

## Natural Deduction Rules for PredCalc

	introduction	elimination	proviso
$\wedge$	$\frac{\varphi \quad \psi}{\varphi \wedge \psi}$	$\frac{\varphi \wedge \psi}{\varphi} \quad \frac{\varphi \wedge \psi}{\psi}$	
$\vee$	$\frac{\varphi \quad \psi}{\varphi \vee \psi} \quad \frac{\psi}{\varphi \vee \psi}$	$\frac{\varphi \vee \psi \quad \varphi \vdash \chi \quad \psi \vdash \chi}{\chi}$	
$\rightarrow$	$\frac{\varphi \vdash \psi}{\varphi \rightarrow \psi}$	$\frac{\varphi \rightarrow \psi \quad \varphi}{\psi} \quad \frac{\varphi \rightarrow \psi \quad \neg \psi}{\neg \varphi}$	
$\perp$	$\frac{\varphi \quad \neg \varphi}{\perp}$	$\frac{\varphi \vdash \perp}{\neg \varphi} \quad \frac{\neg \varphi \vdash \perp}{\varphi}$	
$\neg\neg$	$\frac{\varphi}{\neg\neg\varphi}$	$\frac{\neg\neg\varphi}{\varphi}$	
$=$	$\frac{t = t}{t_1 = t_2}$	$\frac{t_1 = t_2 \quad \varphi(t_1)}{\varphi(t_2)}$	
$\forall$	$\frac{\Gamma \vdash \varphi(x_0)}{\Gamma \vdash \forall x \varphi(x)}$	$\frac{\forall x \varphi(x)}{\varphi(t)}$	$x_0$ does not occur in $\Gamma \cup \{\varphi\}$
$\exists$	$\frac{\varphi(t)}{\exists x \varphi}$	$\frac{\Gamma \vdash \exists x \varphi \quad \Gamma, \varphi(x_0) \vdash \chi}{\Gamma \vdash \chi}$	$x_0$ does not occur in $\Gamma \cup \{\varphi, \chi\}$