Context Free Grammar

CS 585, Fall 2017

Introduction to Natural Language Processing

http://people.cs.umass.edu/~brenocon/inlp2017

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- Syntax: how do words structurally combine to form sentences and meaning?

- Representations
  - Constituents
    - [the big dogs] chase cats
    - [colorless green clouds] chase cats
  - Dependencies
    - The **dog chased** the cat.
    - My **dog**, a big old one, **chased** the cat.

- Idea of a *grammar (G)*: global template for how sentences / utterances / phrases *w* are formed, via latent syntactic structure *y*
  - Linguistics: what do G and P(w,y | G) look like?
  - Generation: score with, or sample from, P(w, y | G)
  - Parsing: predict P(y | w, G)

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[Examples from Eisenstein (2017)]

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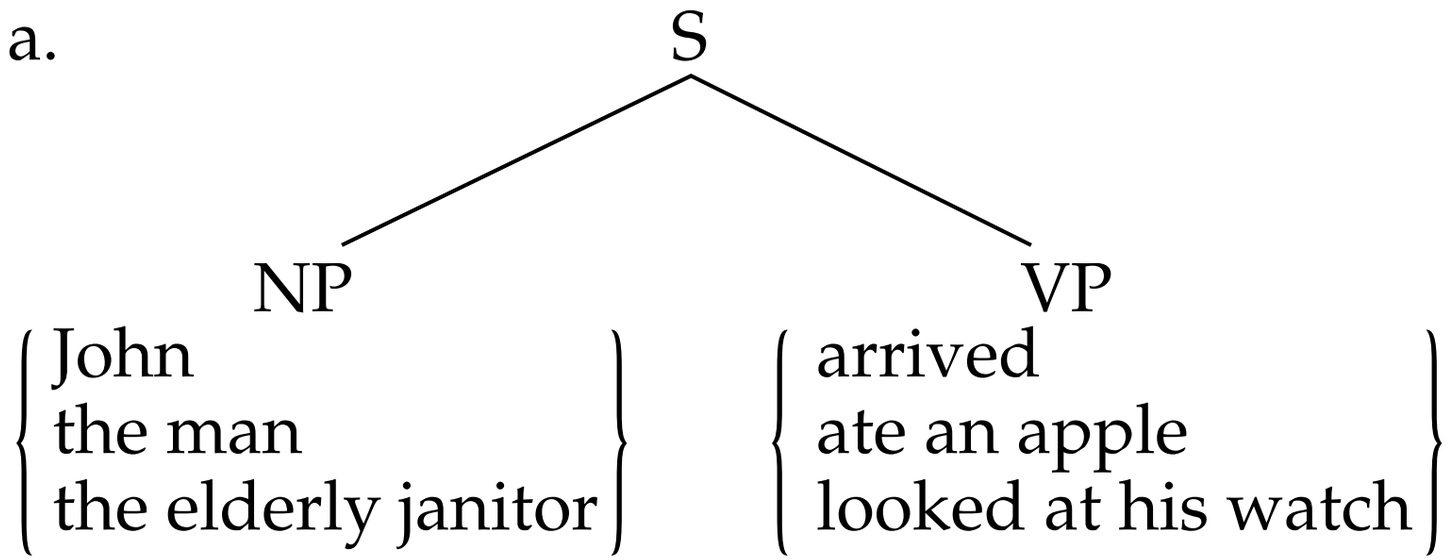
- Competence vs. Performance?

[Examples from Eisenstein (2017)]

Hierarchical view of syntax

- "a Sentence made of Noun Phrase followed by a Verb Phrase"

a.



b. S → NP VP (1)

[From Phillips (2003)]

Is language context-free?

- Practical examples where nesting seems like a useful explanation
  - *The **processor** **has** I0 million times fewer transistors on it than todays typical micro- processors, **runs** much more slowly, and **operates** at five times the voltage...*

- $S \rightarrow NN\ VP$
  $VP \rightarrow VP3S \mid VPN3S \mid \ldots$
  $VP3S \rightarrow VP3S, VP3S, \text{and } VP3S \mid VBZ \mid VBZ\ NP \mid \ldots$

[Examples from Eisenstein (2017)]

- Regular language <=> RegEx <=> paths in finite state machine
- Context-free language <=> CFG <=> derivations in pushdown automaton

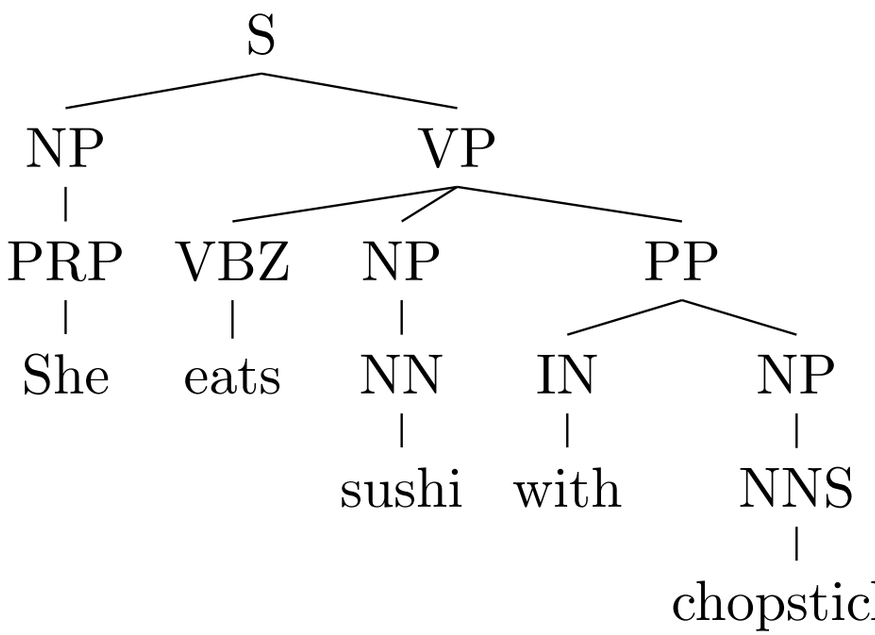
- A context-free grammar is a 4-tuple:

N a set of non-terminals
Σ a set of terminals (distinct from N)
R a set of productions, each of the form $A \rightarrow \beta$, where $A \in N$ and $\beta \in (\Sigma \cup N)^*$
S a designated start symbol

- Derivation: sequence of rewrite steps from S to a string (sequence of terminals, i.e. words)
- Yield: the final string

- A CFG is a "boolean language model"
- A probabilistic CFG is a probabilistic language model:
  - Every production rule has a probability; defines prob dist. over strings.

Example



(S(NP(PRP *She*)(VP(VBZ *eats*)
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- [Parse tree representations: Nested parens *or* non-terminal spans]

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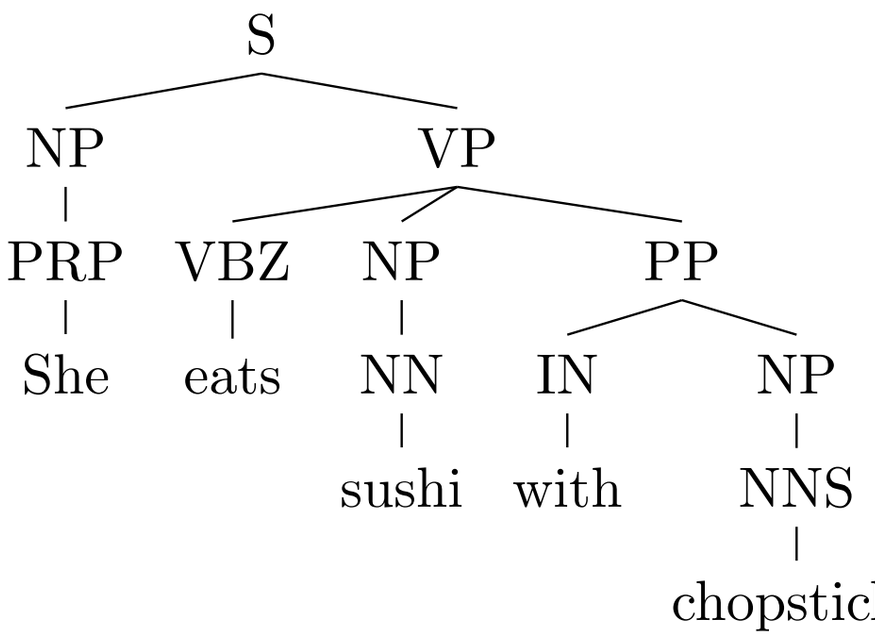

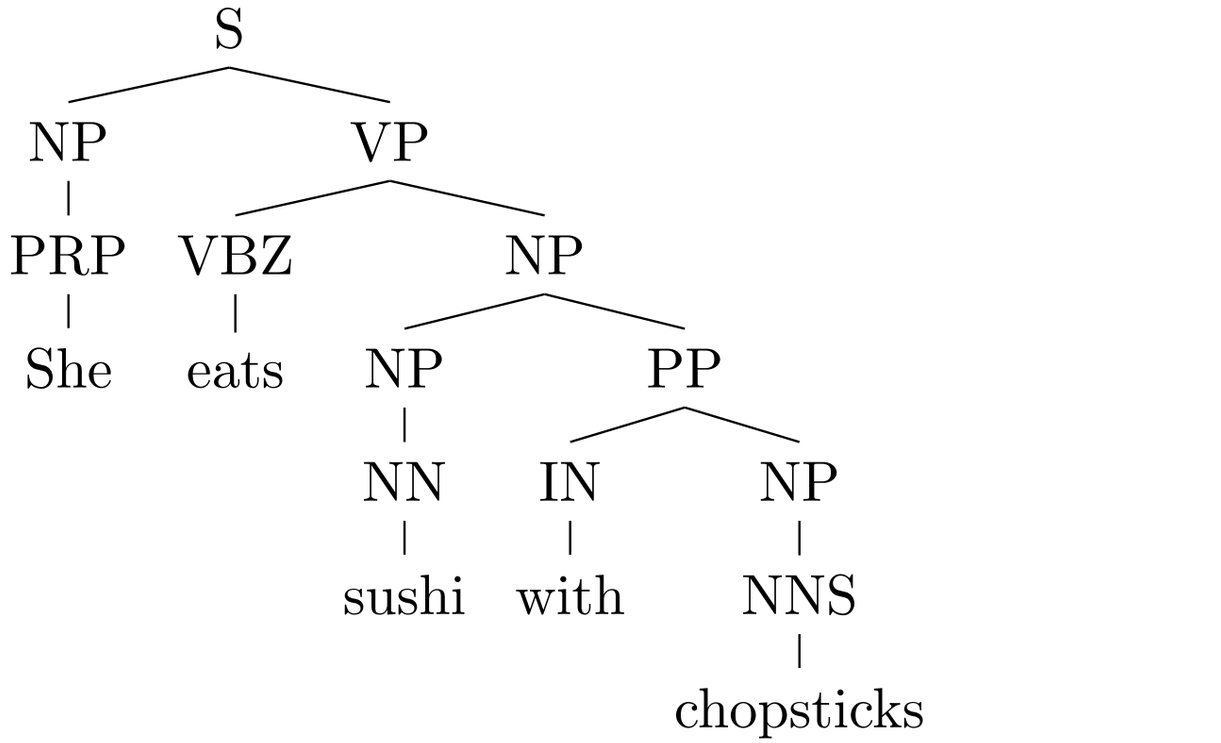

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Constituents

- Constituent tree/parse is one representation of sentence's syntax. What should be considered a constituent, or constituents of the same category?
  - Substitution tests
  - Pronoun substitution
  - Coordination tests

- Simple grammar of English
  - Must balance *overgeneration* versus *undergeneration*
  - Noun phrases
  - NP modification: adjectives, PPs
  - Verb phrases
  - Coordination...

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Parsing with a CFG

- Task: given text and a CFG, answer:
  - Does there exist at least one parse?
  - Enumerate parses (backpointers)

- Cocke-Kasami-Younger algorithm
  - Bottom-up dynamic programming:
    Find possible nonterminals for short spans of sentence, then possible combinations for higher spans
  - Requires converting CFG to Chomsky Normal Form (a.k.a. binarization)

CKY

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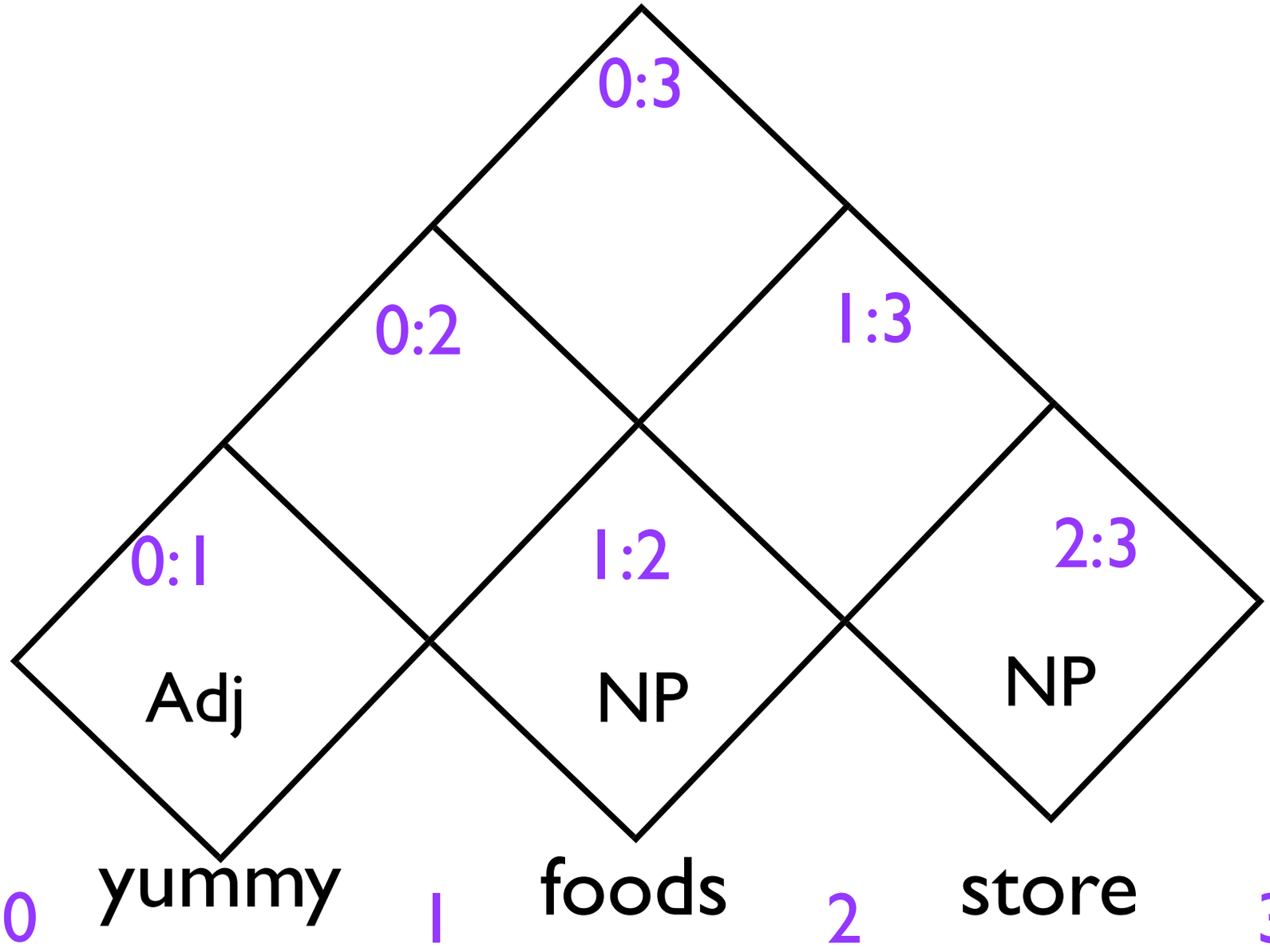

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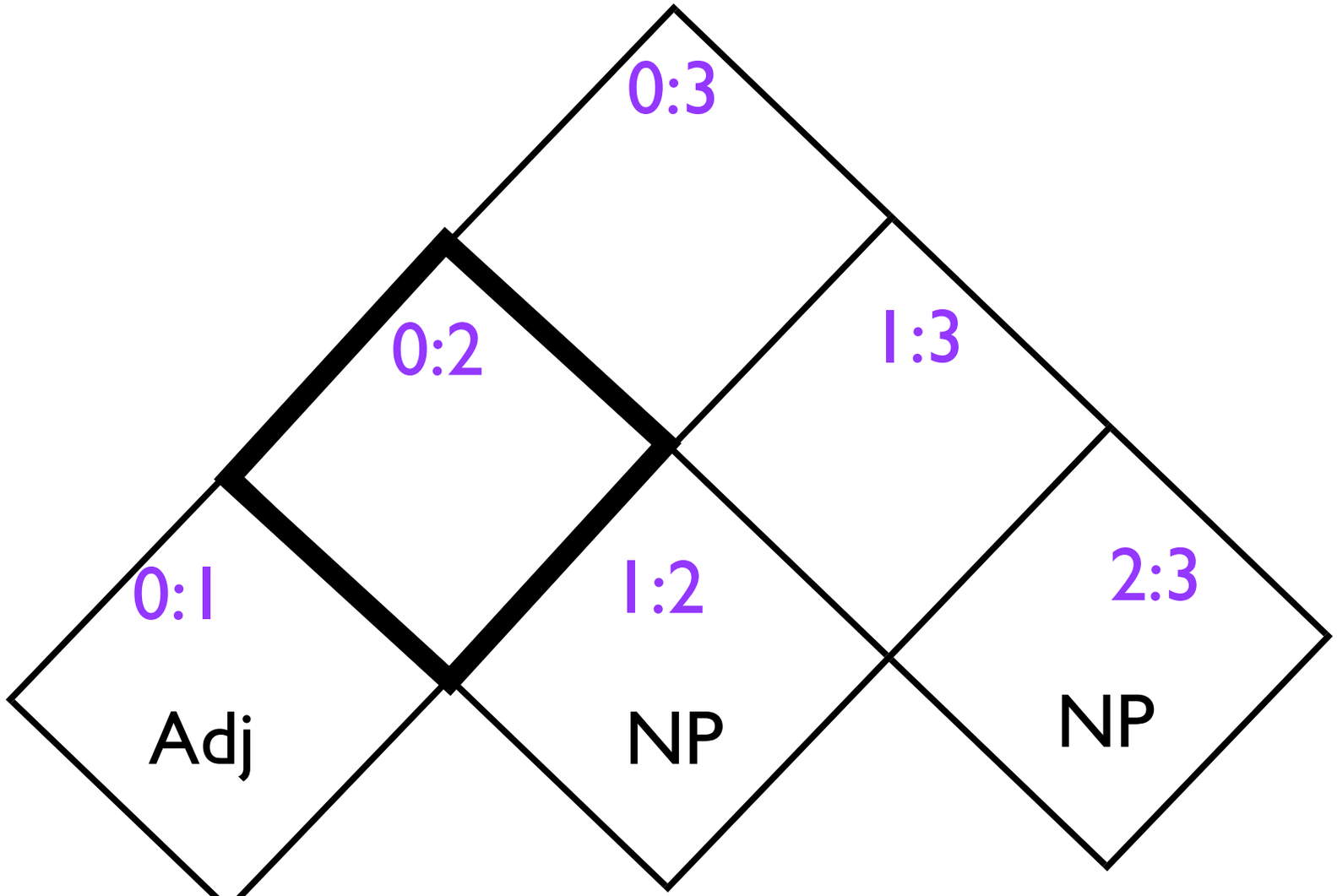

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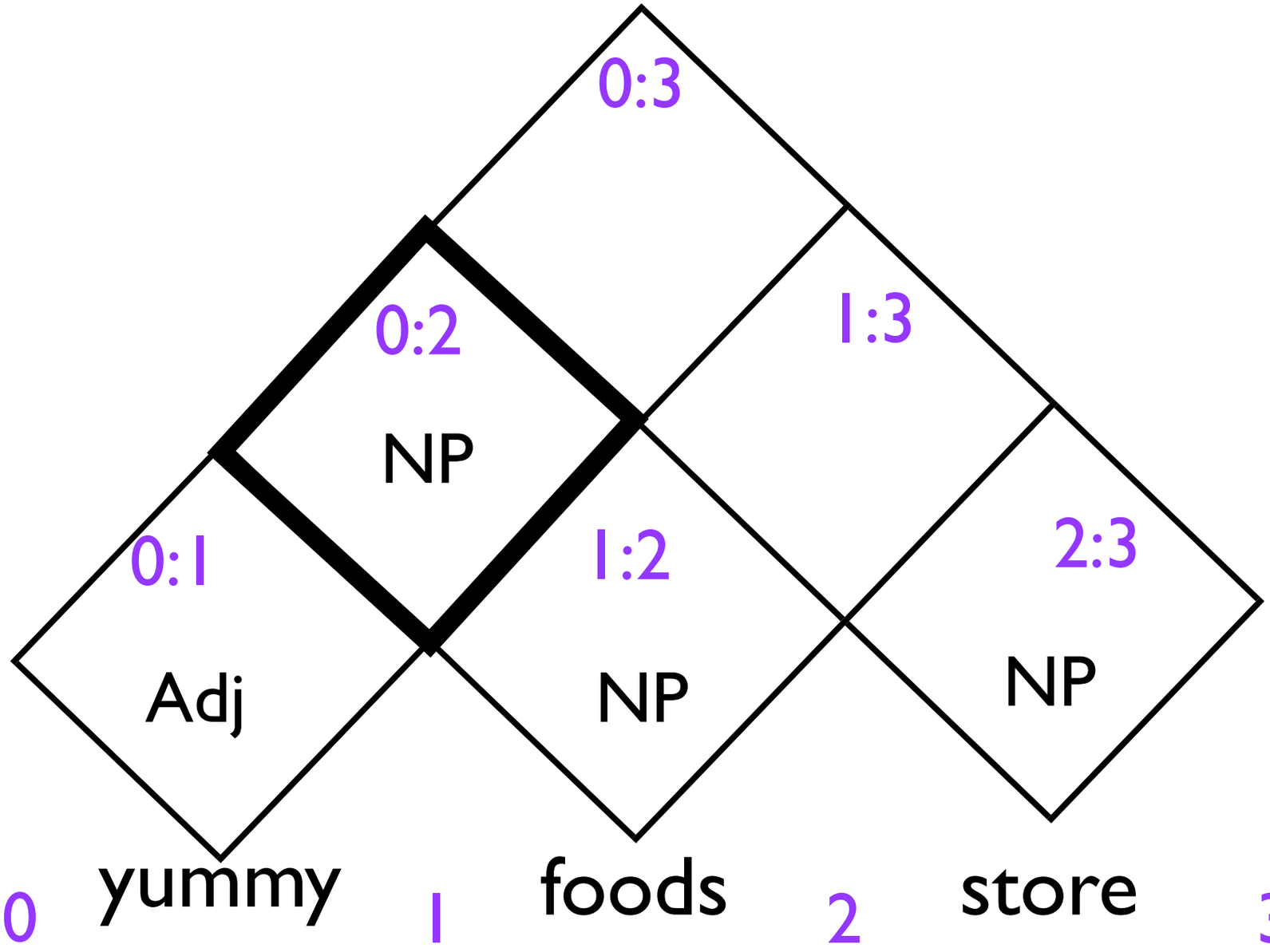

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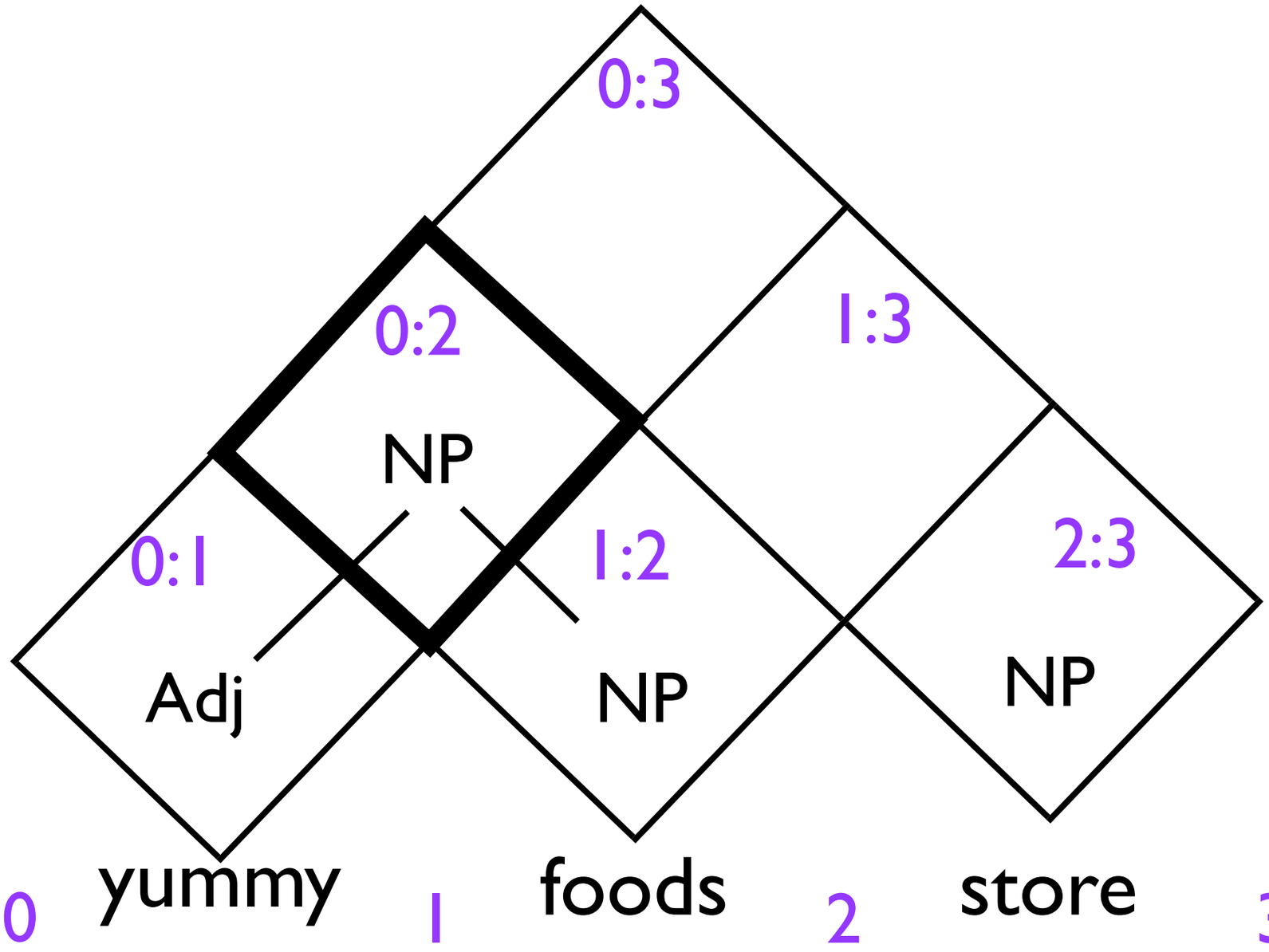

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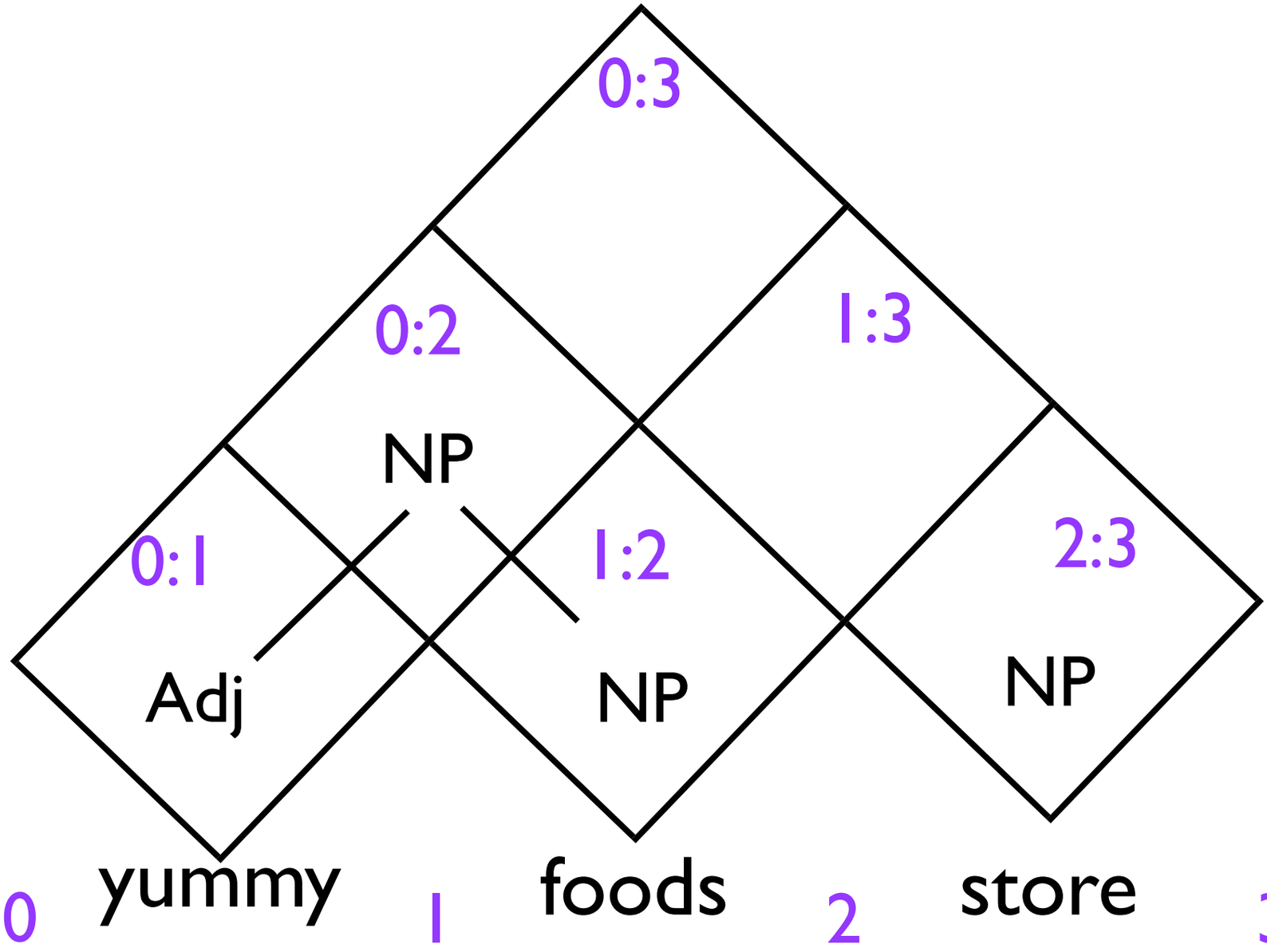

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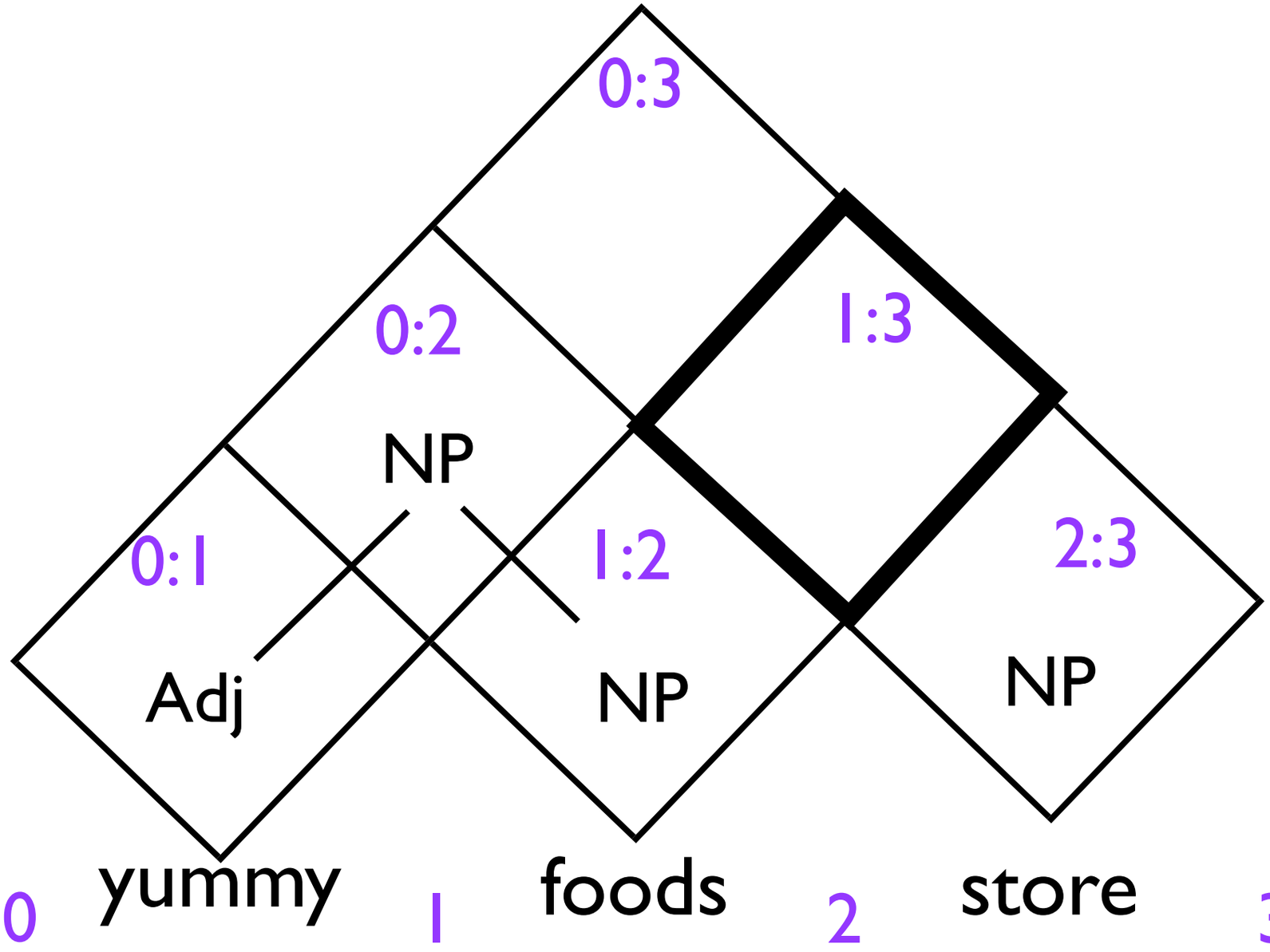

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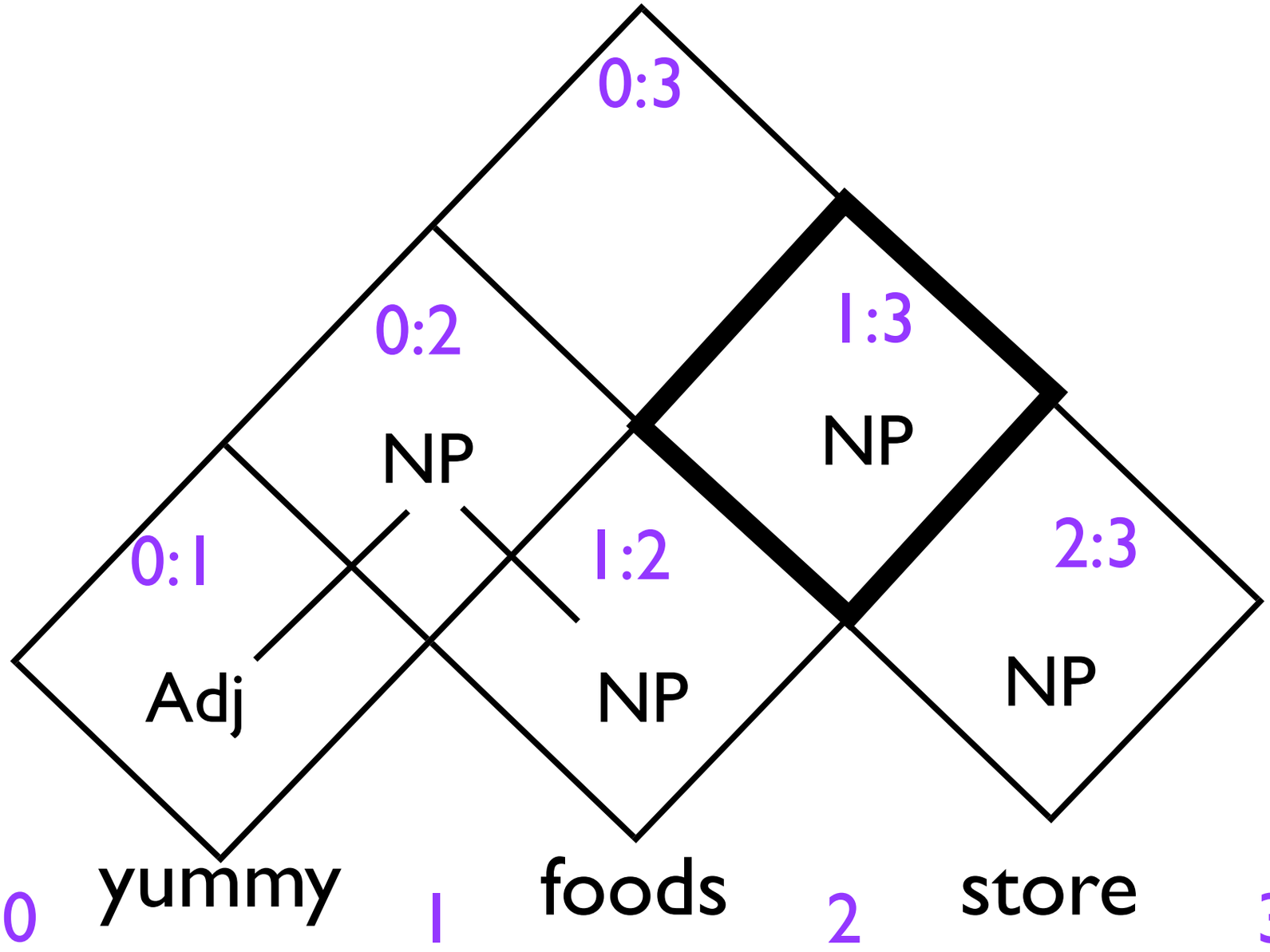

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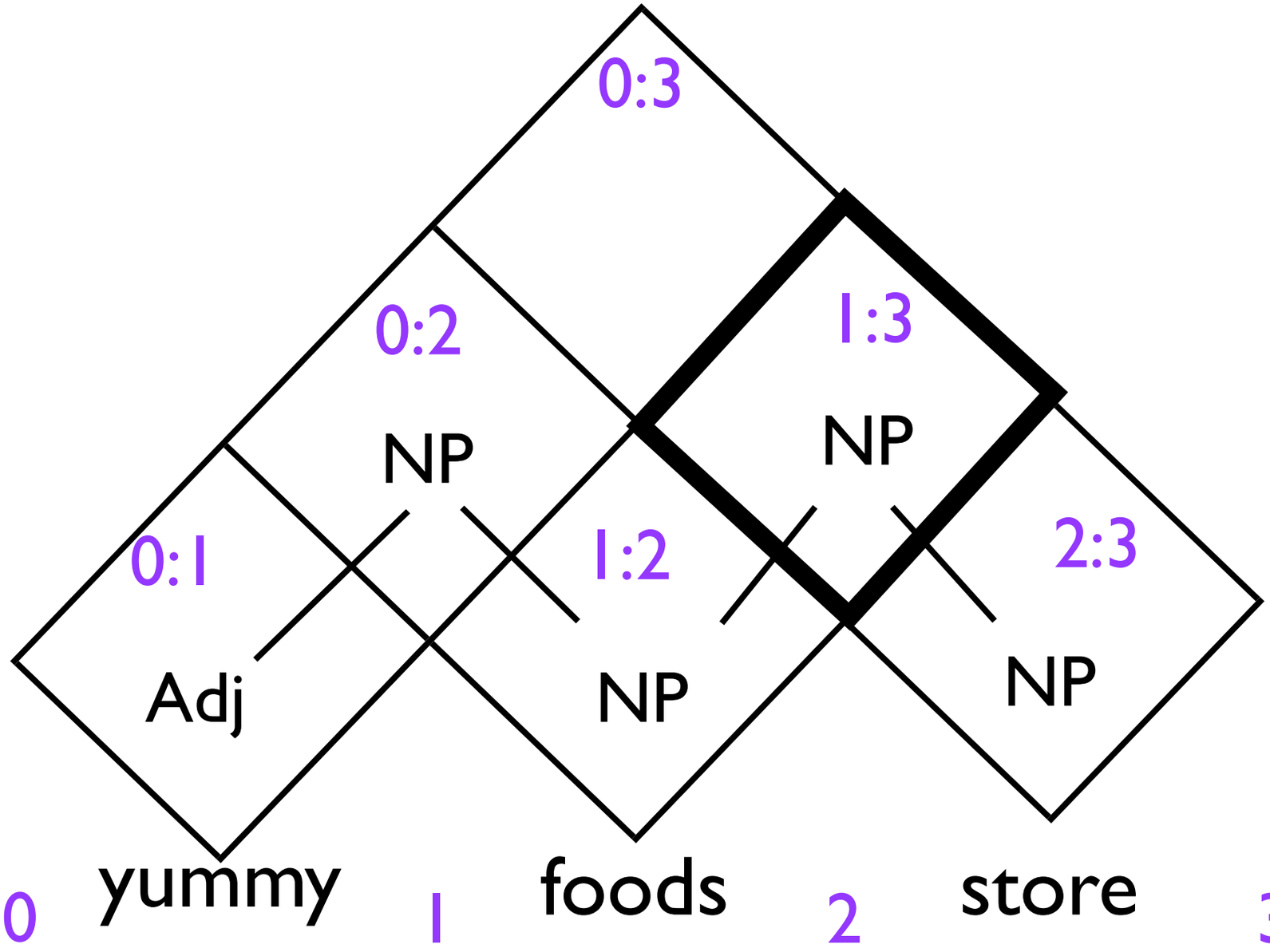

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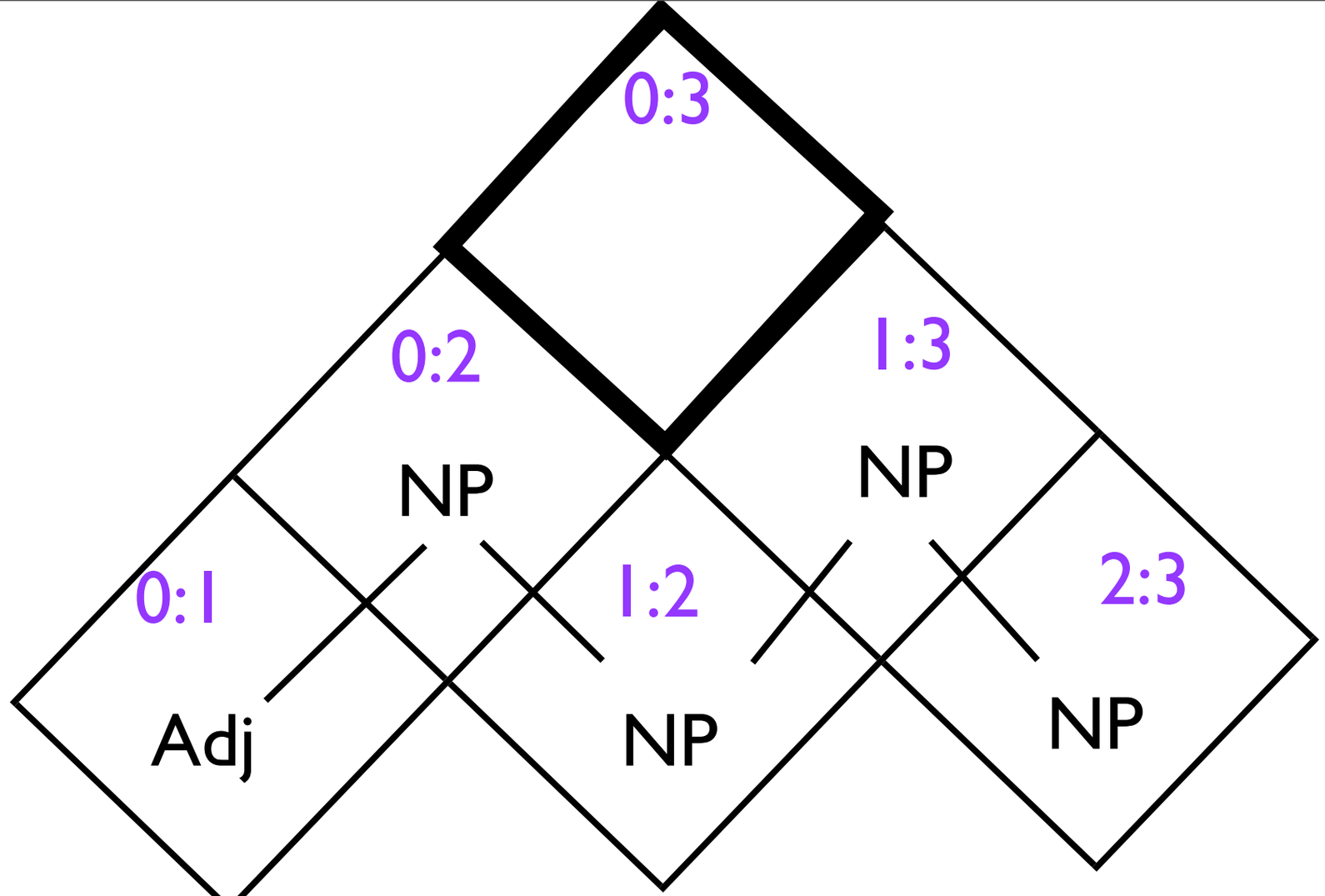

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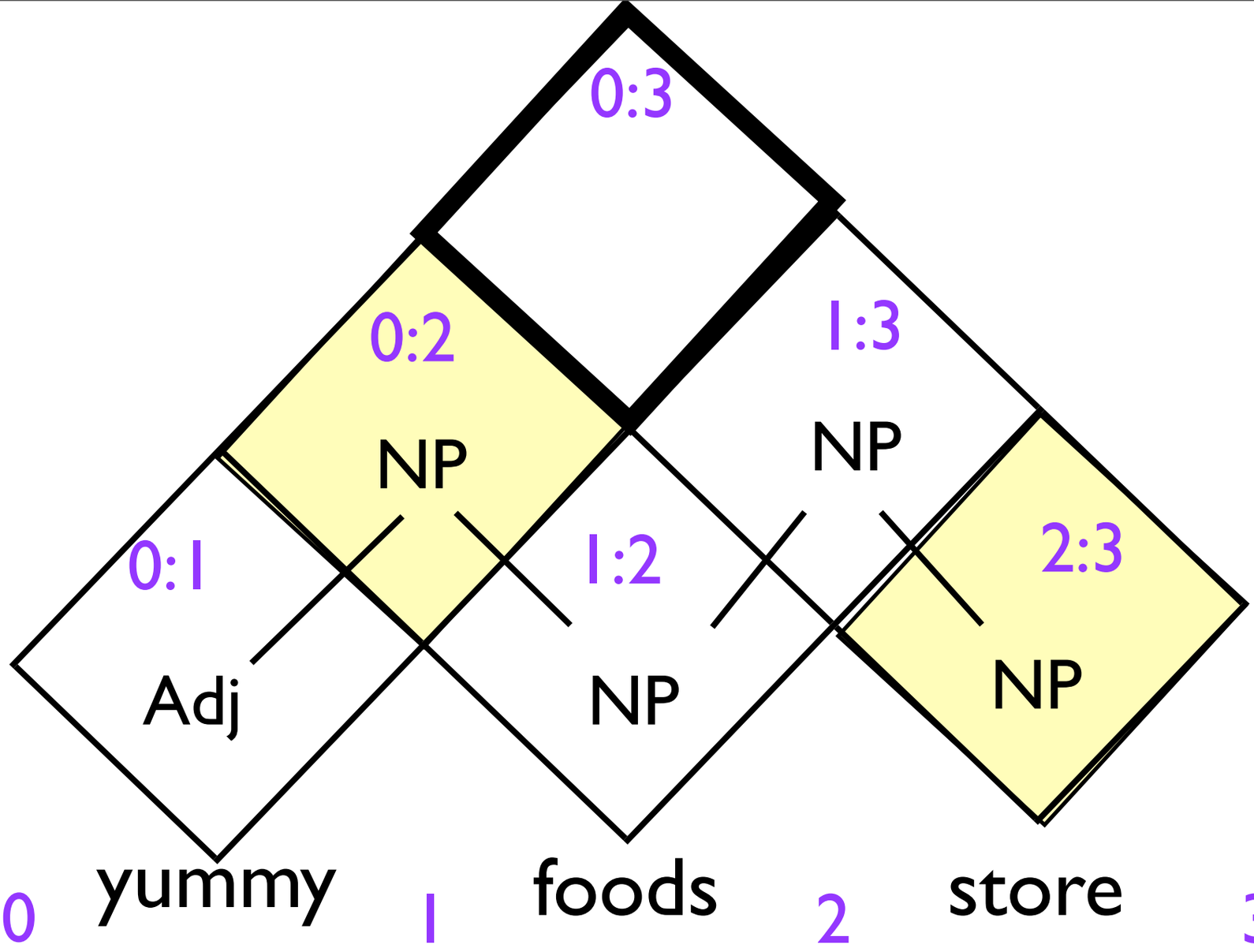

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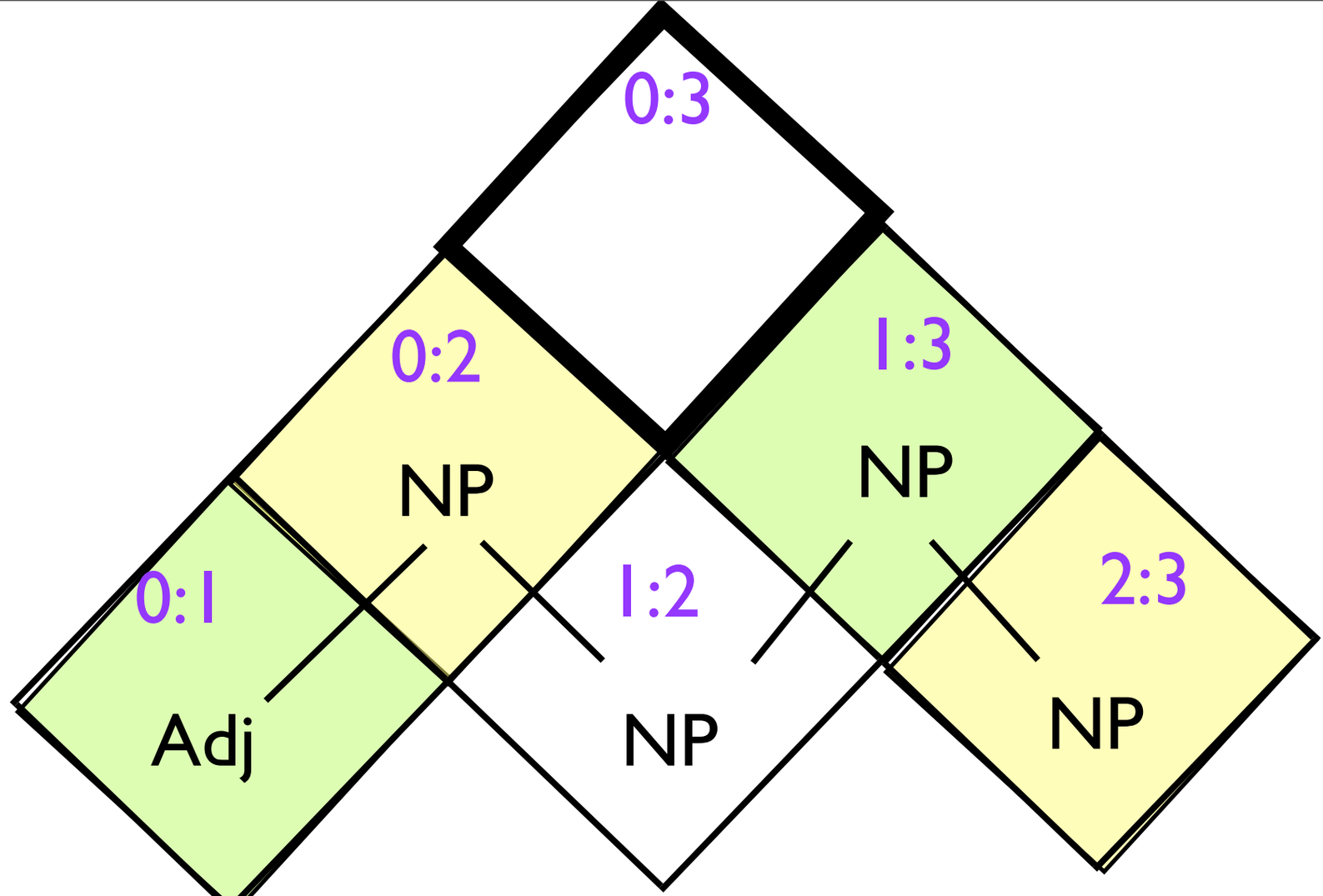

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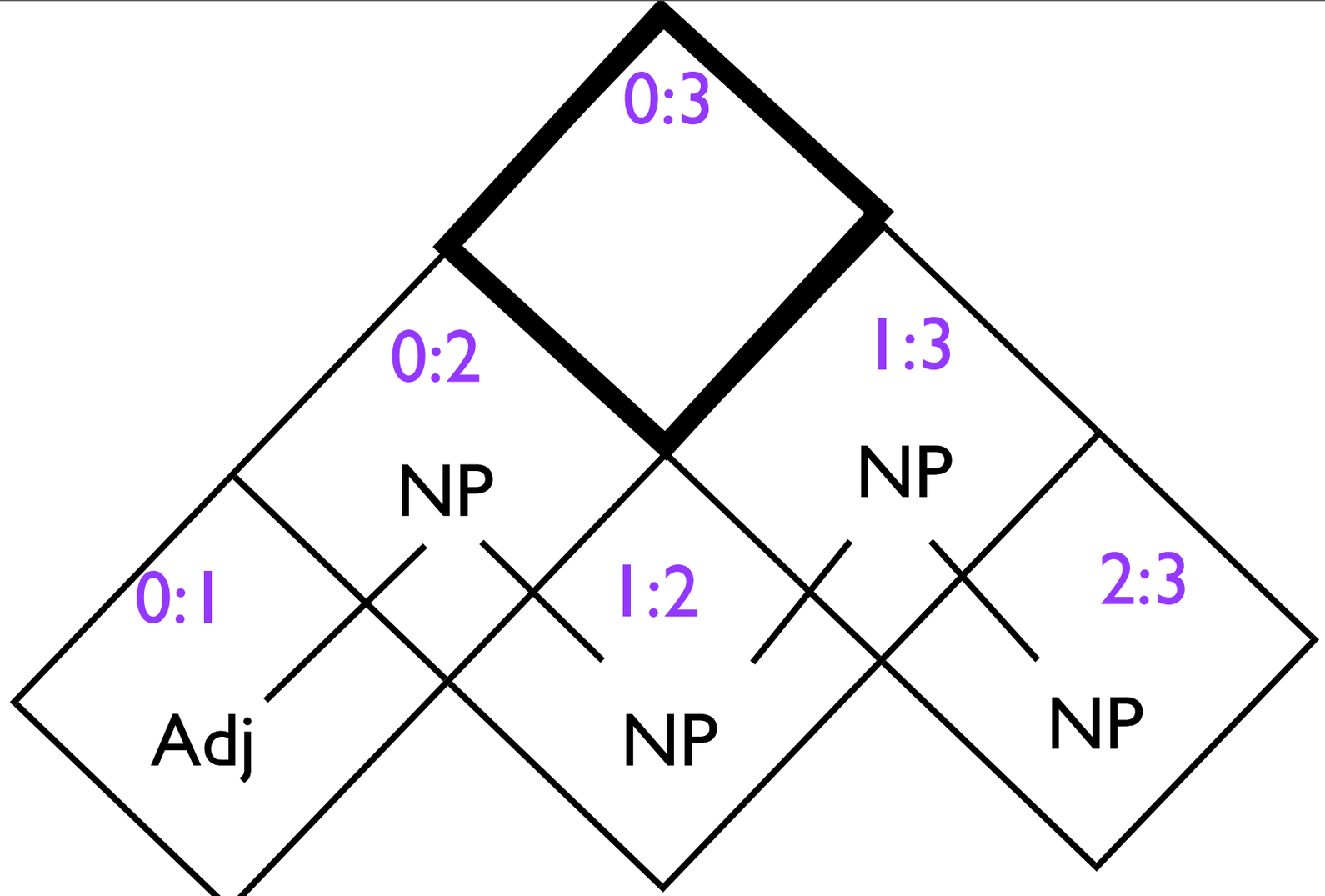

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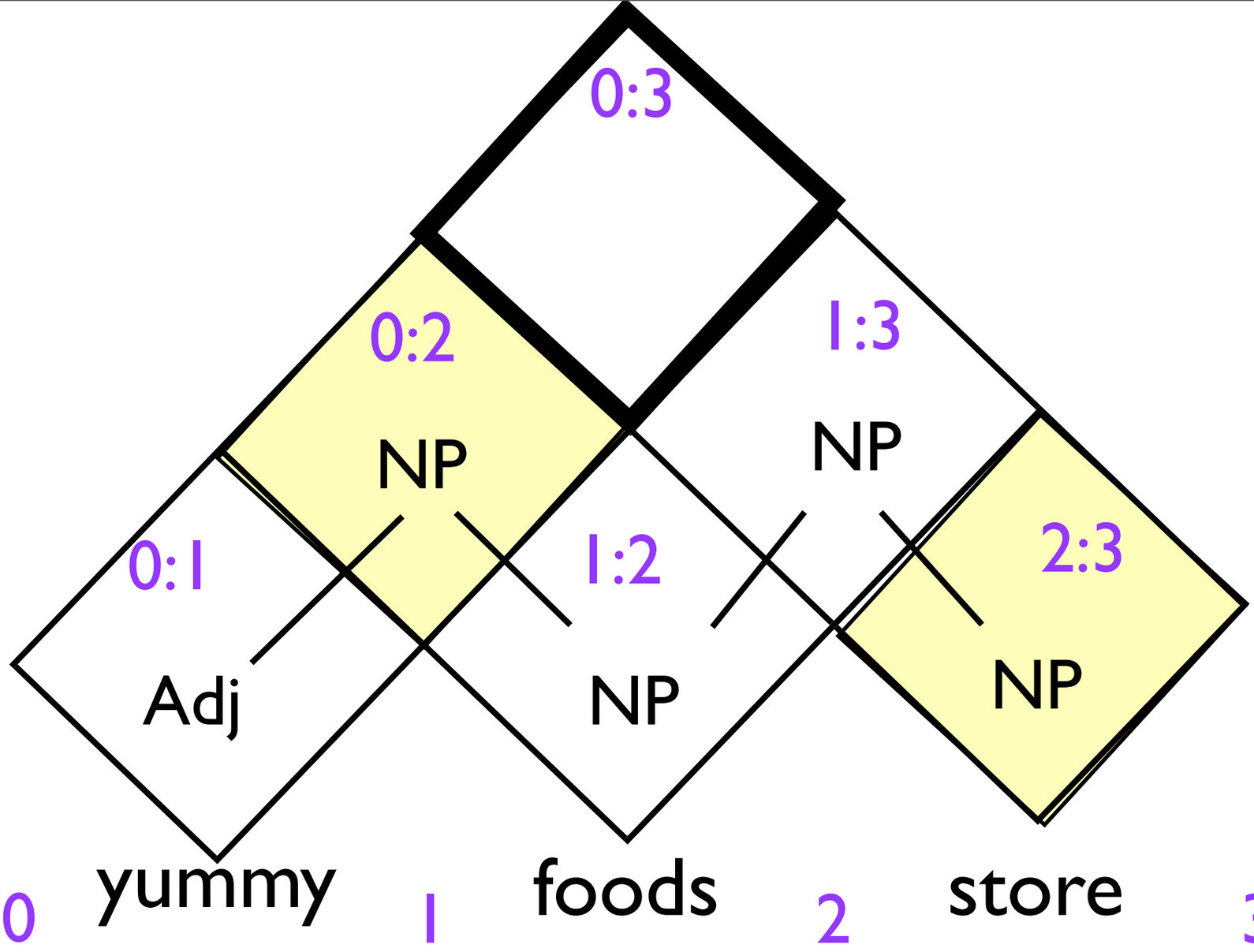

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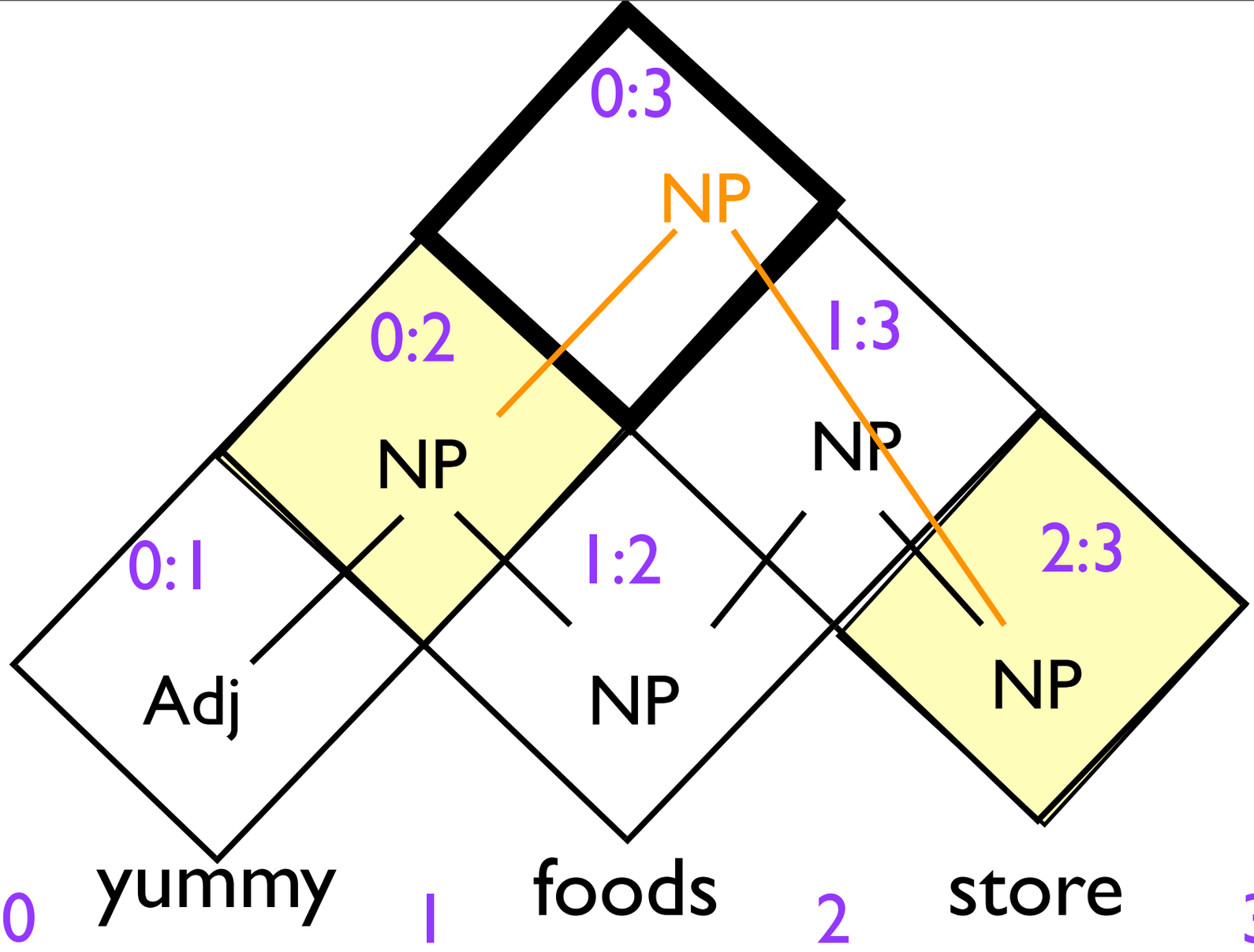

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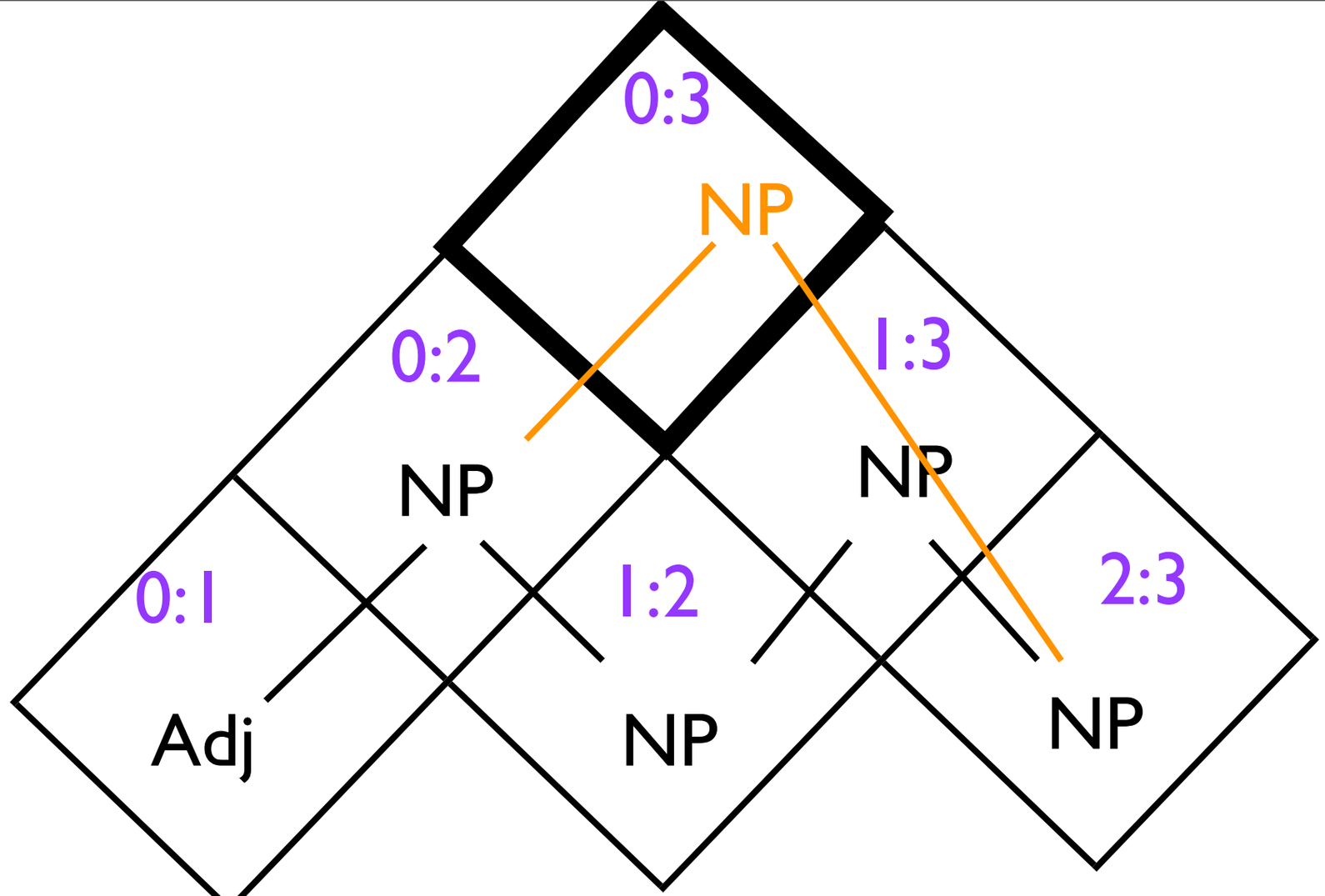

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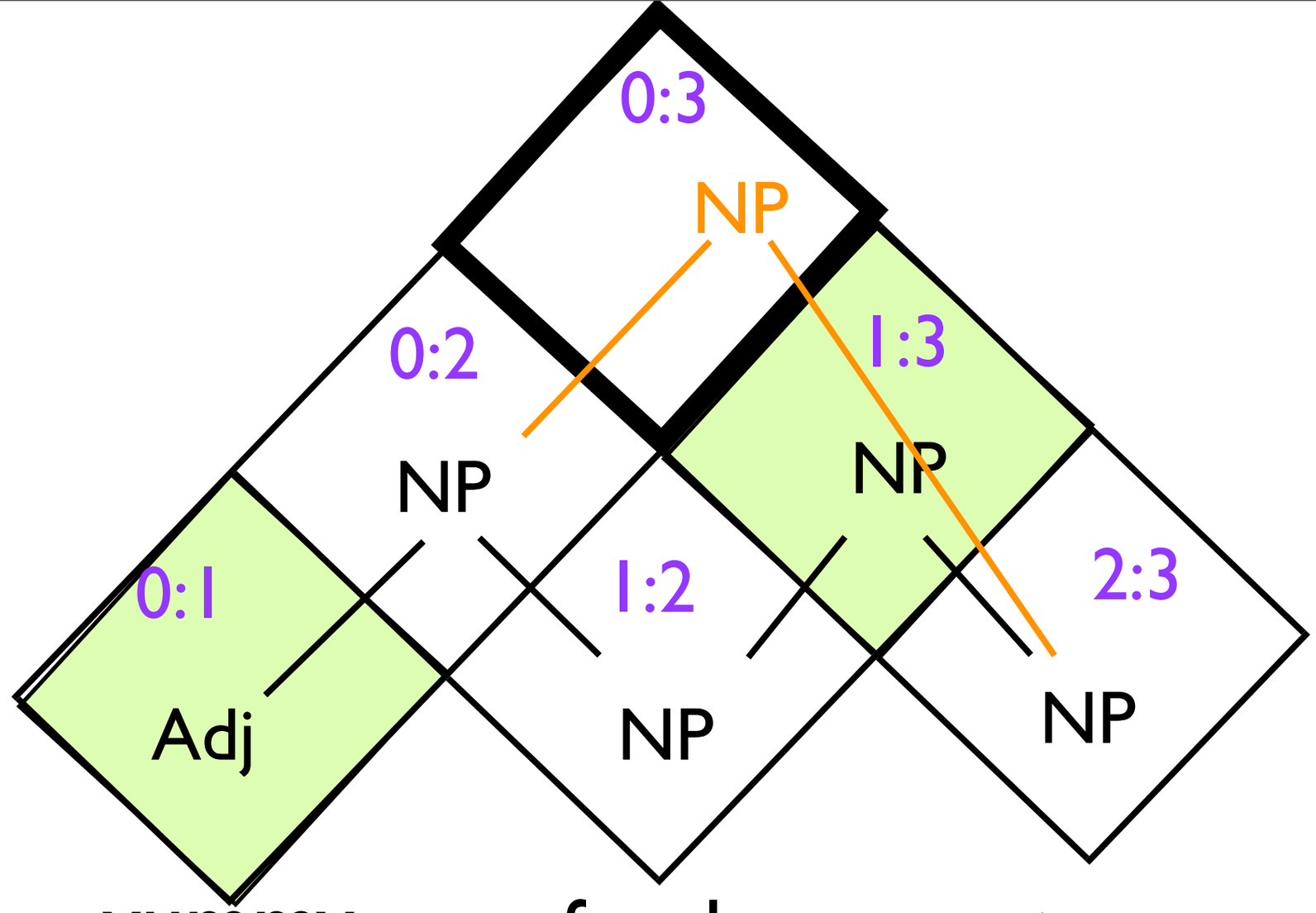

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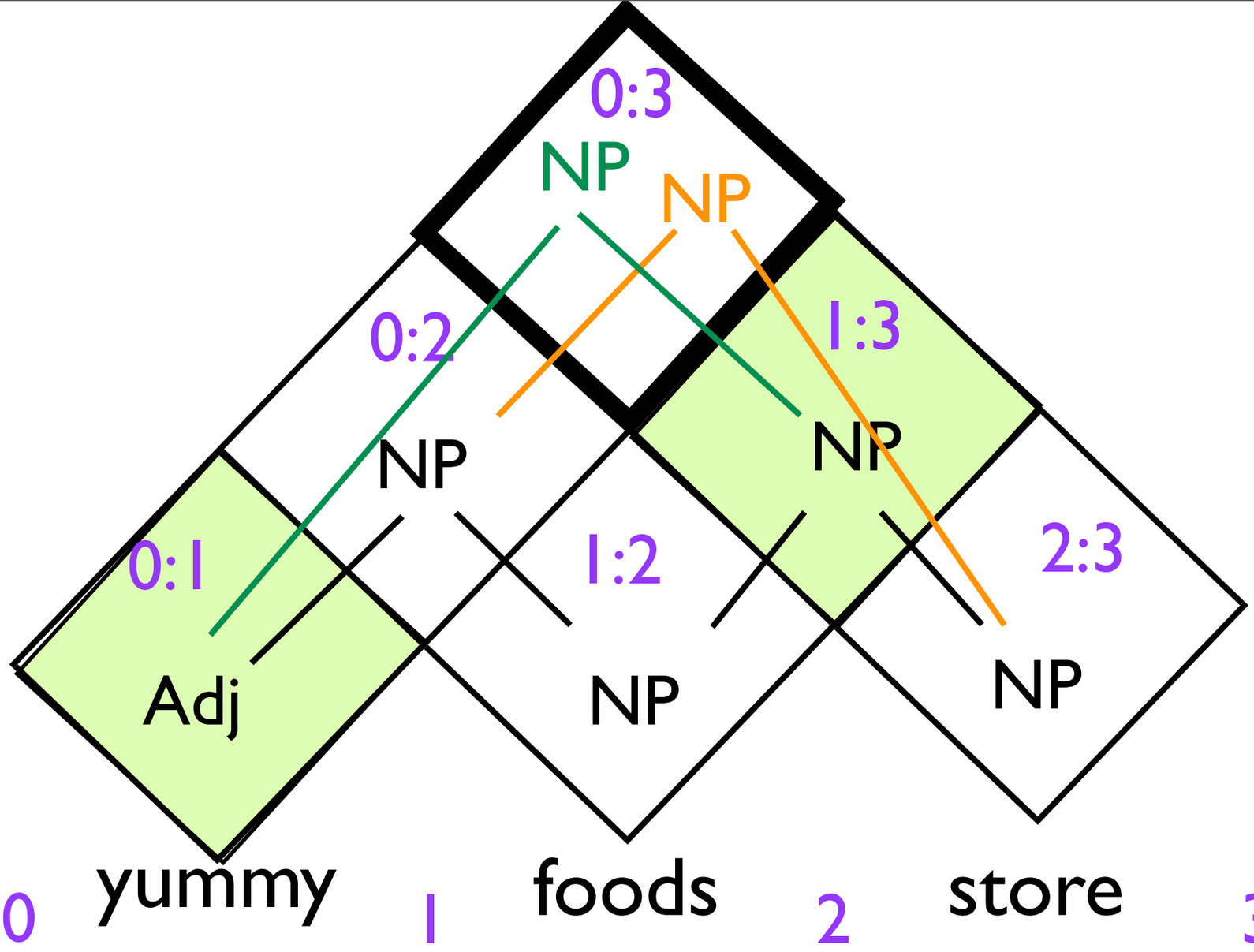

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