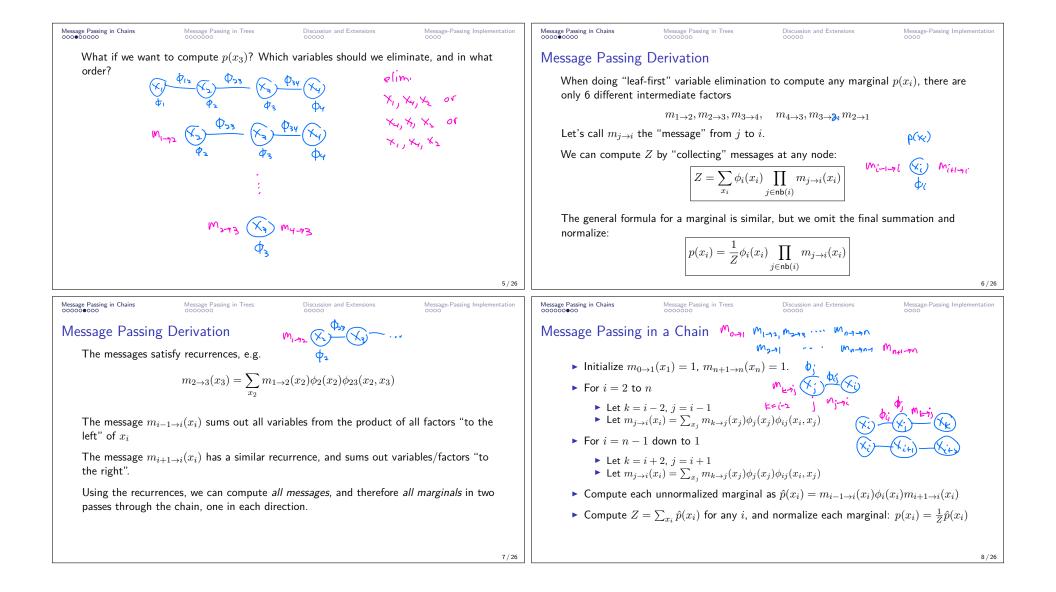
Message Passing in Chains 00000000	Message Passing in Trees 0000000	Discussion and Extensions 00000	Message-Passing Implementation 0000	Message Passing in Chains •0000000	Message Passing in Trees 0000000	Discussion and Extensions 00000	Message-Passing Implementation 0000	
CC	OMPSCI 688: Proba Lecture 9: N	ibilistic Graphical M ^{Aessage Passing}	odels					
	Dan	Sheldon		Message Passing in Chains				
		nation and Computer Sciences assachusetts Amherst						
Partially bas	ed on materials by Benjamin M. Marlin (ma	rlin@cs.umass.edu) and Justin Domke (dom	ke@cs.umass.edu)					
			1/26				2 / 26	
Message Passing in Chains ○●○○○○○○	Message Passing in Trees 0000000	Discussion and Extensions	Message-Passing Implementation	Message Passing in Chains	Message Passing in Trees	Discussion and Extensions 00000	Message-Passing Implementation	
Message Passing	g Derivation							
	our chain example. Supp we eliminate, and in what		$p(x_4)$? Which					
(x) ¢	$\frac{\varphi_{12}}{\varphi_2} \underbrace{(x_2)}_{\varphi_2} \underbrace{(x_3)}_{\varphi_2} (x$	elin	ninate , Xo, Xo					
in _t	$\begin{array}{c} & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & \\ & & & \\ & & & & \\ & & & \\ & & & \\ & & & & \\ & & &$	$\frac{p_{3Y}}{\phi_{Y}} \begin{pmatrix} k_{y} \\ k_{y} \end{pmatrix} \\ \phi_{Y}$	د (د ر					
	Ma+3 (X3) \$\$	$\frac{\Phi_{34}}{\Phi_{4}} \begin{pmatrix} \ddots \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\$						
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Message Passing in Chains	Message Passing in Trees 0000000	Discussion and Extensions 00000	Message-Passing Implementation	Message Passing in Chains 00000000●	Message Passing in Trees	Discussion and Extensions	Message-Passing Implementation		
Pairwise Margin	als			Discussion: Message Passing vs. Variable Elimination					
 Correct form 	nula for a pairwise margi	nal $p(x_i, x_{i+1})$?							
	mula for a pairwise margin \mathfrak{M}_{1-1}	>) M _{4->3}		 Variable elimination can compute marginals and Z exponentially faster than direct summation for nice enough graphs (e.g. chains, trees) 					
				 Naively, to compute all single-node marginals you would have to run variable elimination n times, once per node (but this would repeat work) 					
p(xi,xi	$(+) = \frac{1}{2} m_{i-1} (x_i)$	$\phi_i(x_i) \Phi_{i,i+i}(x_i,x_{i+i}) \Phi_{i}$	$m_{i+s \rightarrow in}(x_{i+s})$ $m_{i+s \rightarrow in}(x_{i+s})$	Message passing can compute all the marginals for the same cost as running variable elimination twice, so is a factor of ≈ n/2 faster than naive variable elimination					
				 (Message passing is nice, but you could say variable elimination did the heavy lifting.) 					
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Message Passing in Chains 000000000	Message Passing in Trees •000000	Discussion and Extensions	Message-Passing Implementation	Message Passing in Chains	Message Passing in Trees 000000	Discussion and Extensions	Message-Passing Implementation		
				Message Passing	g in Trees				
	Message Pa	assing in Trees		A more general version of message passing works for any <i>tree-structured MRF</i> , that is, an MRF of the following form where $G = (V, E)$ is a tree:					
					_				
						$(x_i) \prod_{(i,j)\in E} \phi_{ij}(x_i, x_j).$			
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				Ĭ,					
				(4)					
			11 / 26				12 / 26		

