < 0 \\ \quad \text{with } \gamma_n = \gamma_2 & \quad G(t-1) > 0 \text{ and } d \leq \Pi_X \\ \\ \sigma[M_X - [M_X - X(t_G + \Pi_X)] \cdot e^{\beta d} + \epsilon_X] & \text{if } \tau_G=1 \\ & \text{and } G(t-1) > 0 \text{ and } d > \Pi_X \end{cases}$$

## 2.6 DA<sub>c</sub> - Saliency of Drug-Associated Cues (Dopamine)

$$DA_c(t) \equiv X(t) = \begin{cases} \sigma[X(t-1) + \epsilon_X] & \text{if } \tau_G=0 \\ & \text{or } \tau_G=1 \text{ and } G(t-1) \leq 0 \\ \sigma[M_X - [M_X - X(t_G)] \cdot e^{-\gamma d} + \epsilon_X] & \text{if } \tau_G=1 \\ & \text{and } G(t-1) > 0 \text{ and } d \leq \Pi_X \\ \cdot \sigma[M_X - [M_X - X(t_G + \Pi_X)] \cdot e^{\beta d} + \epsilon_X] & \text{if } \tau_G=1 \\ & \text{and } G(t-1) > 0 \text{ and } d > \Pi_X \end{cases}$$

## 2.7 GL<sub>PFC,ic</sub> - Harmful Consequences of Drug Consumption

$$GL_{PFC,ic}(t) \equiv X(t) = \begin{cases} \sigma[X(t-1) + \epsilon_X] & \text{if } \tau_G=0 \\ & \text{or } \tau_G=1 \text{ and } G(t-1)=0 \\ \sigma[M_X - [M_X - X(t_G)] \cdot e^{-\gamma d} + \epsilon_X] & \text{if } \tau_G=1 \text{ and } G(t-1) < 0 \\ \sigma[M_X - [M_X - X(t_G)] \cdot e^{\beta d} + \epsilon_X] & \text{if } \tau_G=1 \text{ and } G(t-1) > 0 \end{cases}$$

### 3. Discrete processes

#### 3.1 $\Lambda_X$ - General definition

$$\Lambda_X(t) = \begin{cases} 1 & \text{if } (*) \text{ or } d_\Lambda \geq 1, \delta_X \geq 1 \\ \max(0, \rho_X \cdot \Lambda_X(t-1)) & \text{if } d_\Lambda \geq \delta_X, \pi_X(t) \geq \delta_X \\ 0 & \text{otherwise} \end{cases}$$

where

$$\pi_X(t) = \begin{cases} \pi_X(t-1) + \Delta_i & \text{if } (*) \\ \max(0, \pi_X(t-1) - \Delta_d) & \text{otherwise} \end{cases}$$

where (\*) is the activation condition of the discrete process, as described below.

##### 3.1.1 $A_{DP}$ - Drug Priming

(\*) stands for:  $\tau_G = 1$  and  $G(t-1) \geq 0$  and  $P_{DP}(t) \leq \theta_{DP}$

##### 3.1.2 $A_{DC}$ - Drug-associated Cues

(\*) stands for:  $\tau_G = 1$  and  $P_{DC}(t) \leq \theta_{DC}$

##### 3.1.3 $A_S$ - Stress

(\*) stands for:  $\tau_G = 1$  and  $G(t-1) \geq 0$  and  $P_S(t) \leq \theta_S$

##### 3.1.4 $A_R$ - Recovery

(\*) stands for:  $\tau_G = 1$  and  $G(t-1) \leq 0$  and  $P_R(t) \leq \theta_R$

## 4. Processes integration and output of the model

### 4.1 n - Input to the behavioral process

$$n(t) = \begin{cases} DA_b^\omega(t) + GL_{PFC,b}^\omega(t) - \widetilde{DA}_p(t) - & \text{if } \text{mod}(t-1,24)=0 \\ \widetilde{GL}_{PFC,p}(t) - \widetilde{GL}_{PFC,c}(t) - \widetilde{GL}_{Amg,c}(t) - & \text{or } \Lambda_{DP}(t) \neq 0 \text{ or } \Lambda_{DC}(t) \neq 0 \\ \widetilde{GL}_{HPC,c}(t) - \widetilde{DA}_c(t) + \widetilde{GL}_{PFC,ic}(t) & \text{or } \Lambda_S(t) \neq 0 \text{ or } \Lambda_R(t) \neq 0 \\ n(t-1) & \text{otherwise} \end{cases}$$

where

$$DA_b^\omega(t) = \omega_X \cdot DA_b(t)$$

$$GL_{PFC,b}^\omega(t) = \omega_X \cdot GL_{PFC,b}(t)$$

$$\widetilde{DA}_p(t) = \omega_X \cdot DA_p(t) + \omega_{DP1} \cdot \Lambda_{DP}(t) + \omega_{S1} \cdot \Lambda_S(t)$$

$$\widetilde{GL}_{PFC,p}(t) = GL_{PFC,p}(t) + \omega_{DP2} \cdot \Lambda_{DP}(t) + \omega_{S2} \cdot \Lambda_S(t)$$

$$\widetilde{GL}_{N,c}(t) = GL_{N,c}(t) + \omega_{DCn} \cdot \Lambda_{DC}(t)$$

$$\widetilde{DA}_c(t) = DA_c(t) + \omega_{DC4} \cdot \Lambda_{DC}(t)$$

$$\widetilde{GL}_{PFC,ic}(t) = GL_{PFC,ic}(t) + \omega_R \cdot \Lambda_R(t)$$

with  $\omega_{DCn} = \{\omega_{DC1}, \omega_{DC2}, \omega_{DC3}\}$  for respectively  $GL_{PFC,c}$ ,  $GL_{Amg,c}$ , and  $GL_{HPC,c}$ .  
and

At the last active step of the acute processes  $\Lambda_{DP}$  and  $\Lambda_S$  (means at  $d_\Lambda = \pi_X(t)$ , with  $X = \{DP, S\}$ ) the value of  $DA_p(t)$  is updated.

#### 4.2 [output] G - Tendency of drug-seeking behavior

$$G(t) = \begin{cases} \tanh(\alpha \cdot G(t-1) + \beta \cdot n(t) - \gamma) & \text{if } \text{mod}(t-1, 24) = 0 \text{ or } \Lambda_{\text{DP}}(t) \neq 0 \\ & \text{or } \Lambda_{\text{DC}}(t) \neq 0 \text{ or } \Lambda_{\text{S}}(t) \neq 0 \text{ or } \Lambda_{\text{R}}(t) \neq 0 \\ G(t-1) & \text{otherwise} \end{cases}$$

where

$\alpha, \beta \in [0, 1]$   
 $\gamma$  is a constant:

$$\gamma = \frac{1}{2}\alpha - \frac{11}{2}\beta$$

$G(t) \in [-1, 1]$